



Faculty of Science

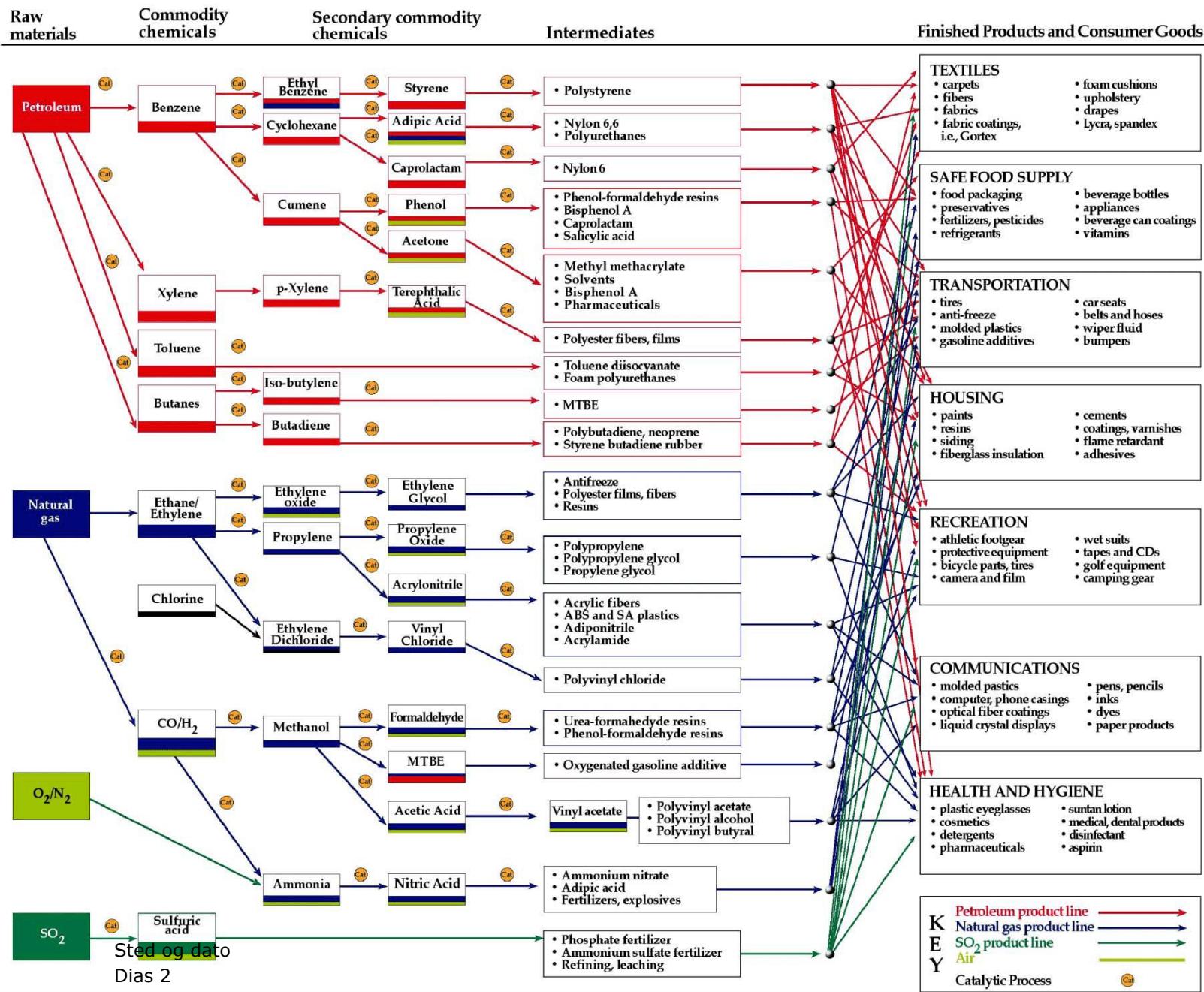


# (Towards)-Modelling the Electrochemical Interface

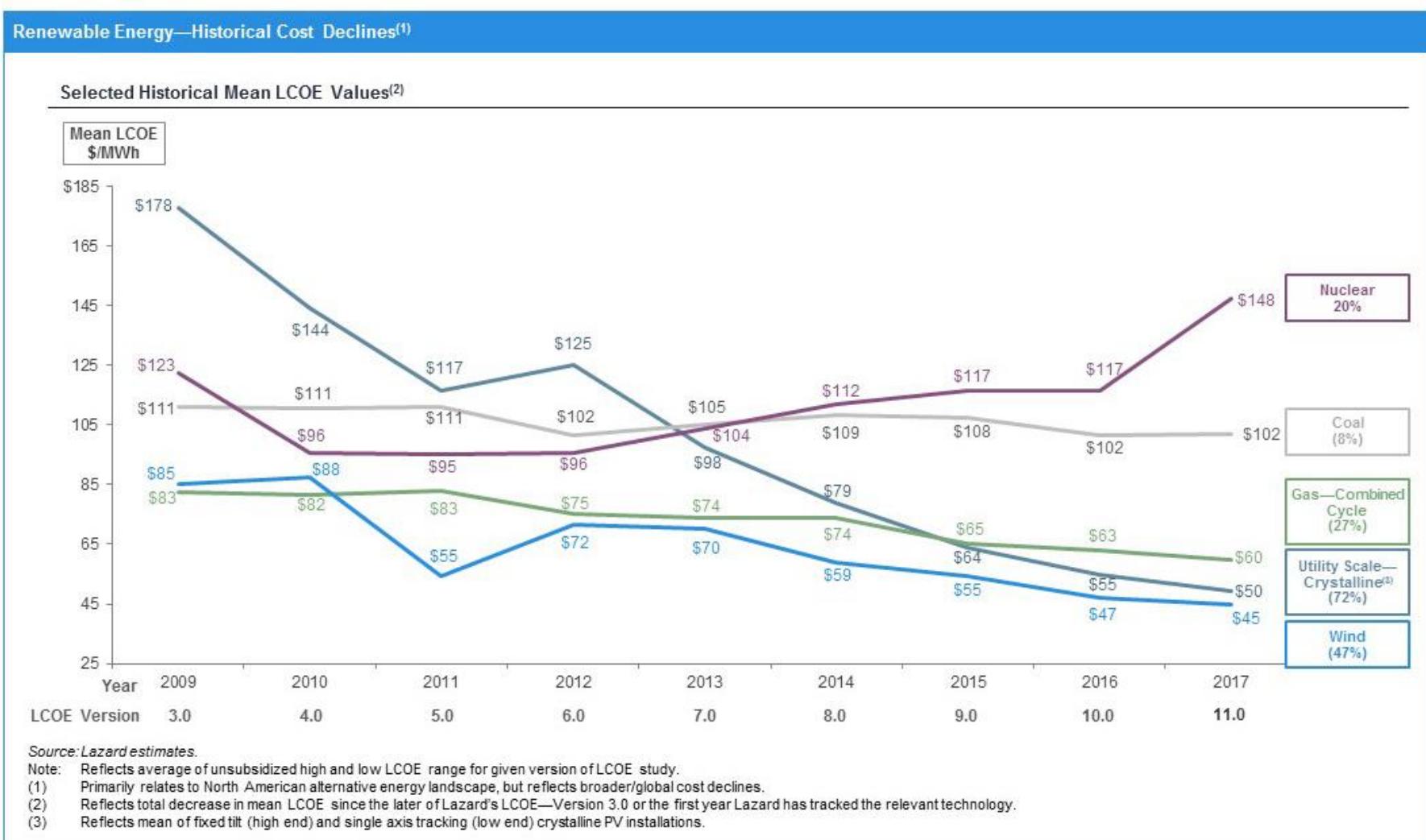
Jan Rossmeisl.

Department of Chemistry  
University of Copenhagen



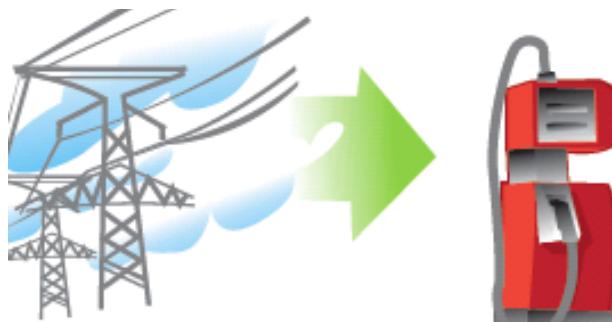


# Future: cheap (free) electricity



# Electrochemical Energy Conversion

Electric energy

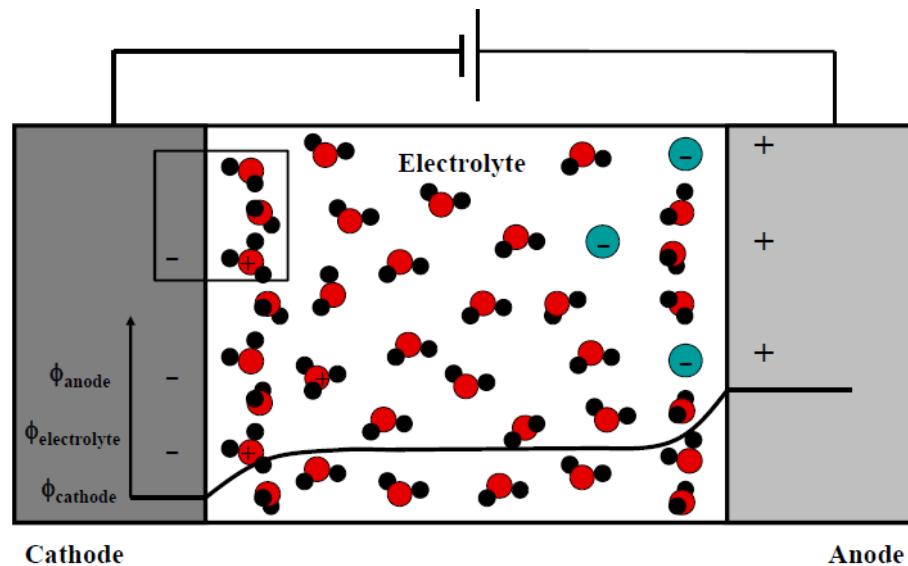


Chemical energy

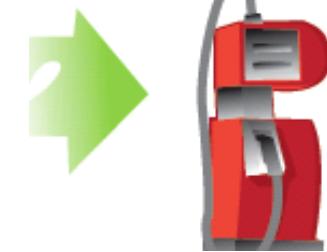


# Challenge, control the surface chemistry

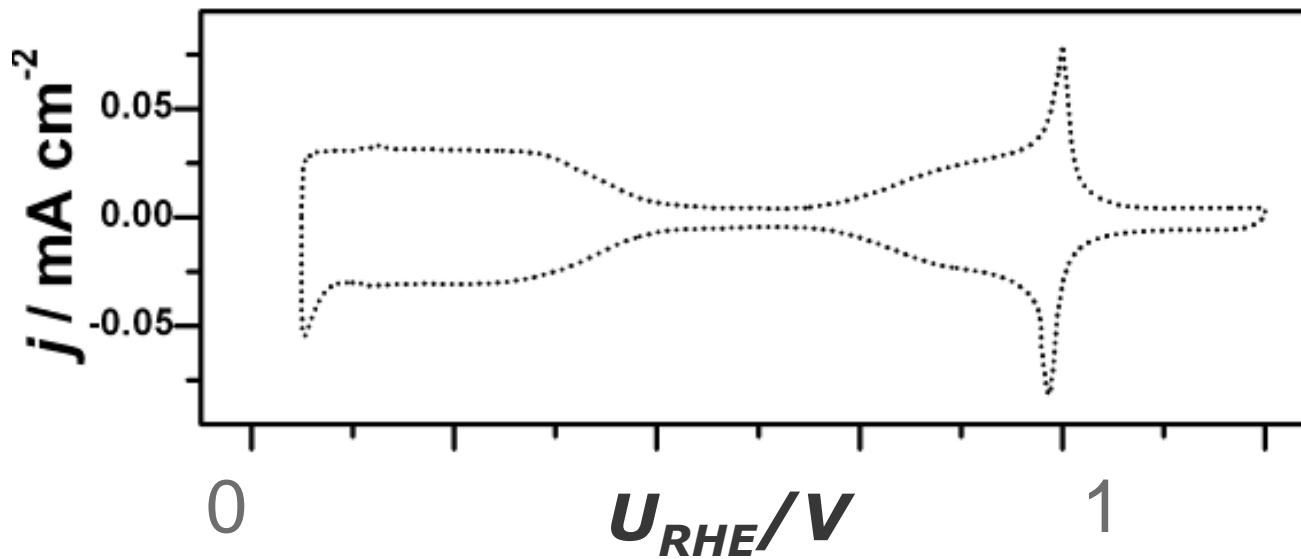
Electric energy

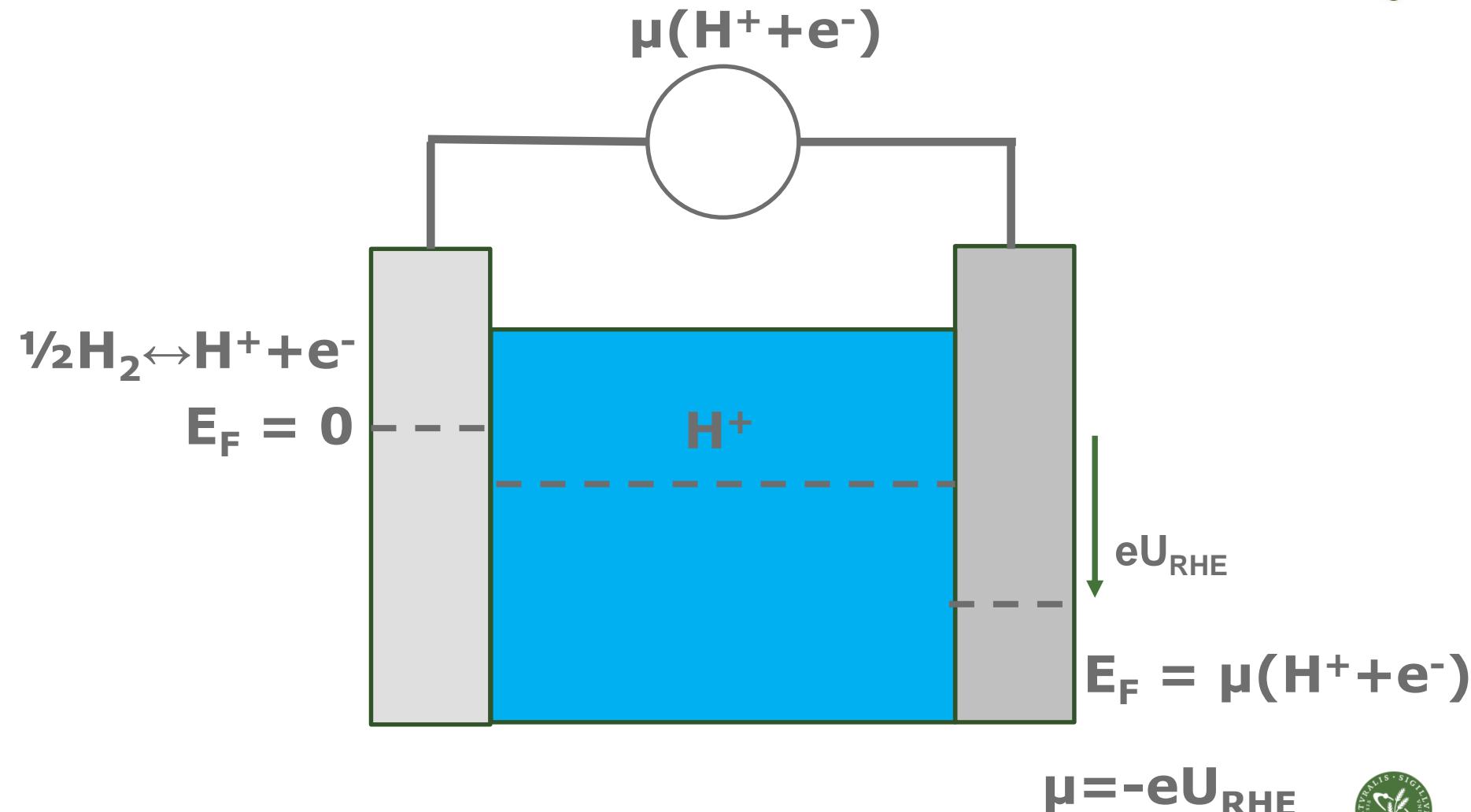


Chemical energy

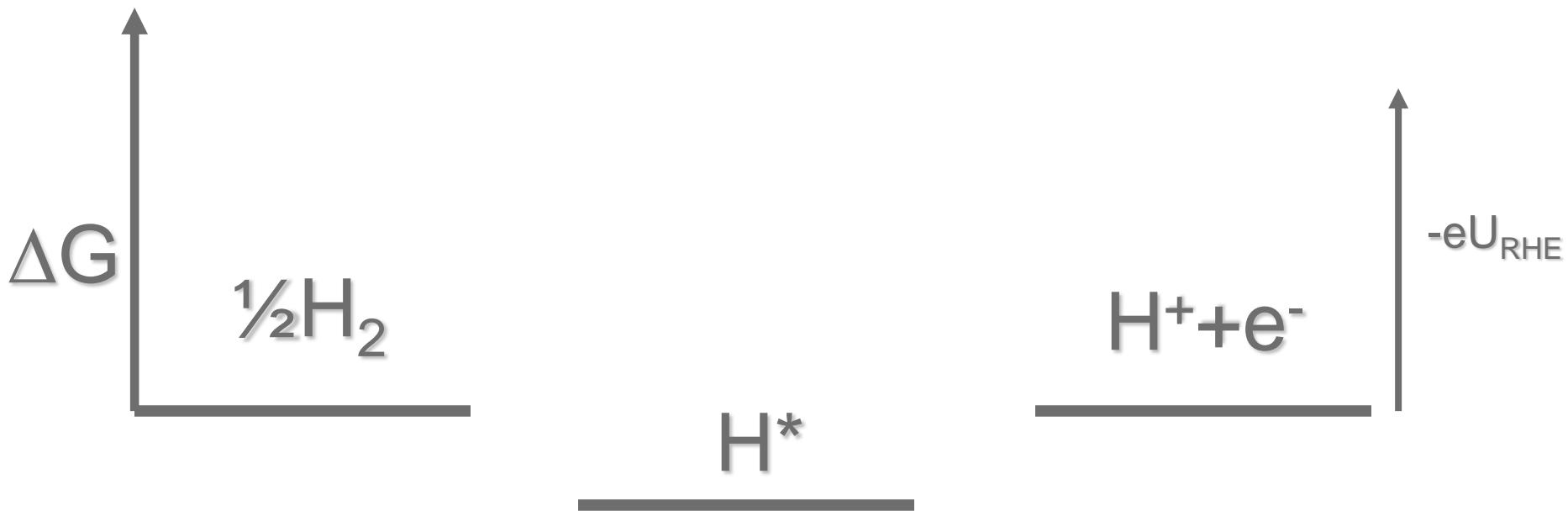


# Why use DFT

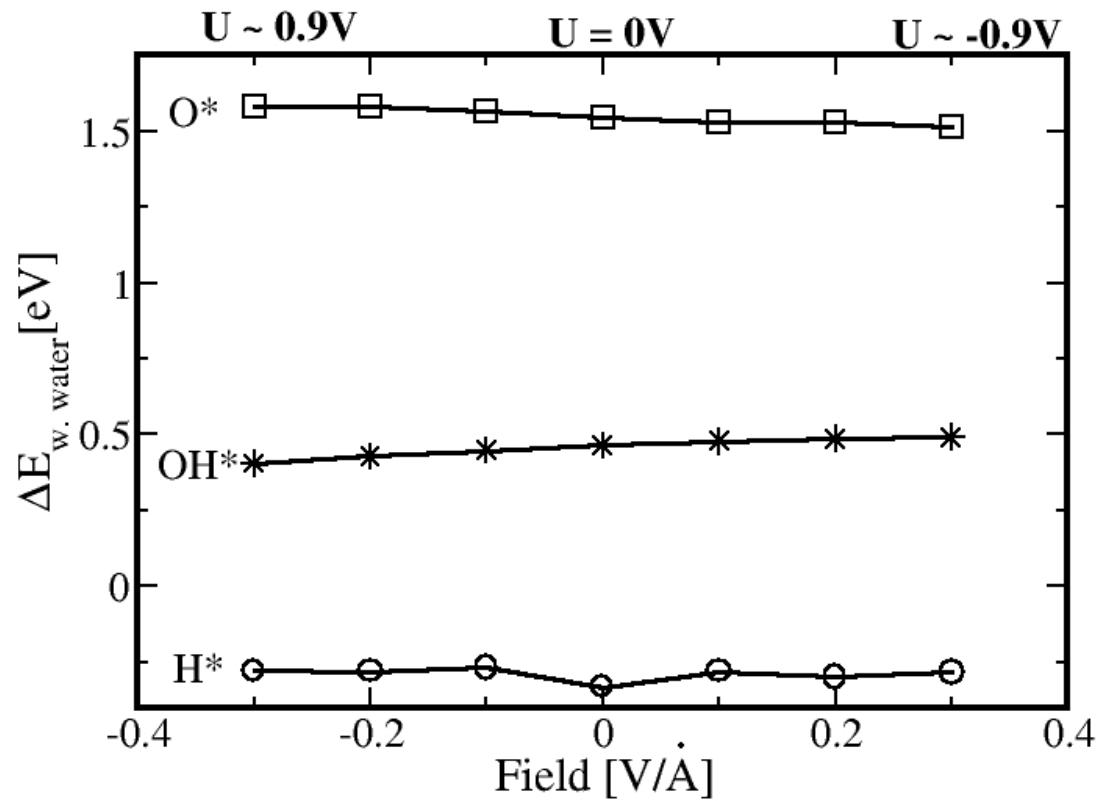
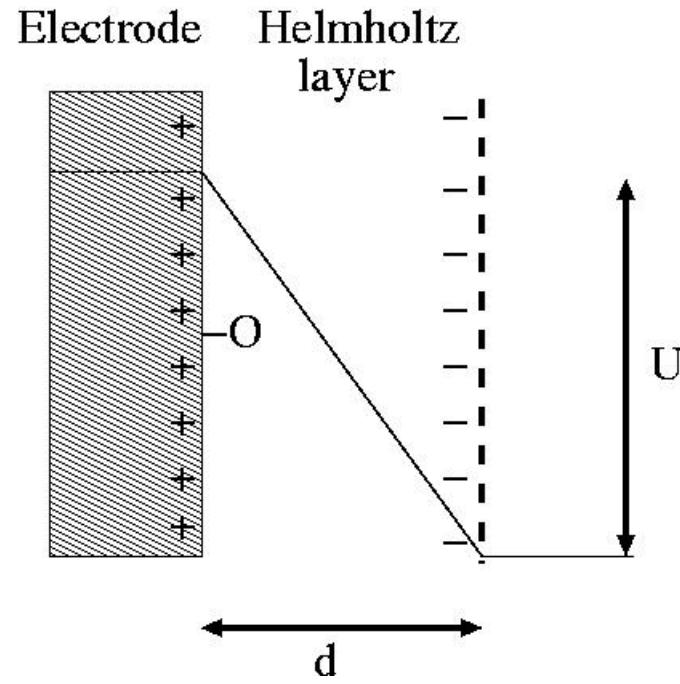




# Computational Hydrogen Electrode



# Field effects



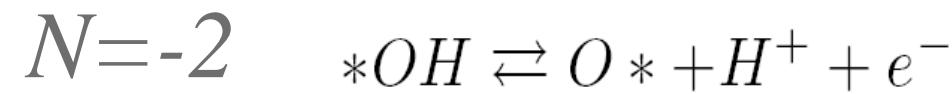
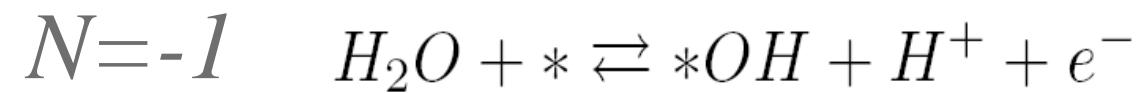
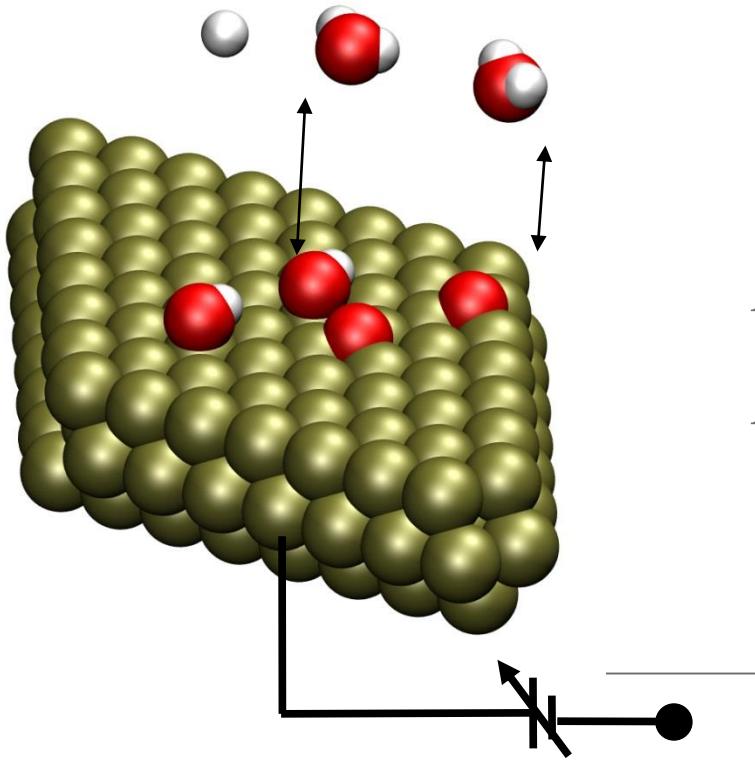
Rossmeisl, Nørskov, Taylor, Janik,  
Neurock. *J. Phys. Chem. B* **110**,  
(2006), 21833-21839

Karlberg, Rossmeisl, Nørskov, PCCP, 9 (2007)  
5158



# Evaluate energy of the surface as function of the potential

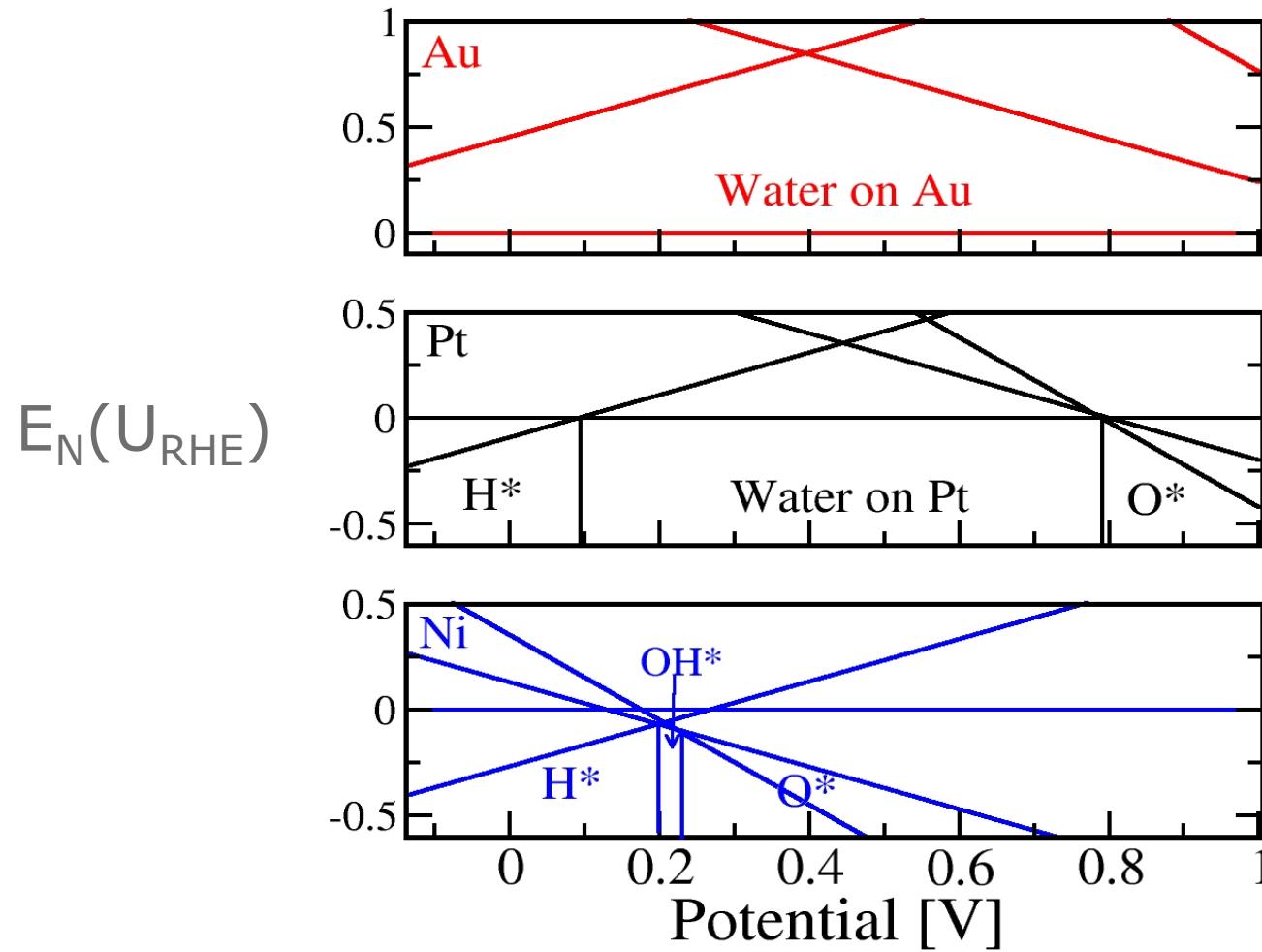
$$E_N(U_{\text{RHE}}) = E(N) - E(0) - \frac{1}{2}NG(H_2) - \frac{1}{2}NeU_{\text{RHE}}$$



U vs. RHE



# Phase-diagrams

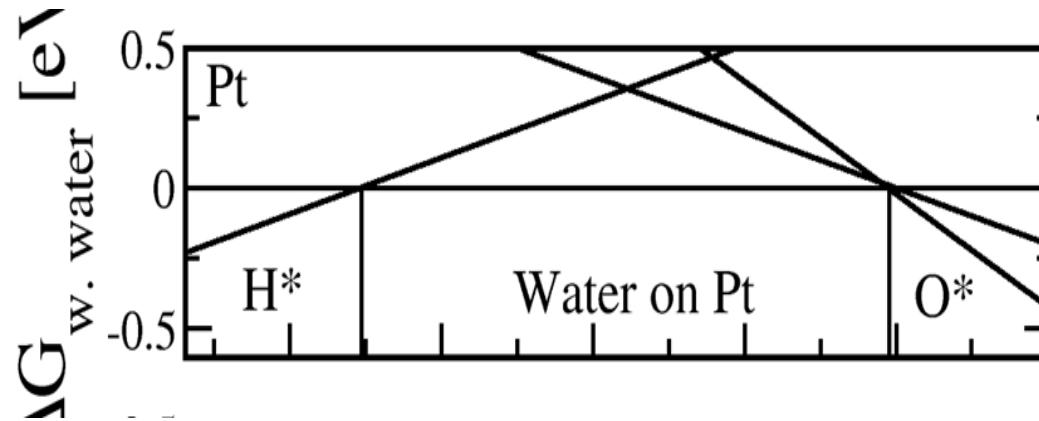
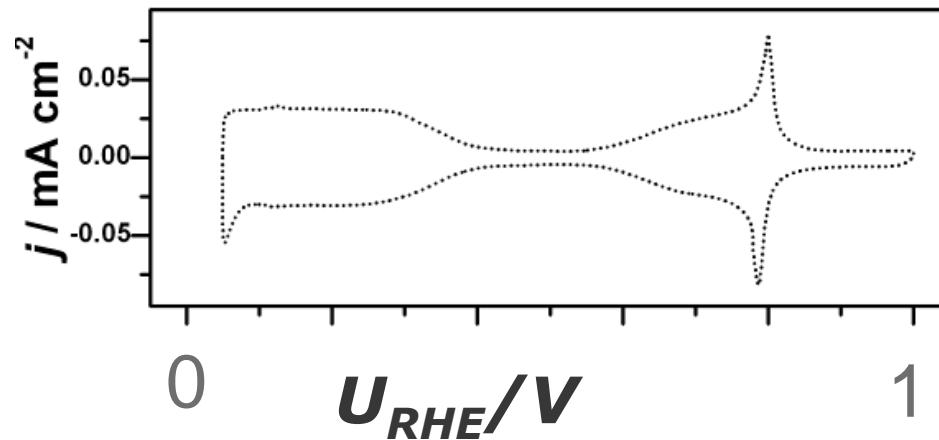


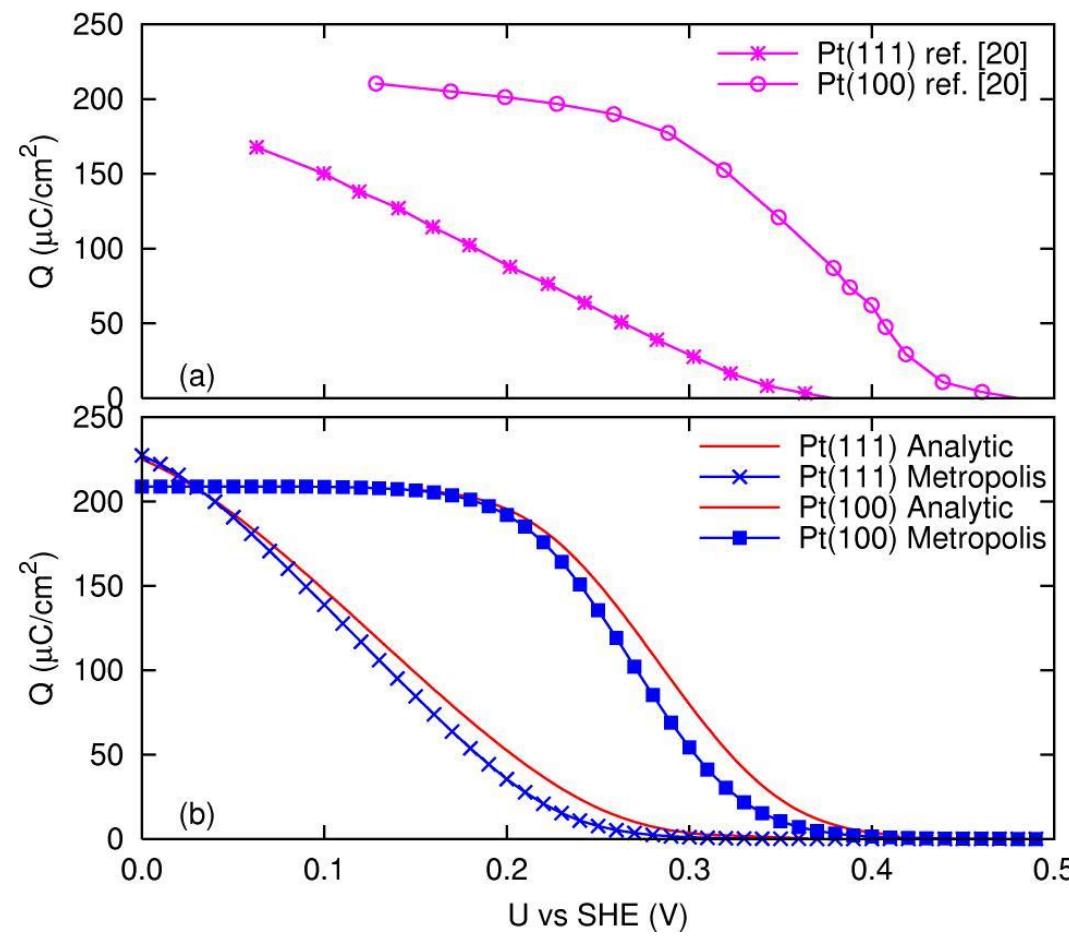
Rossmeisl, Nørskov, Taylor, Janik, Neurock. *J. Phys. Chem. B* **110**, (2006)



# Cyclic voltammetry

CV for Pt(111)



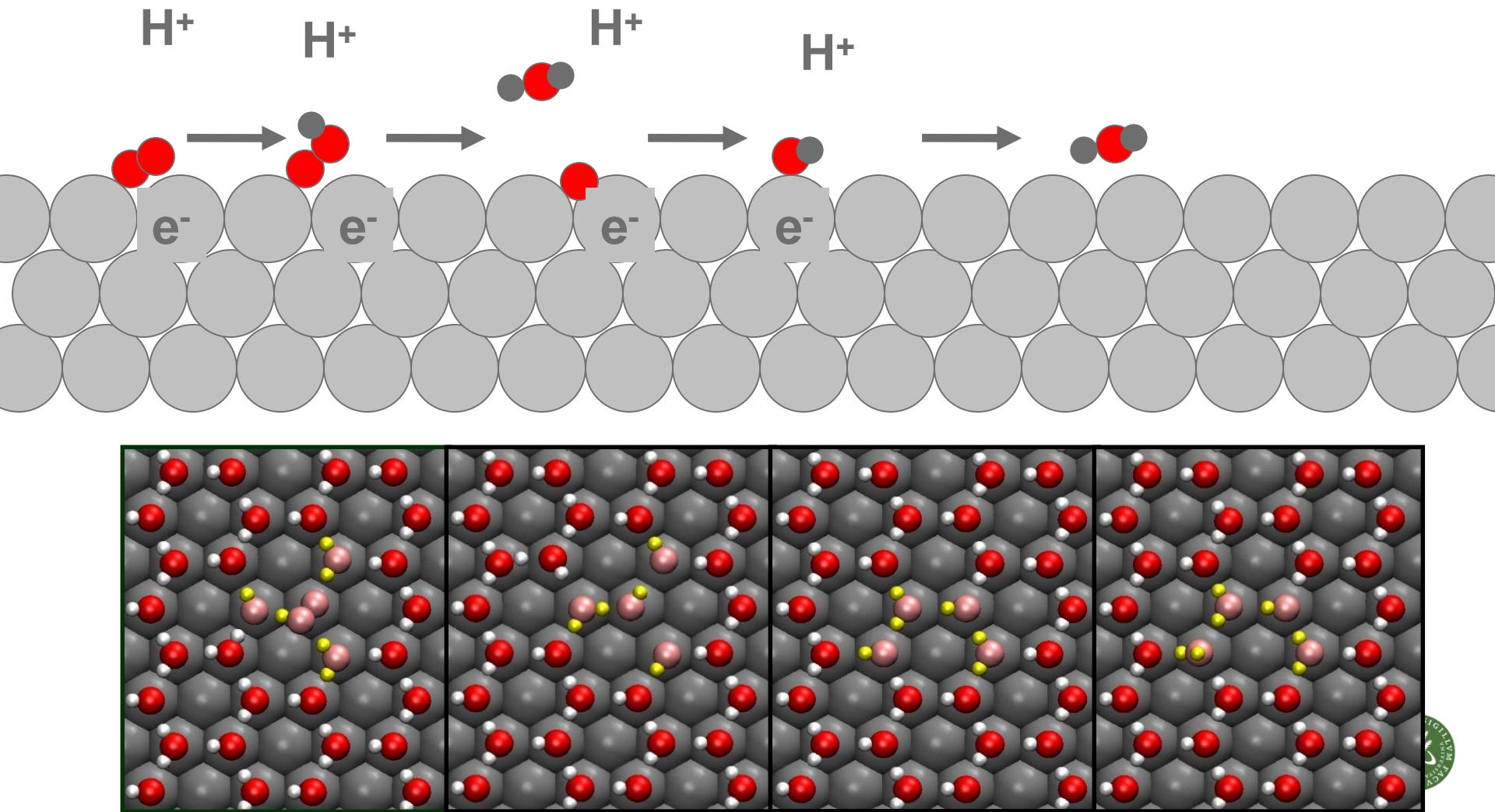


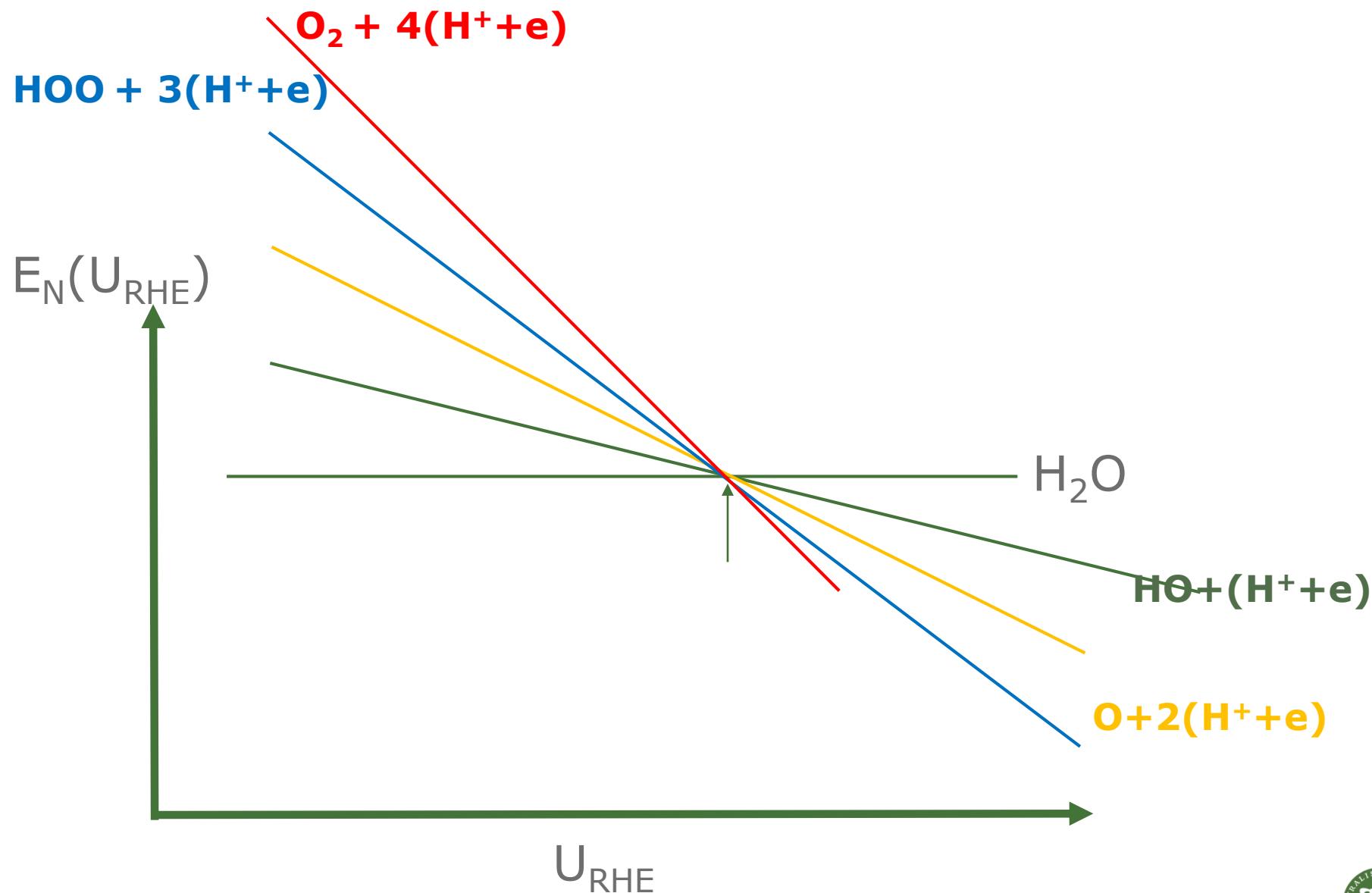
Markovic et al J. Phys. Chem. **101**, 5405 (1997)

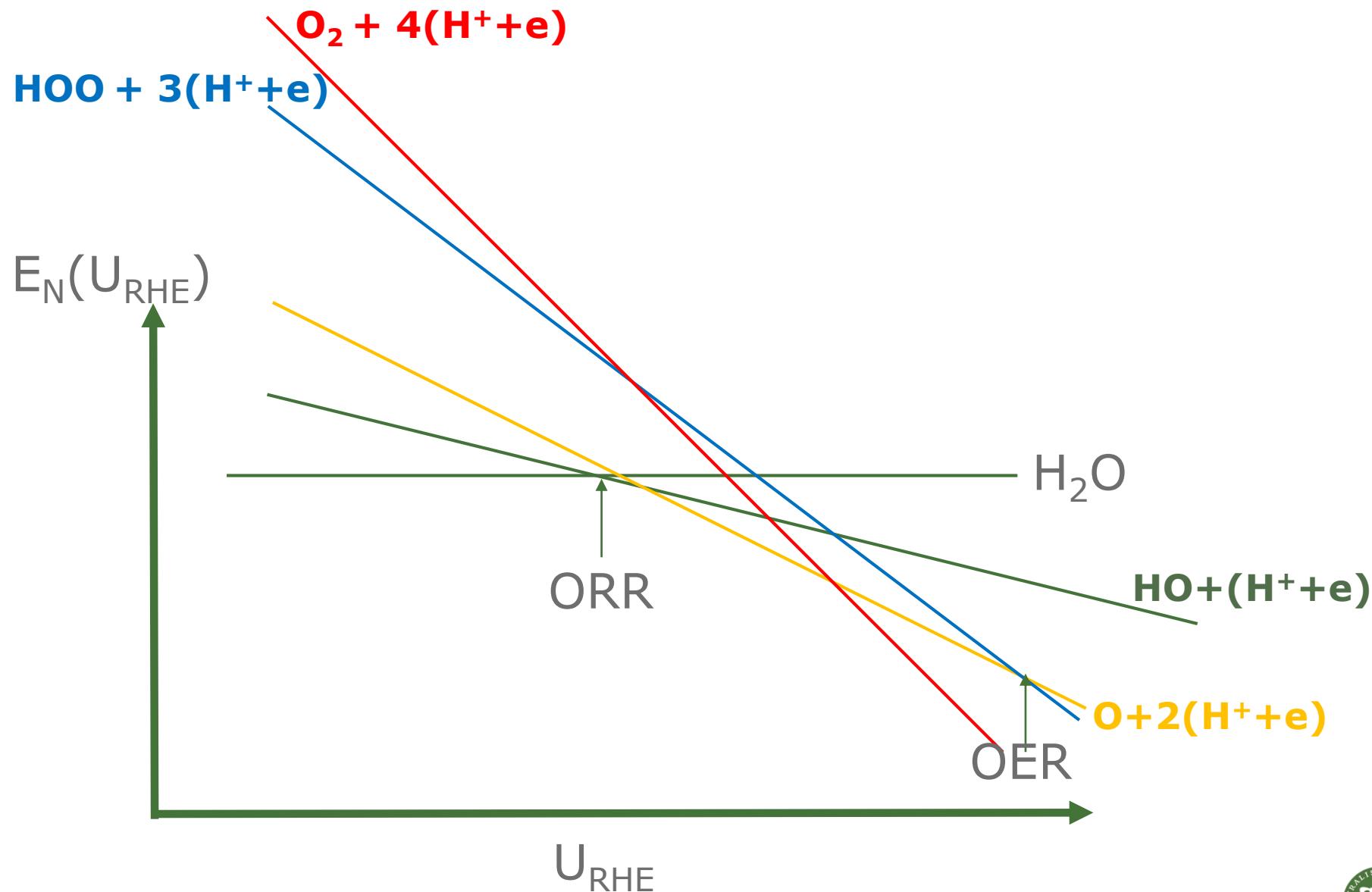
G.S. Karlberg, T. Jaramillo, E. Skulason, J. Rossmeisl, T. Bligaard, J.K. Nørskov. PRL, 99, (2007)



# ORR and OER intermediates



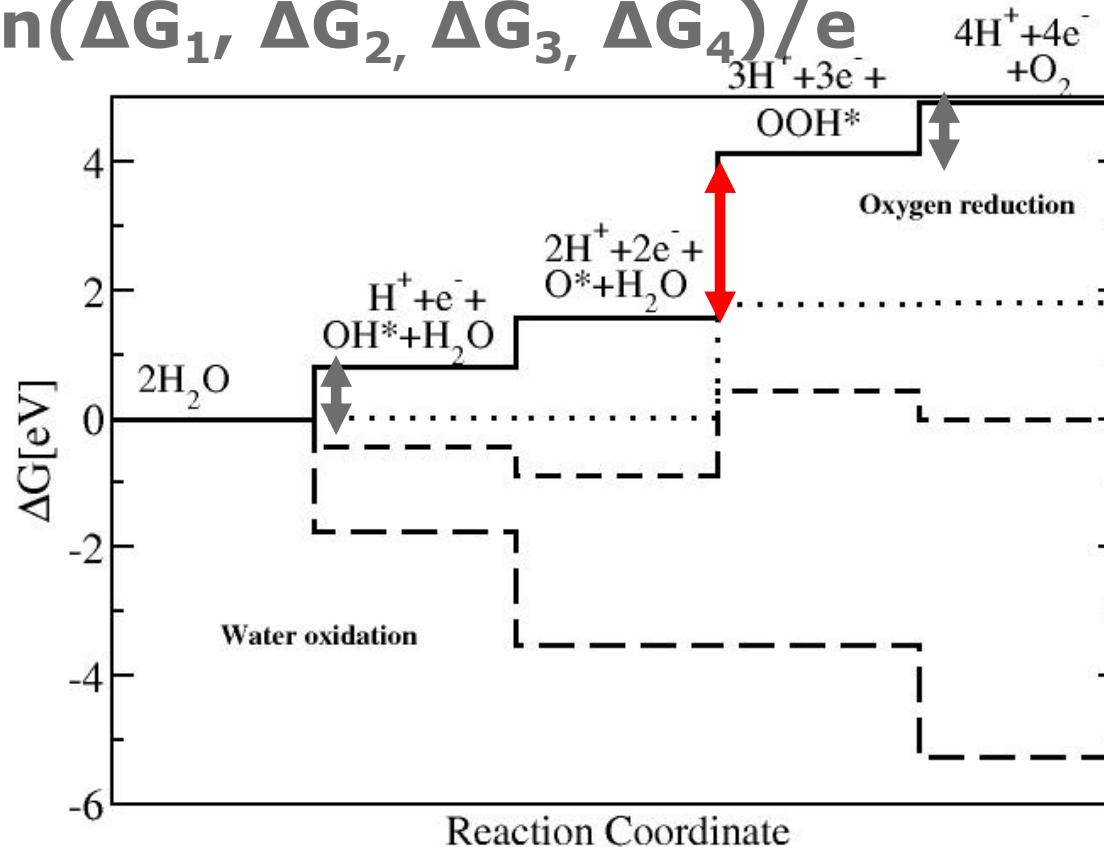




# $U_{\text{ORR}}$ and $U_{\text{OER}}$

$$U_{\text{OER}} = \max(\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4)/e$$

$$U_{\text{ORR}} = \min(\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4)/e$$



## OER and ORR double pyramid

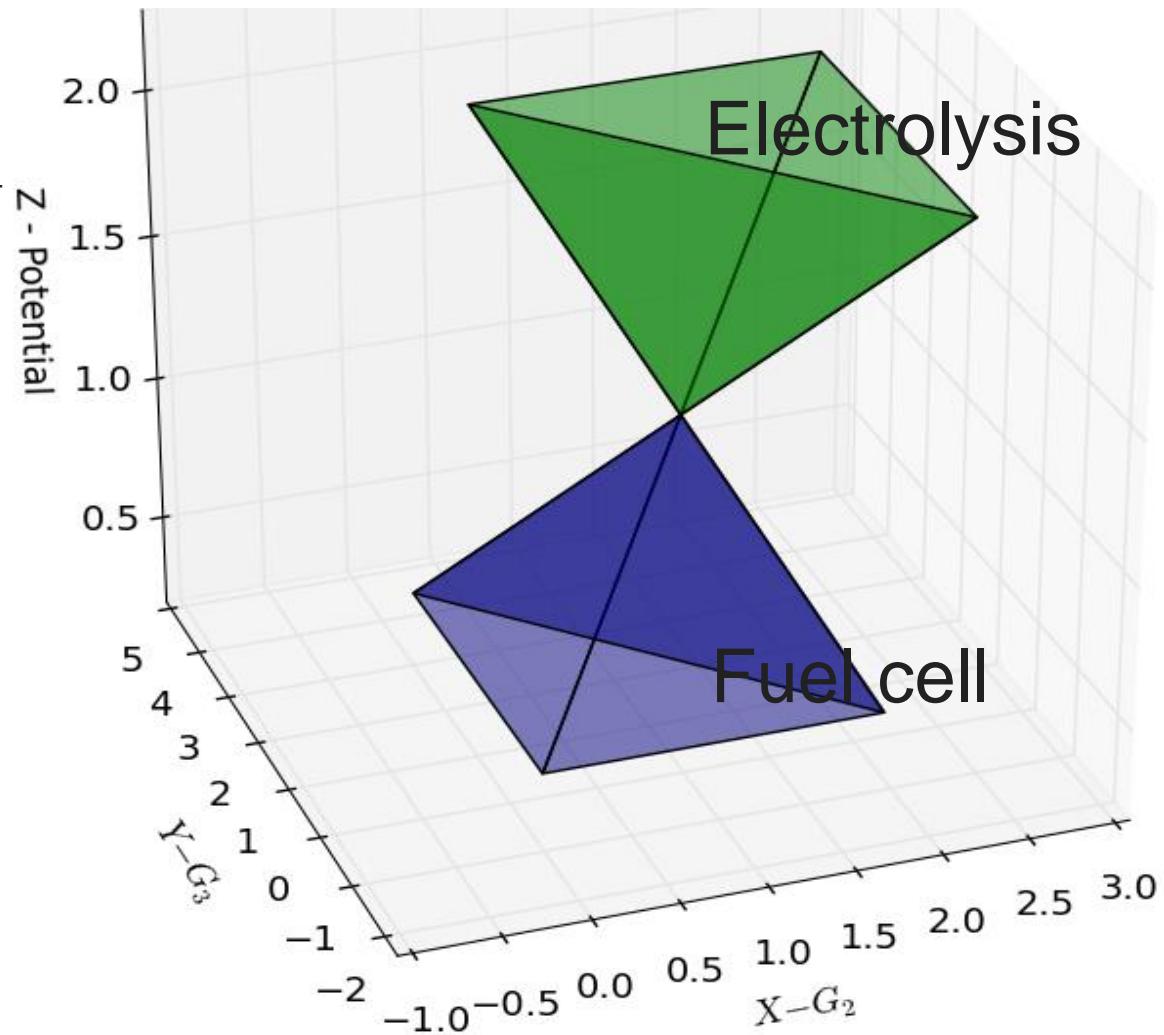
$$\Delta G_2 \sim \Delta G_1$$

$$4.92 \text{ eV} = \Delta G_1 + \Delta G_1 + \Delta G_3 + \Delta G_4$$

$$\Delta G_4 = 4.92 \text{ eV} - 2\Delta G_1 - \Delta G_3$$

$$U_{\text{ORR}}(\Delta G_1, \Delta G_3)$$

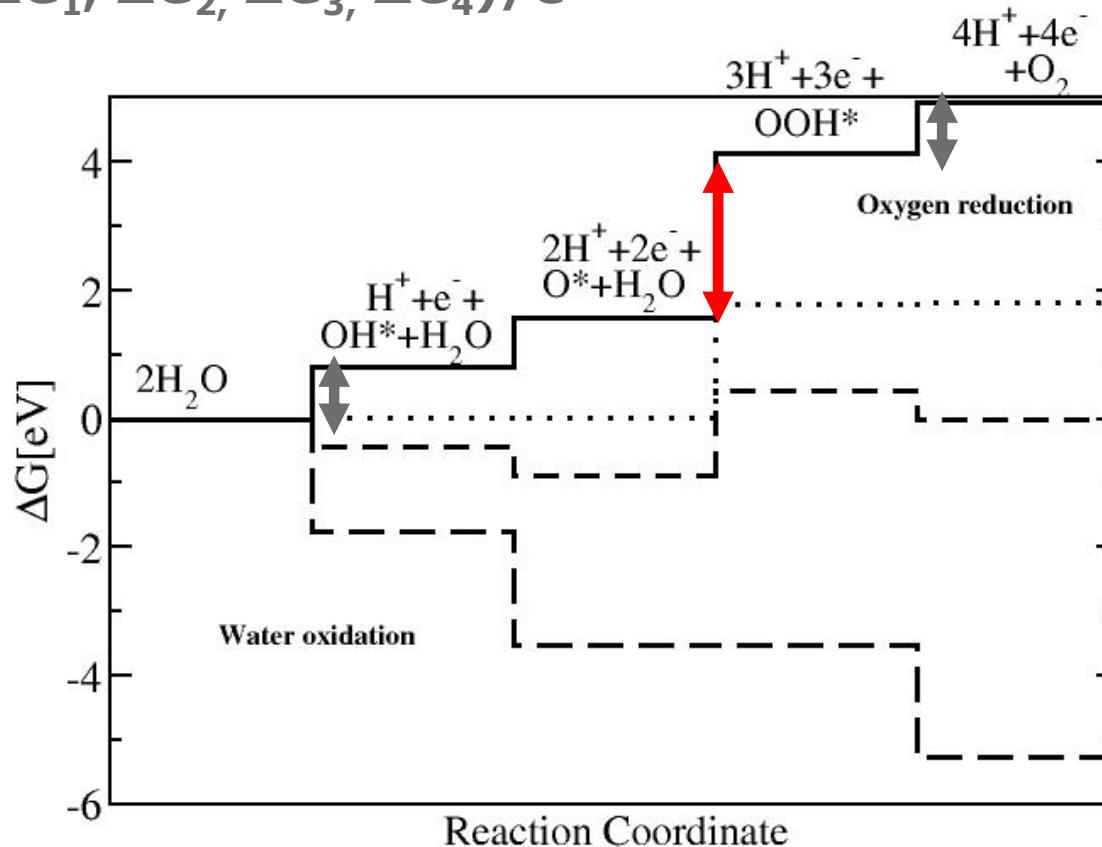
$$U_{\text{OER}}(\Delta G_1, \Delta G_3)$$



$U_{\text{ORR}}$  and  $U_{\text{OER}}$ 

$$U_{\text{OER}} = \max(\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4)/e$$

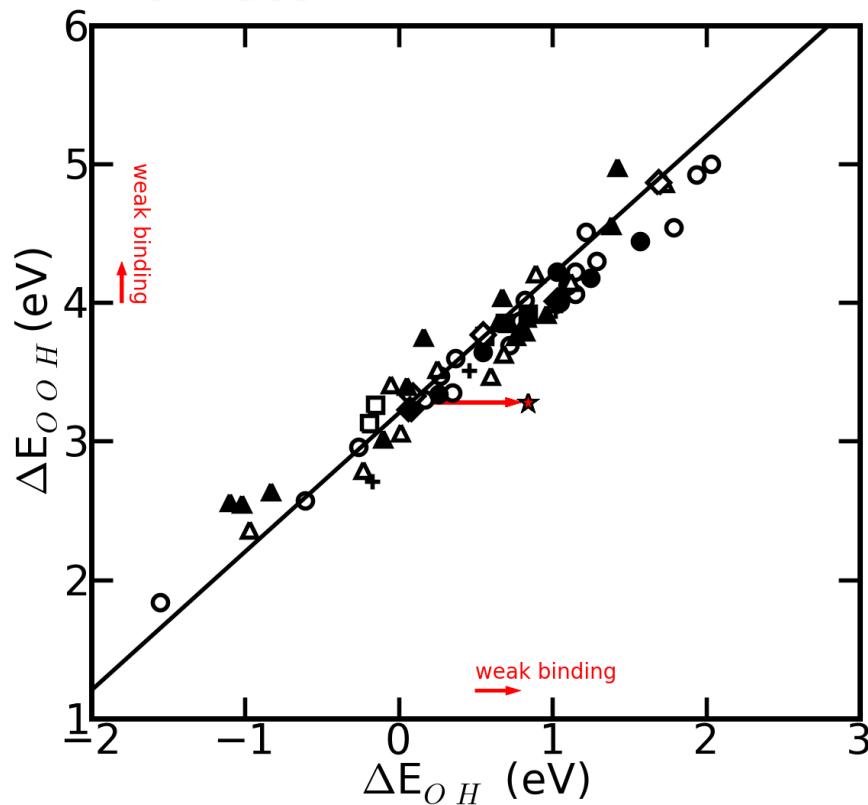
$$U_{\text{ORR}} = \min(\Delta G_1, \Delta G_2, \Delta G_3, \Delta G_4)/e$$



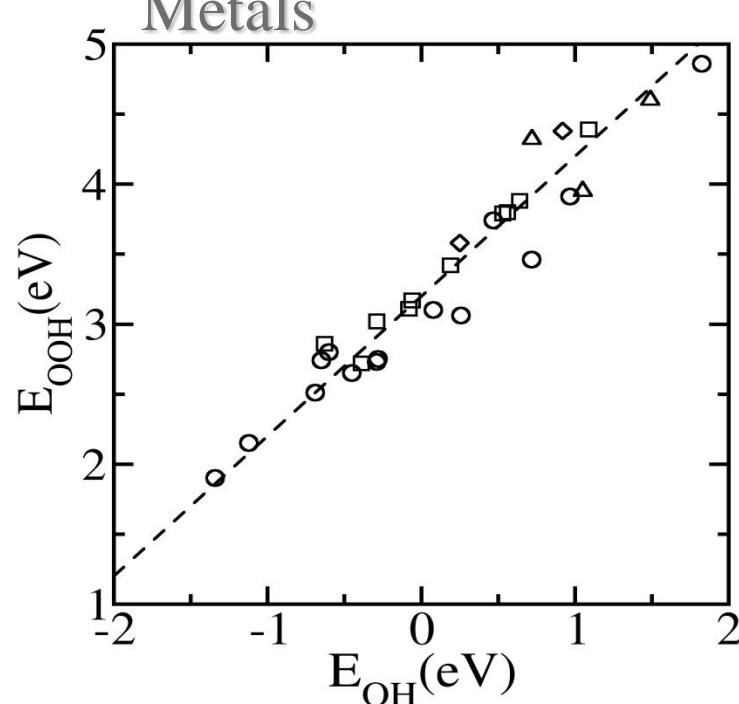
# Universal scaling

$$E_{OOH} = E_{OH} + 3.2 \pm 0.2 \text{ eV}$$

Oxides



Metals



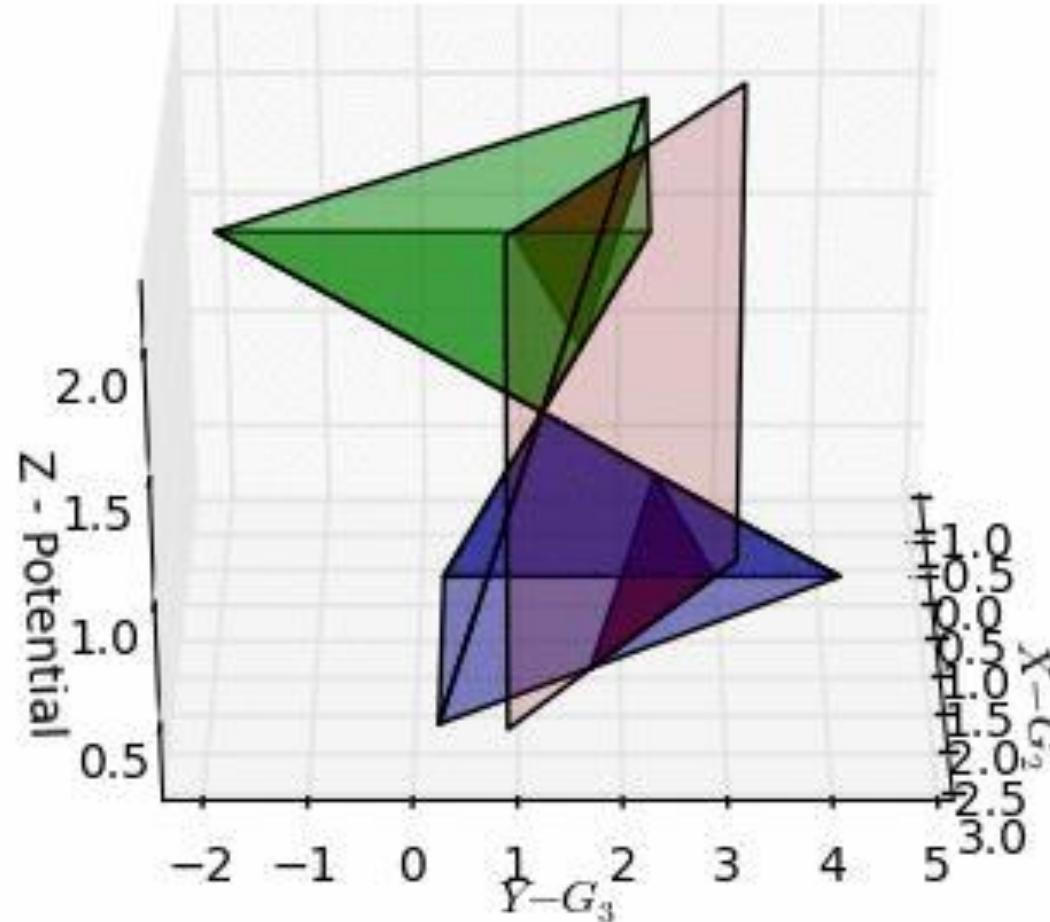
M. Koper, Journal of Electroanalytical Chemistry 2011

Man, Su, Calle-Vallejo, Hansen, Martinez, Inoglu, Kitchin, Nørskov, Rossmeisl ChemCatChem 2011





$$\text{Scaling: } \Delta G_1 + 3.2\text{eV} = 2\Delta G_2 + \Delta G_3$$
$$\Leftrightarrow \Delta G_3 = 3.2\text{eV} - \Delta G_1$$

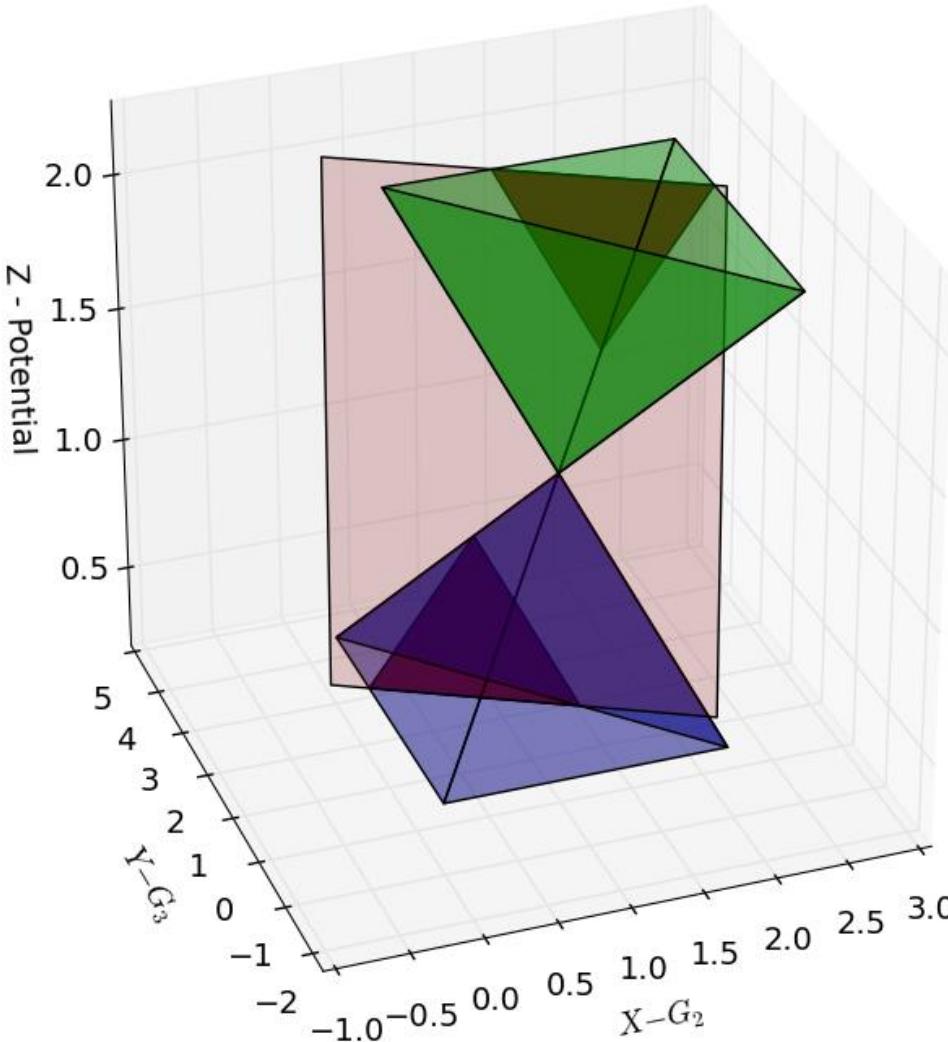


OER

ORR



# Scaling → Volcanos



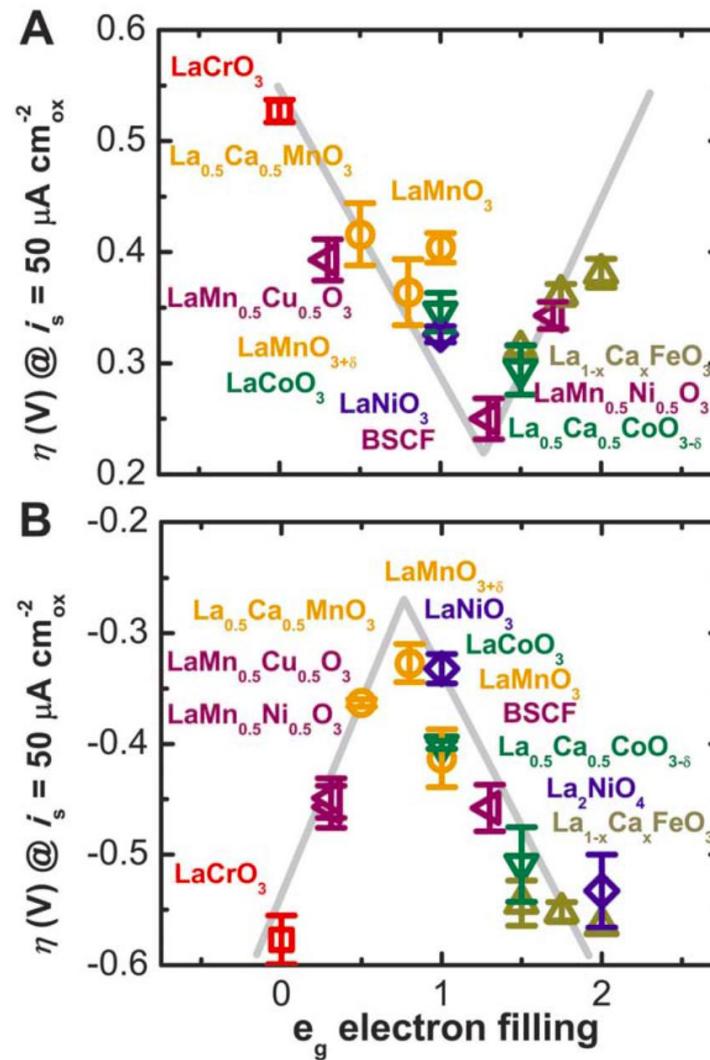
OER

ORR



# Double Volcano

Suntivich, May, Gasteiger, Goodenough, Shao-Horn *Science* **334**, 1383 (2011)

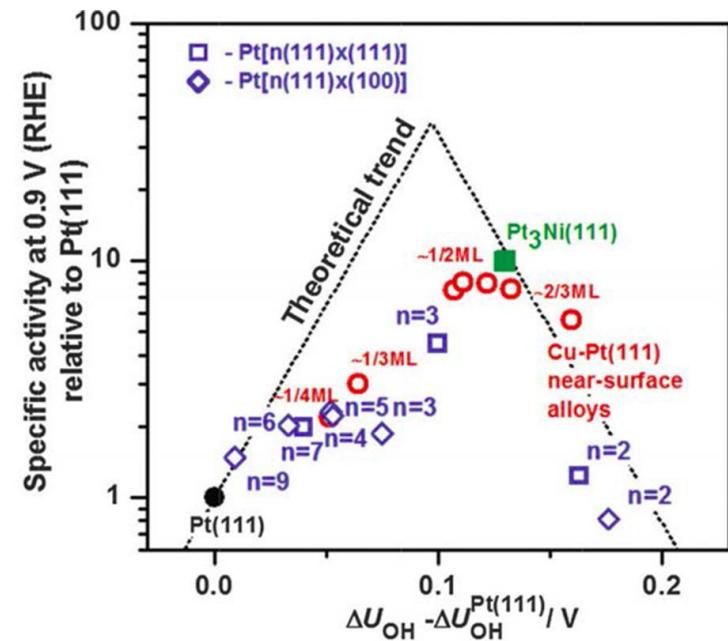
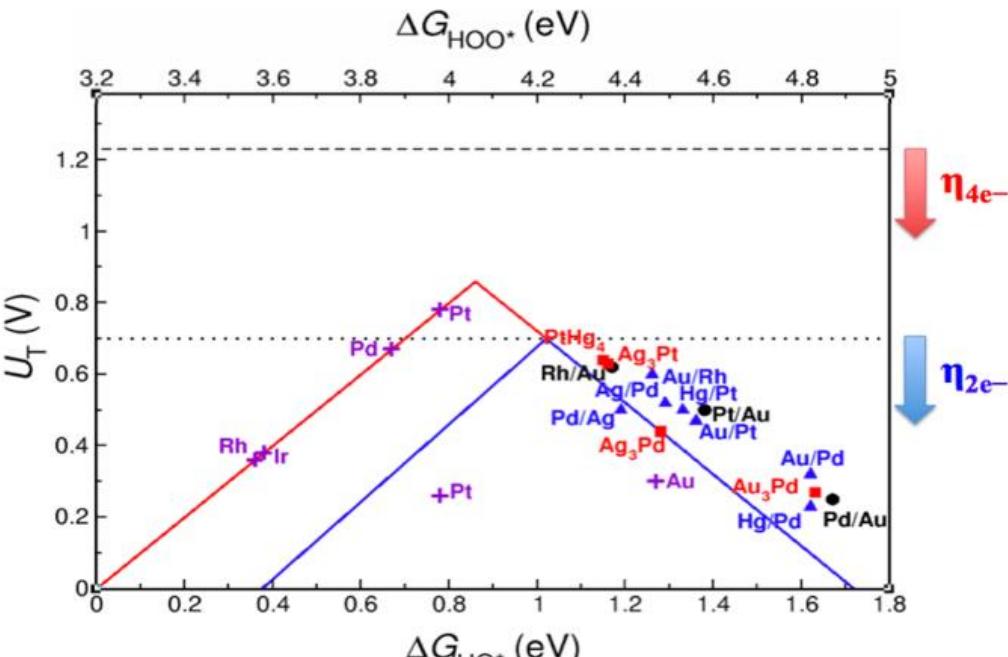


OER

ORR



# The role of the surface



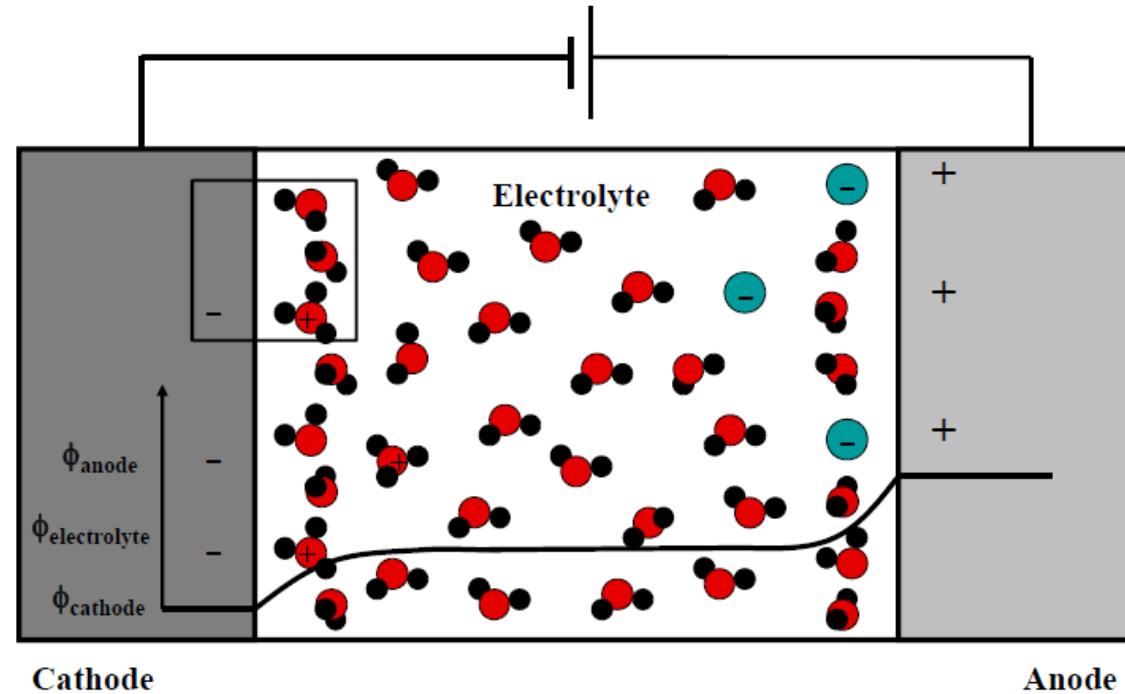
What is the role of the electrolyte?



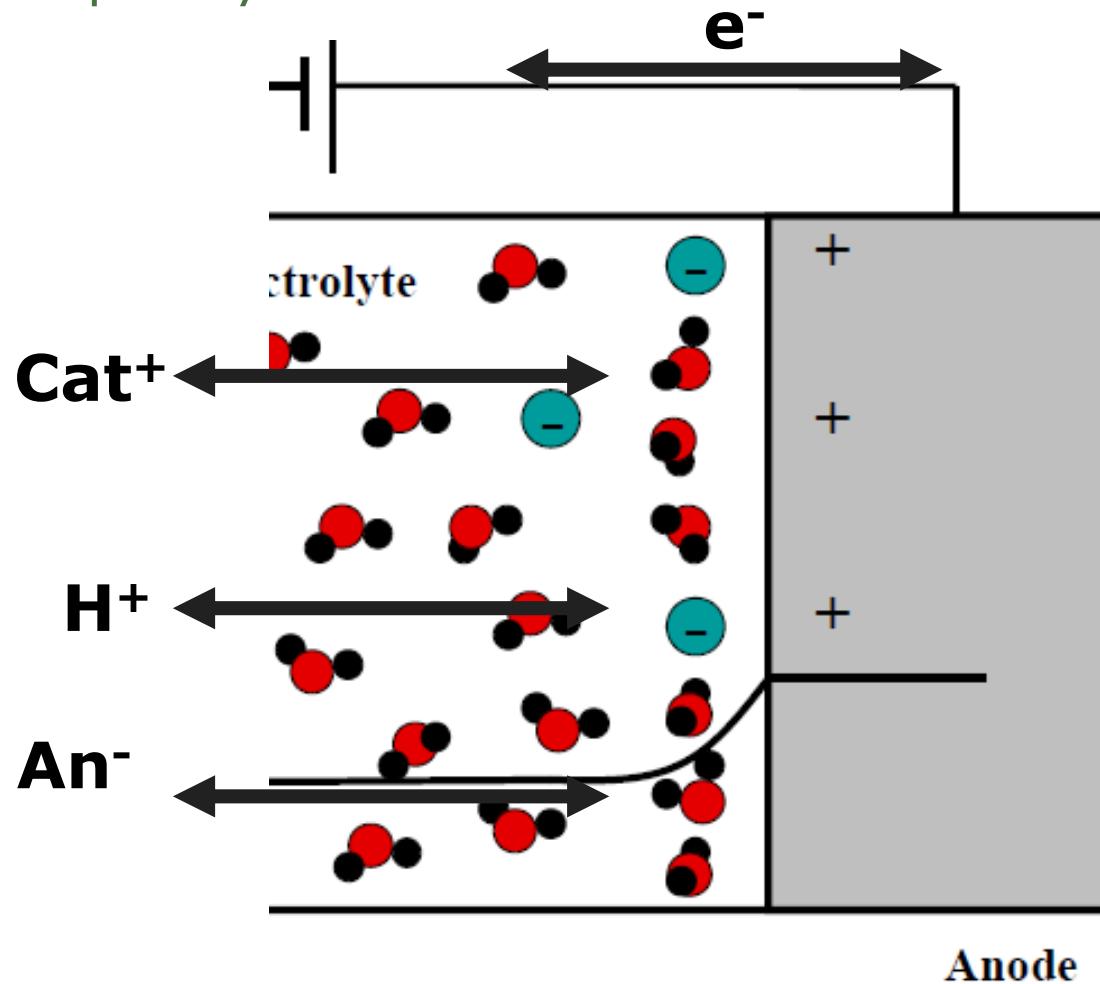
# Towards Electrochemical interfaces

PARENTAL  
ADVISORY  
EXPLICIT CONTENT

# Open system

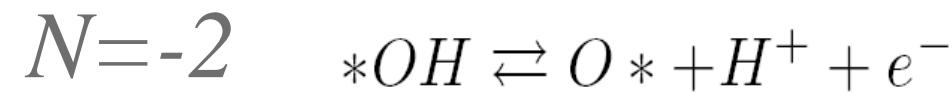
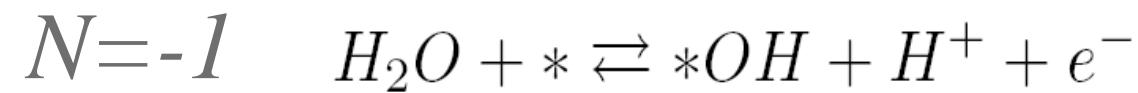
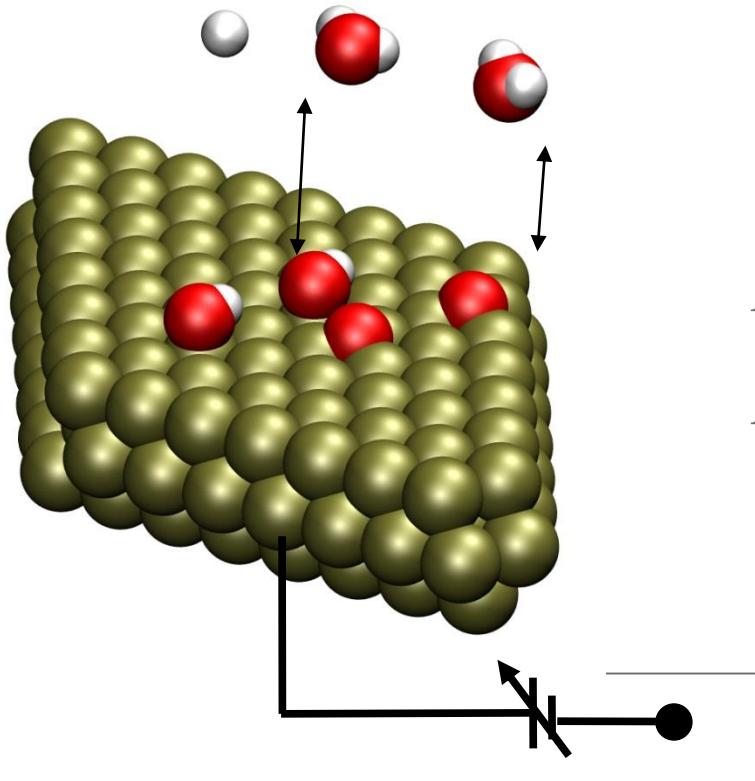


## Open system



# Evaluate energy of the surface as function of the potential

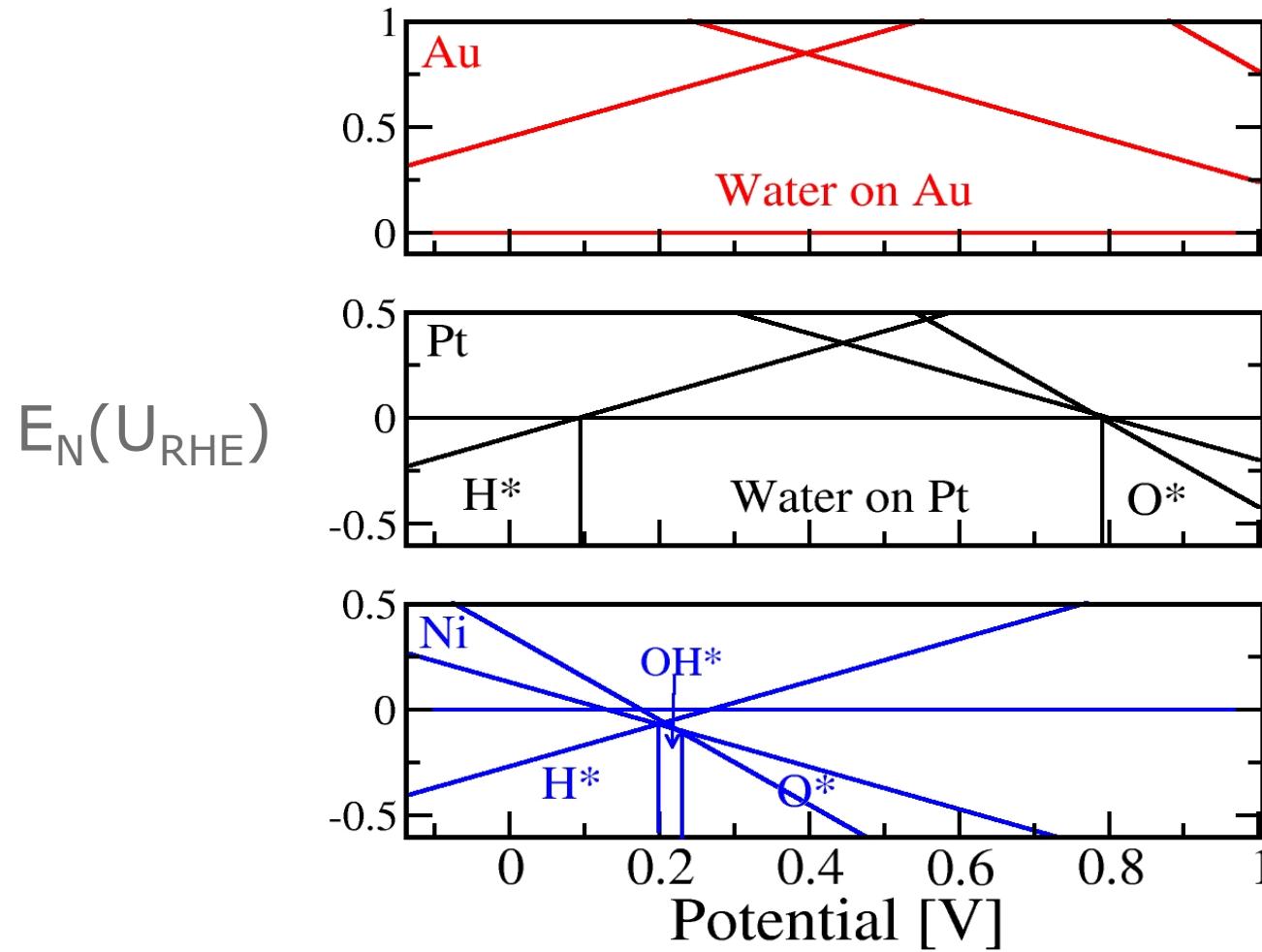
$$E_N(U_{\text{RHE}}) = E(N) - E(0) - \frac{1}{2}NG(H_2) - \frac{1}{2}NeU_{\text{RHE}}$$



U vs. RHE



# Phase-diagrams



Rossmeisl, Nørskov, Taylor, Janik, Neurock. *J. Phys. Chem. B* **110**, (2006)



## What have we done

$$U = E(N) - E(0) - \frac{1}{2}N G_{H_2}$$

In an open system with constant  $\mu$ ,  $\text{Min}(U(N))$

$$d(U) = \mu dN$$

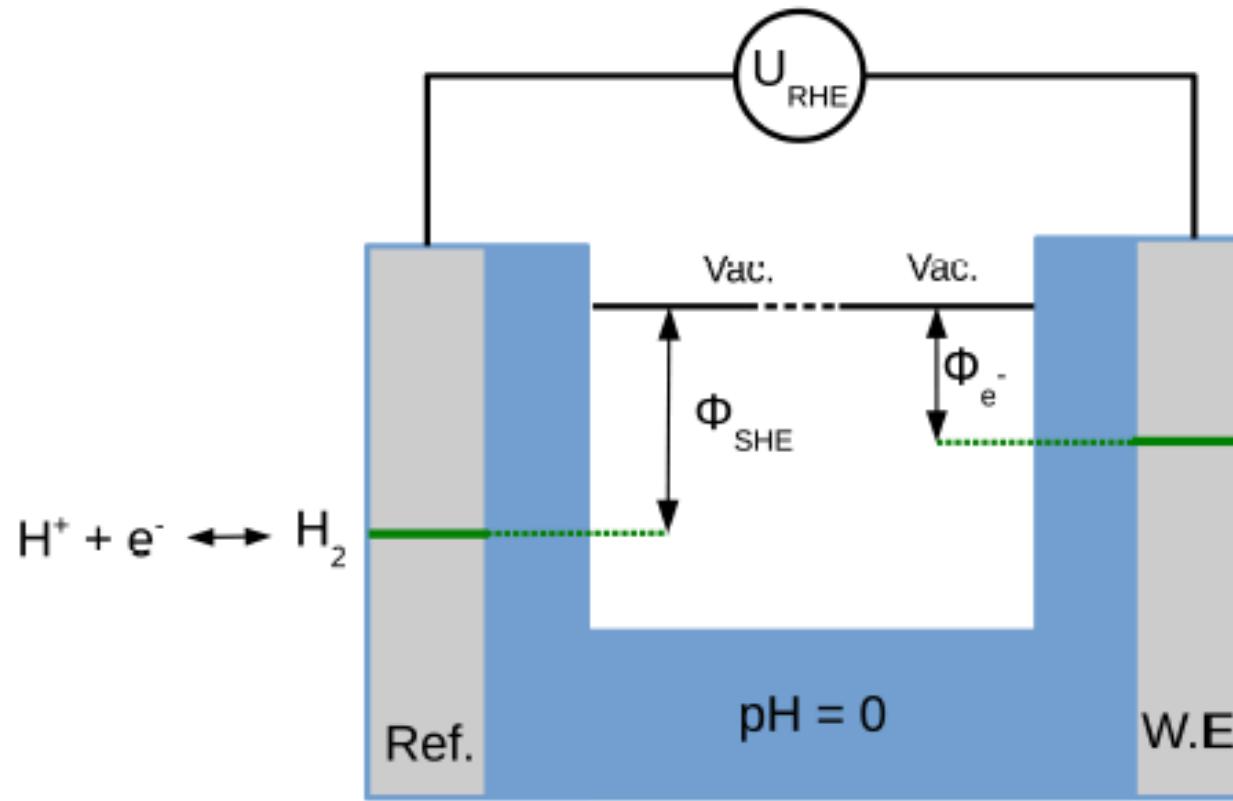
In a closed system with constant  $N$ ,  $\gamma = U - \mu N$ ,  $\text{Min}(\gamma(\mu))$

$$d(U - \mu N) = -N d\mu$$

$$E_N(U_{RHE}) = E(N) - E(0) - \frac{1}{2}N G(H_2) - \frac{1}{2}N e U_{RHE}$$



# Generalized Computational electrode Workfunction is linked to the potential



Martin Hangaard Hansen, Chengjun Jin, Kristian S. Thygesen, Jan Rossmeisl, JPC 2016

# What can we do with pH?

$$\mu = \phi_{\text{electrons}} + \phi_{\text{protons}}$$

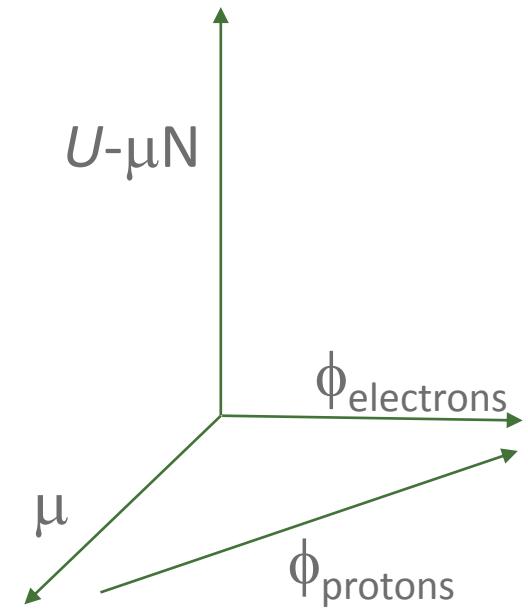
$$\text{pH} \sim \phi_{\text{protons}}$$

$$d(U) = \mu dN = \phi_{\text{electrons}} dN + \phi_{\text{protons}} dN$$

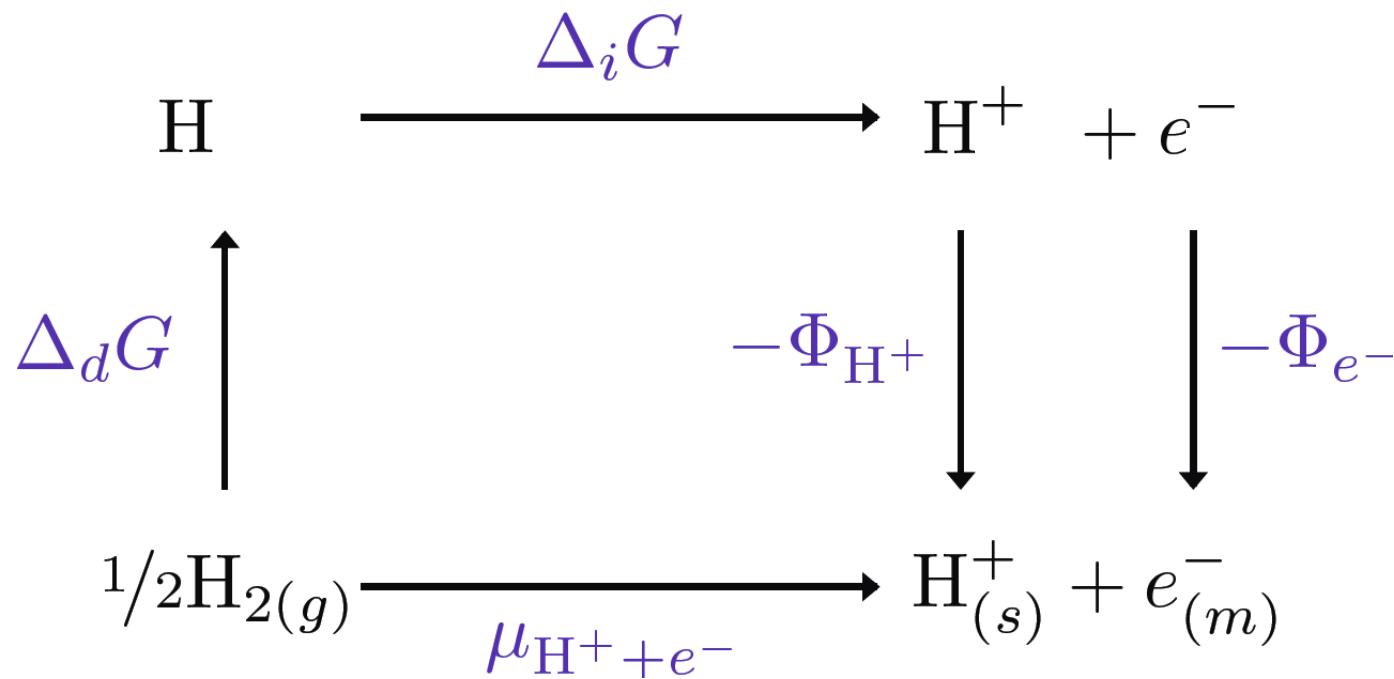
$$d(\gamma) = d(U - \mu N) = -Nd\mu = -Nd\phi_{\text{electrons}} - Nd\phi_{\text{protons}}$$

$$\text{Min}(\gamma(\mu, \phi_{\text{electrons}}))$$

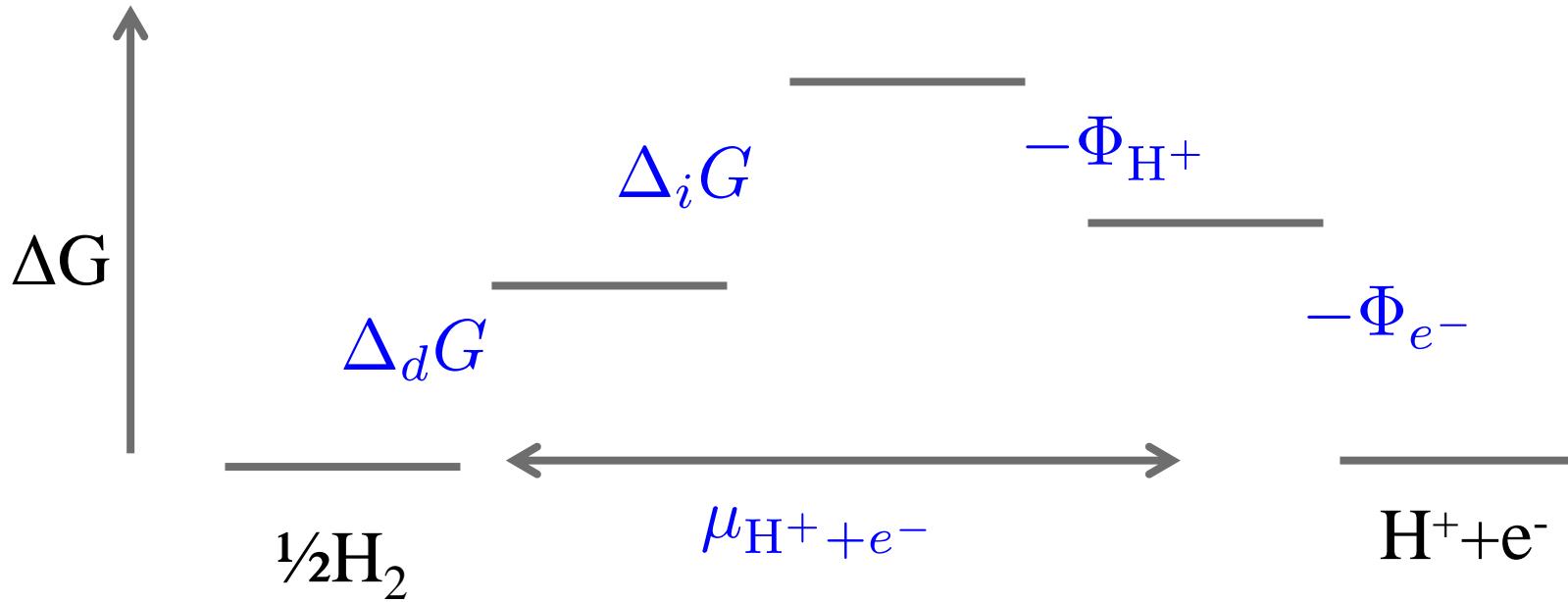
Rossmoel, Bagger, Arnarson in preparation



# Born-Haber-cycle



## Born-Haber



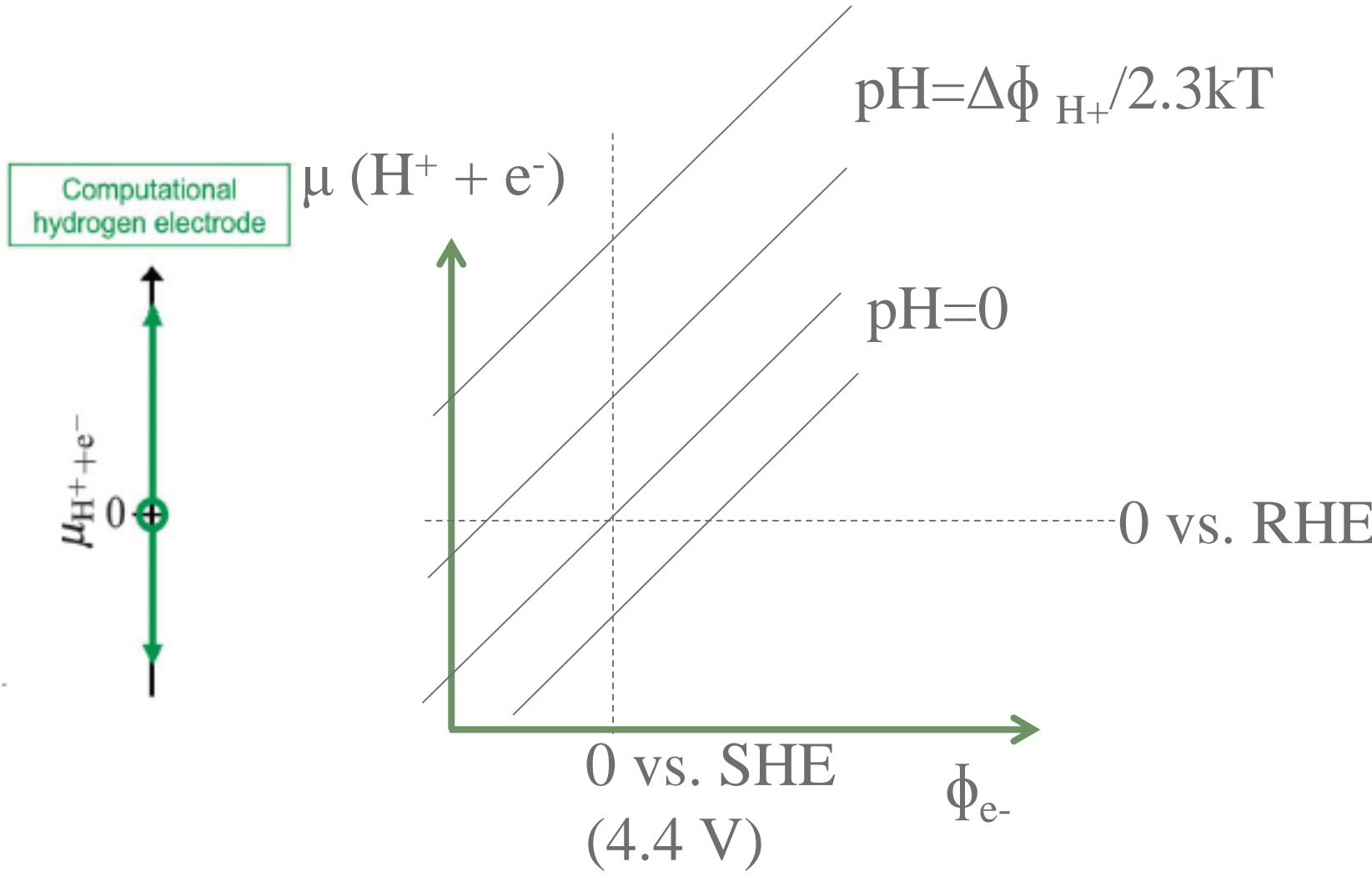
From experiments  $\Phi_{\text{e}^-} \sim 4.4 \text{ eV}$  at pH=0

$$\Delta\Phi_{\text{H}^+} = kT \ln [a_{\text{H}^+}] = 0.059 \text{ eV/pH}$$

Knowing  $\mu_{\text{H}^+ + \text{e}^-}$  and  $\Phi_{\text{e}^-}$  means that pH is known as well



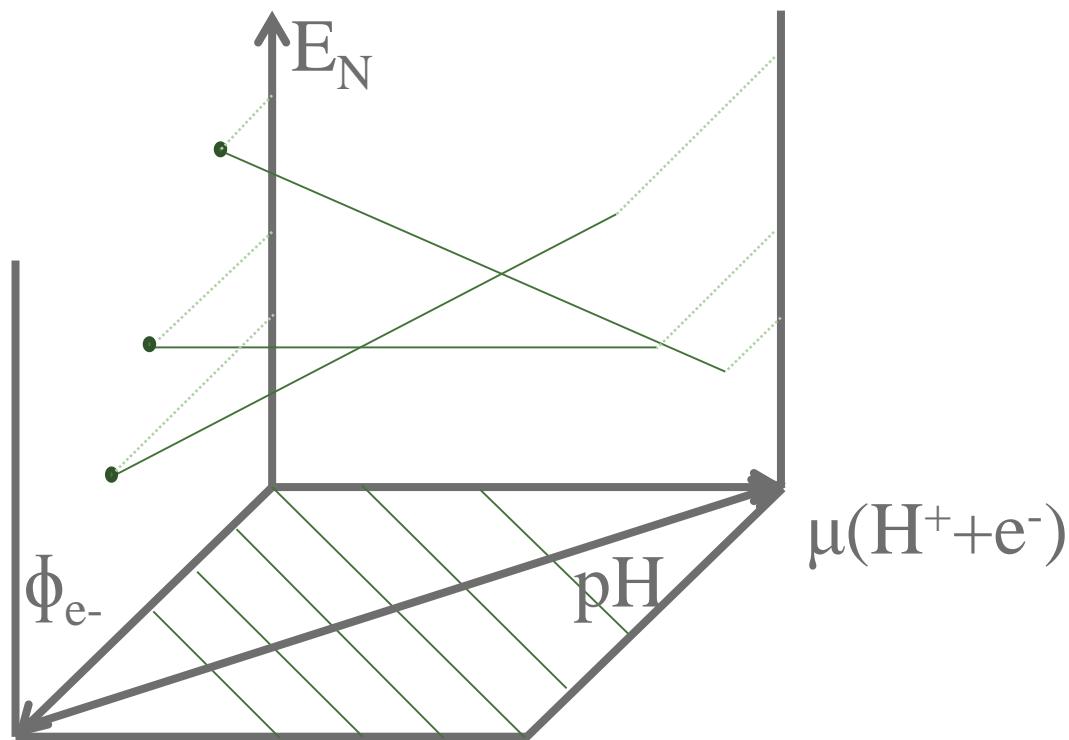
# pH and potential



# The energy of the interface

$$E_N(U_{RHE}) = E(N) - E(0) - \frac{1}{2}NG(H_2) - \frac{1}{2}NeU_{RHE}$$

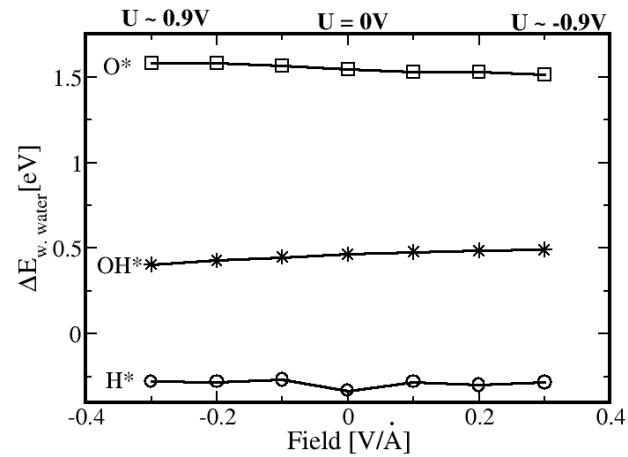
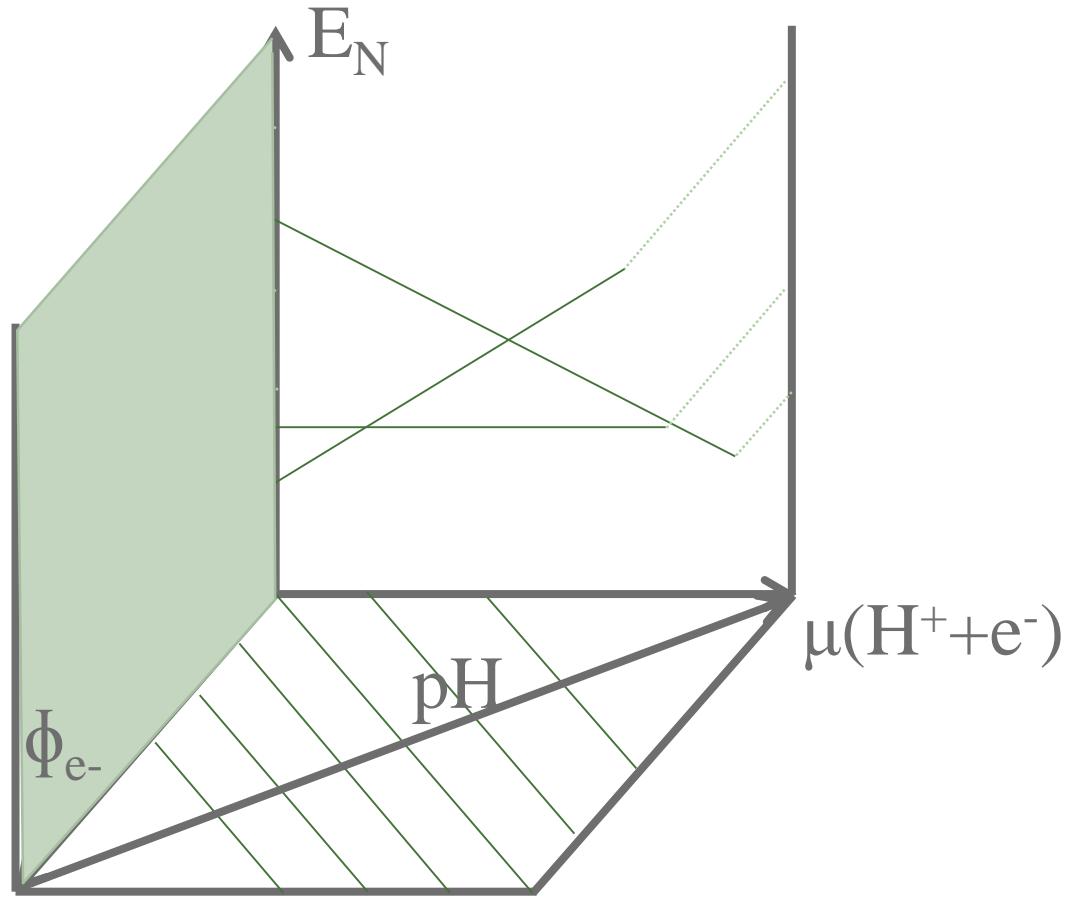
$$E_N(\phi_{e^-}, U_{RHE}) = E(N, \phi_{e^-}) - E(0) - \frac{1}{2}NG(H_2) - \frac{1}{2}NeU_{RHE}$$



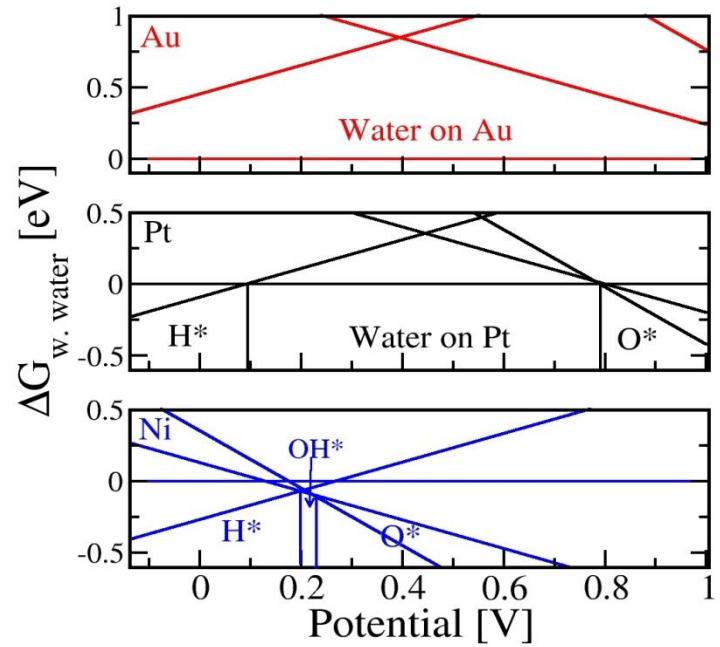
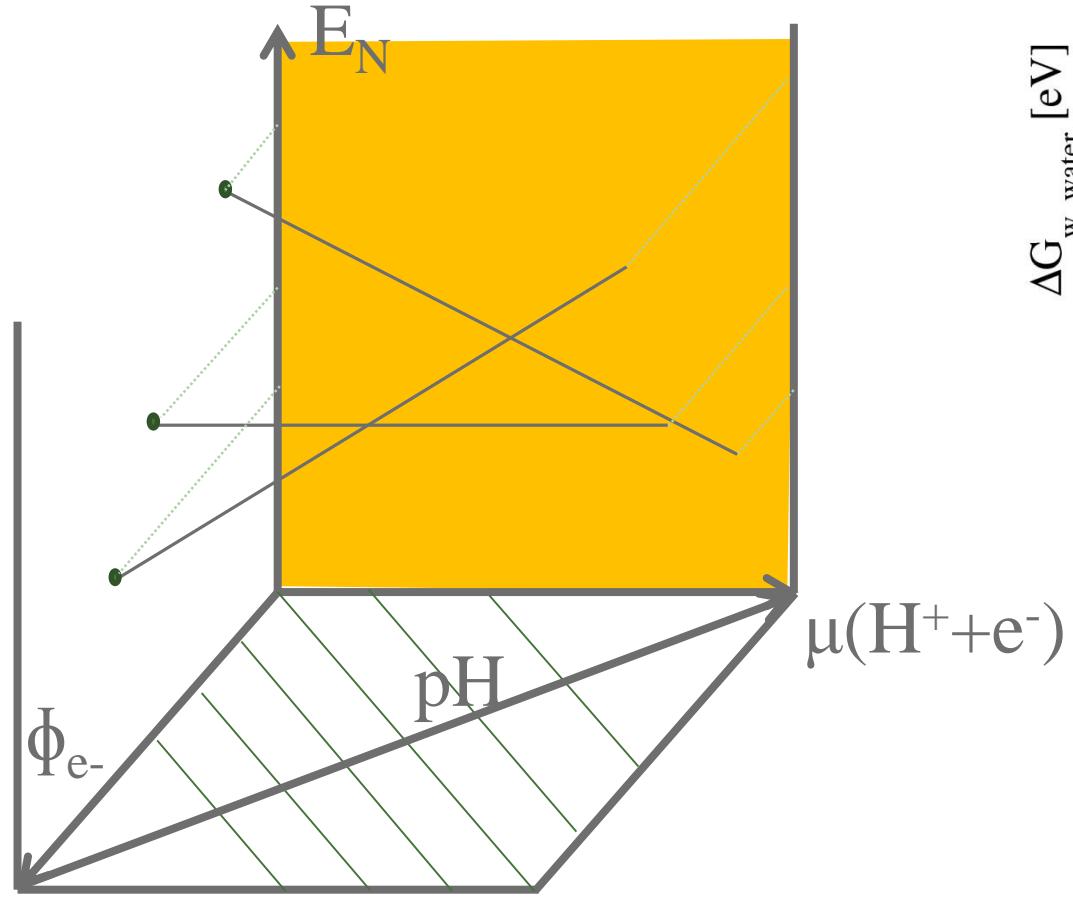
Rossmeisl, Chan, Ahmed, Tripkovic, Bjorketun, PCCP 2013



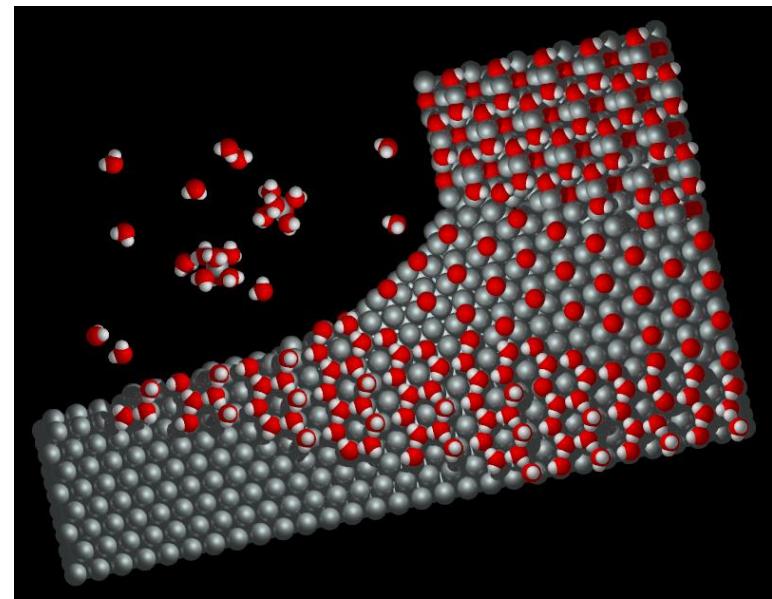
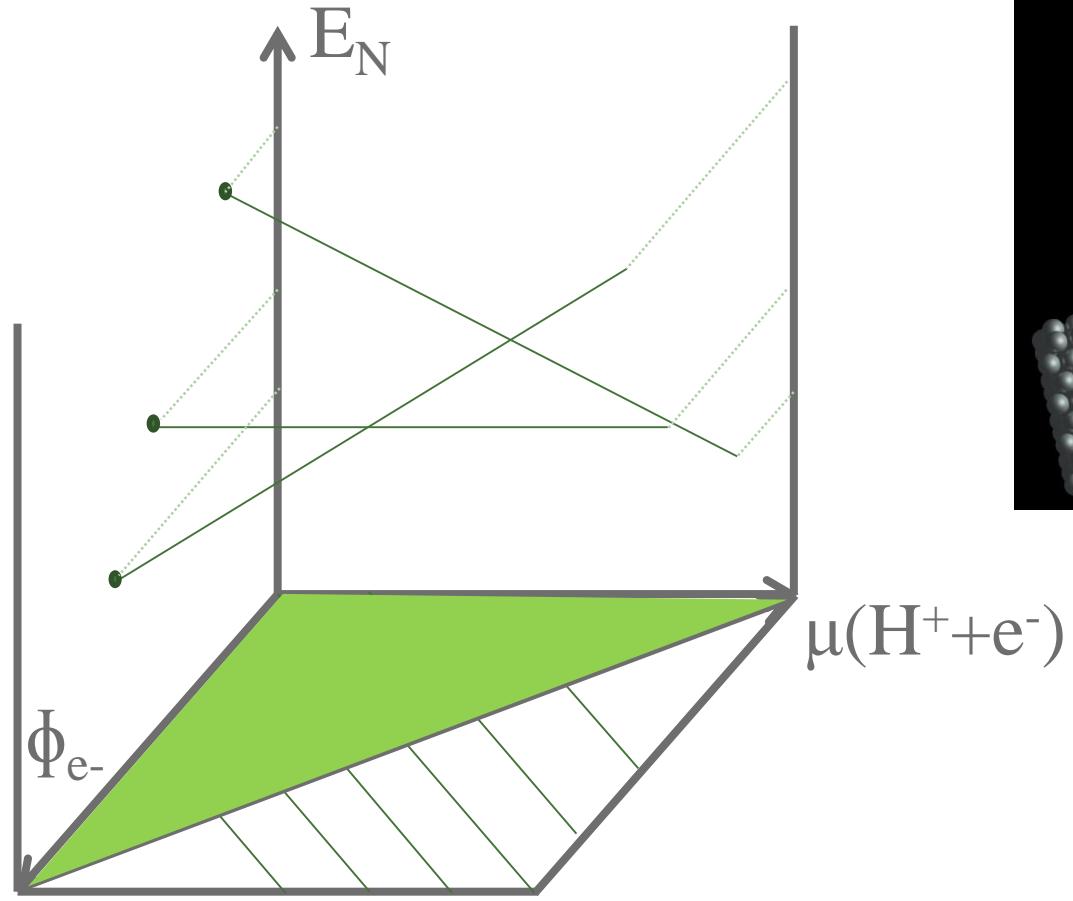
# Projections



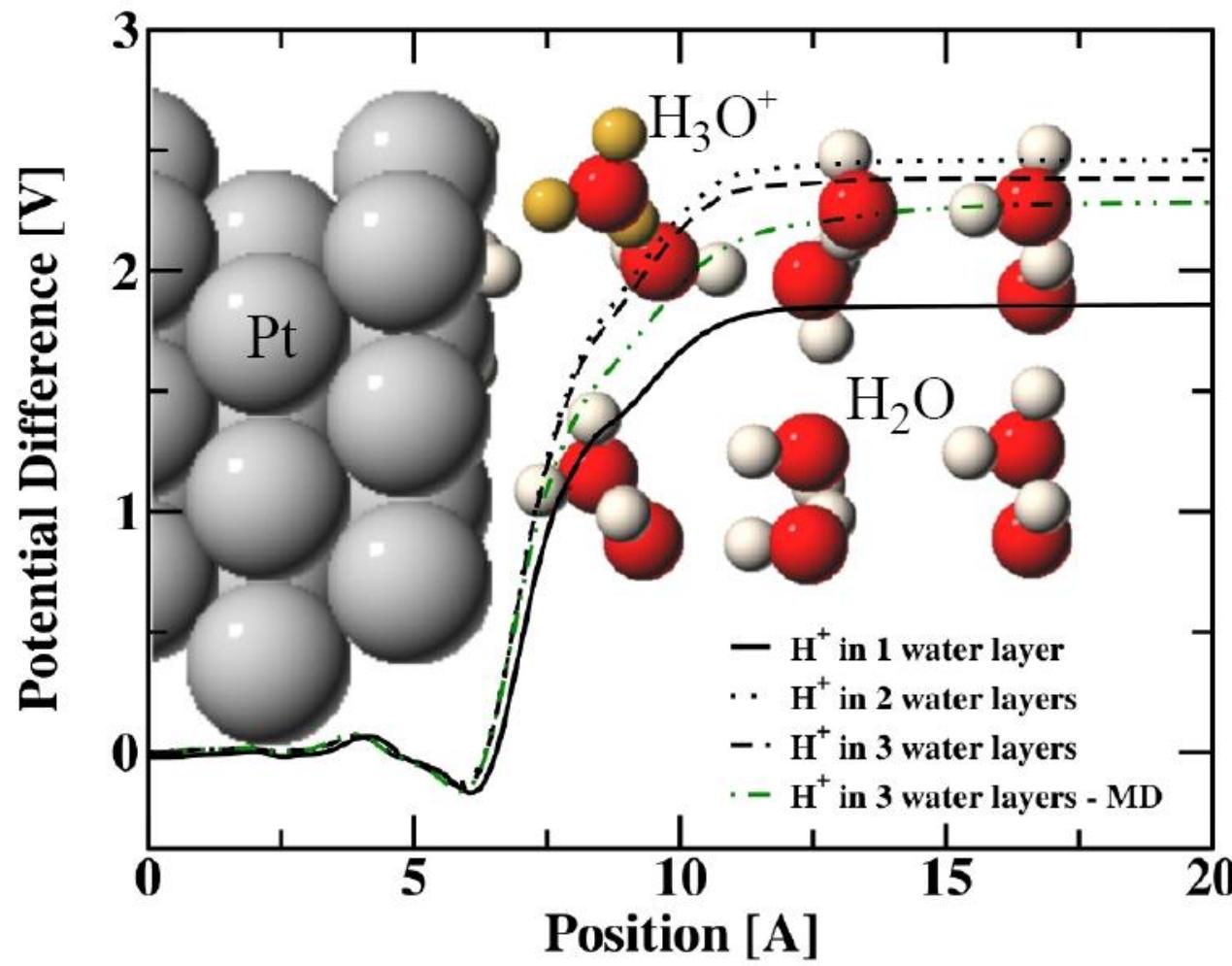
# Projections



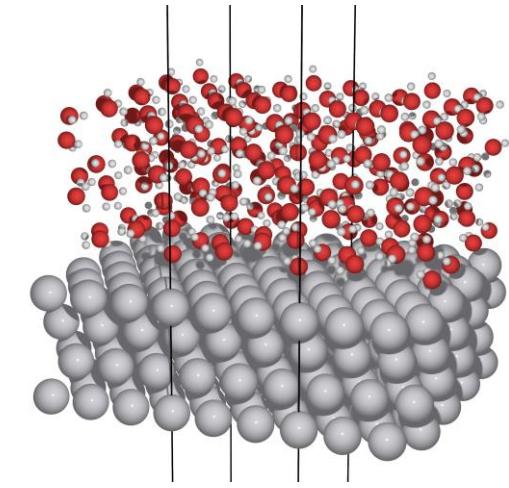
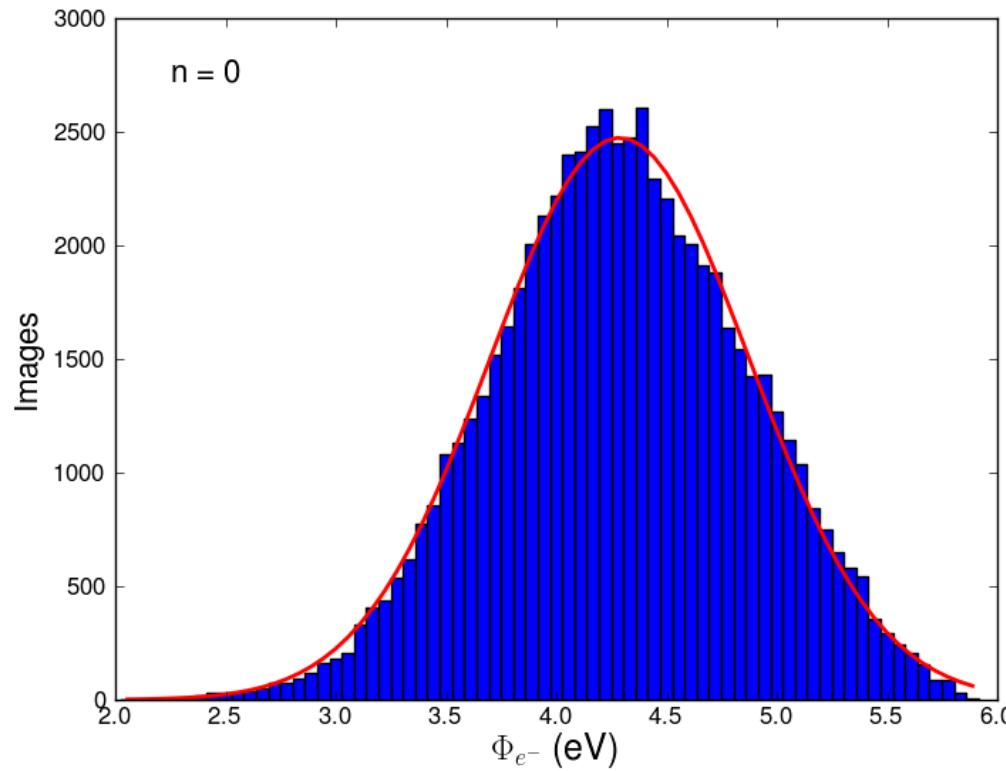
# Projections



## Adding hydrogen to the electrolyte $E_N$

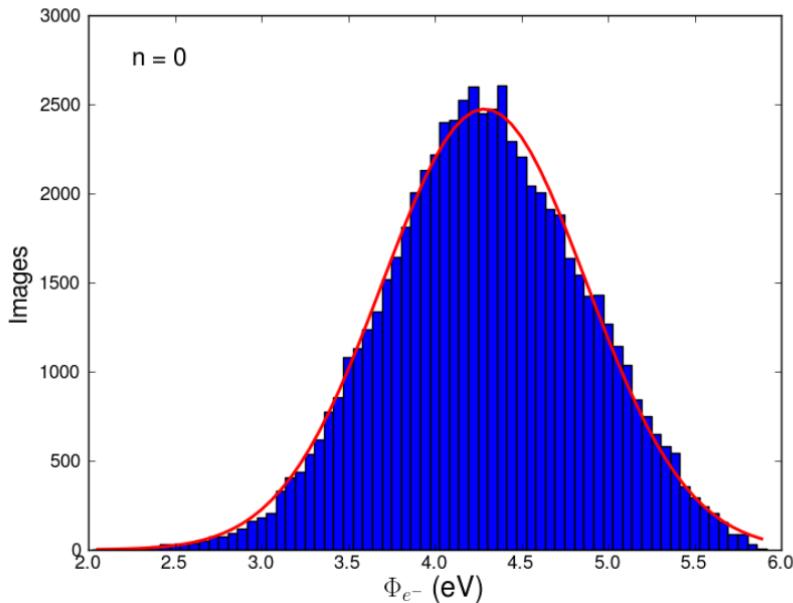


# Work function as order parameter Normal distribution $E_N(\phi_{e^-})$

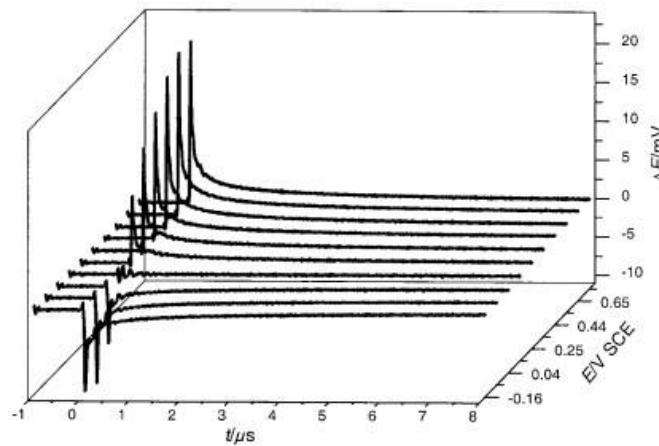


Hansen, Nilsson, Rossmeisl, PCCP, 2017

# Potential of maximum entropy



$$\left( \frac{\partial U}{\partial T} \right)_T = - \left( \frac{\partial \Delta S}{\partial q^M} \right)_q$$

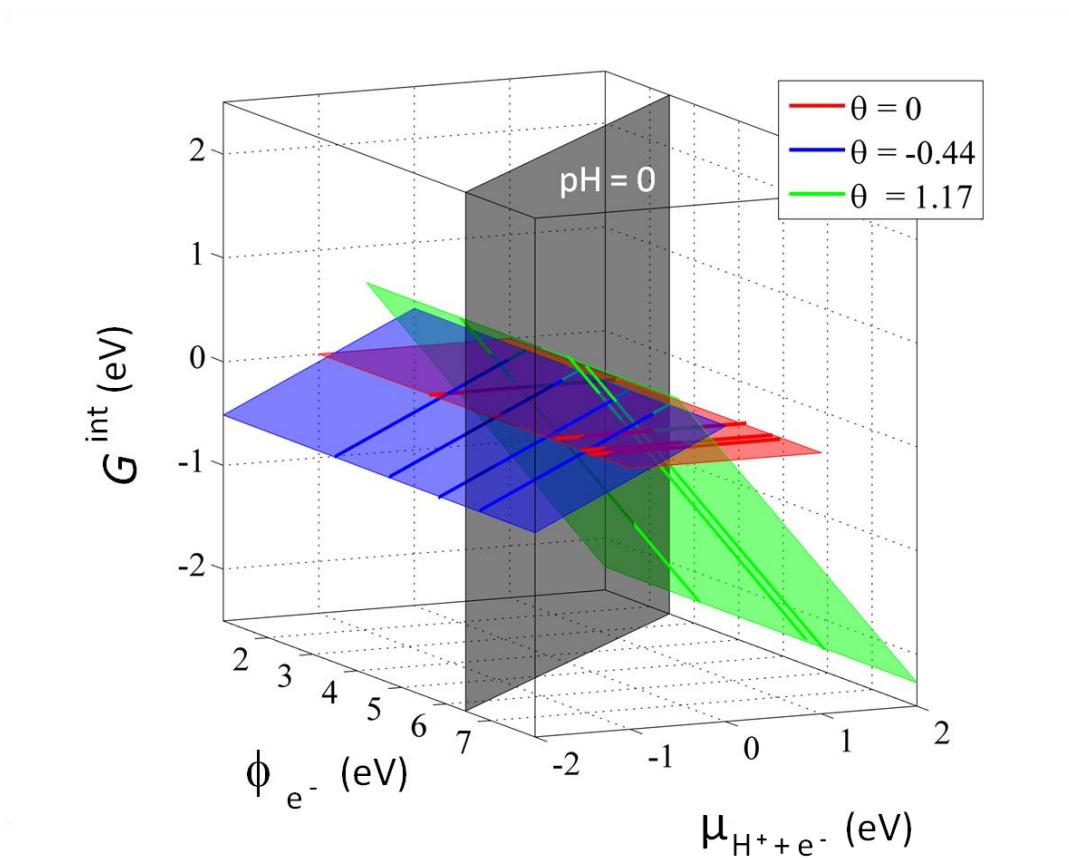


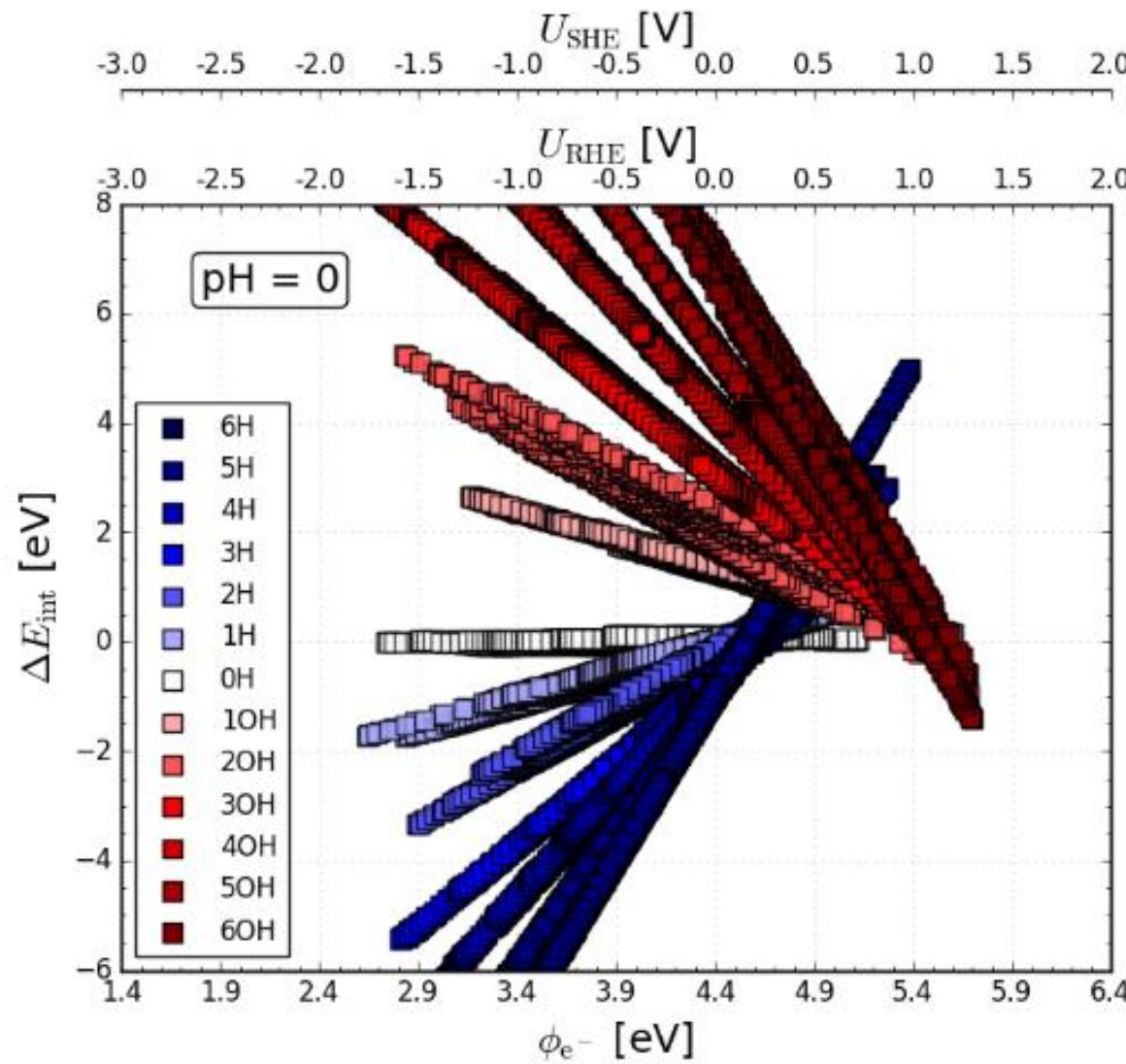
Clement, V.; Coles, B. A.; Compton, R. G. *Laser-Induced Potential Transients on a Au(111) Single-Crystal Electrode. Determination of the Potential of Maximum Entropy of Double-Layer Formation*. J. Phys. Chem. B 2002, 106, 5258–5265

Sted og dato

Dias 42



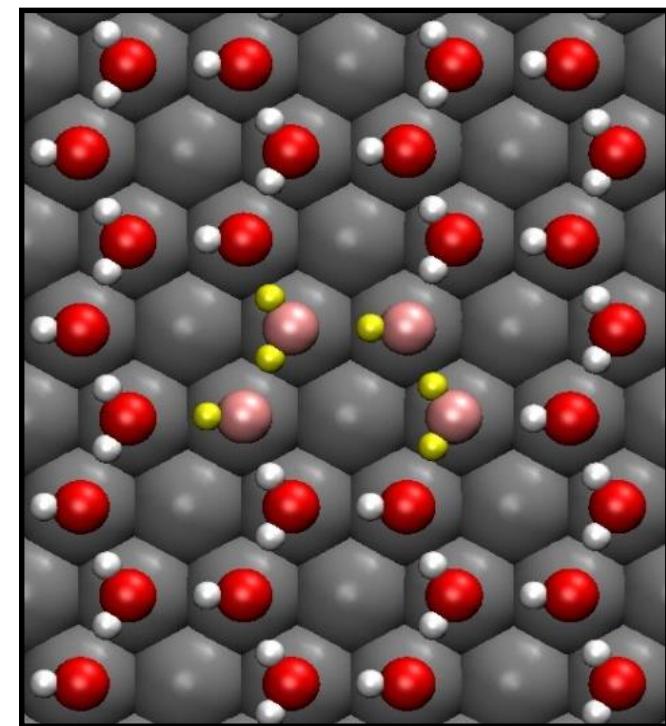
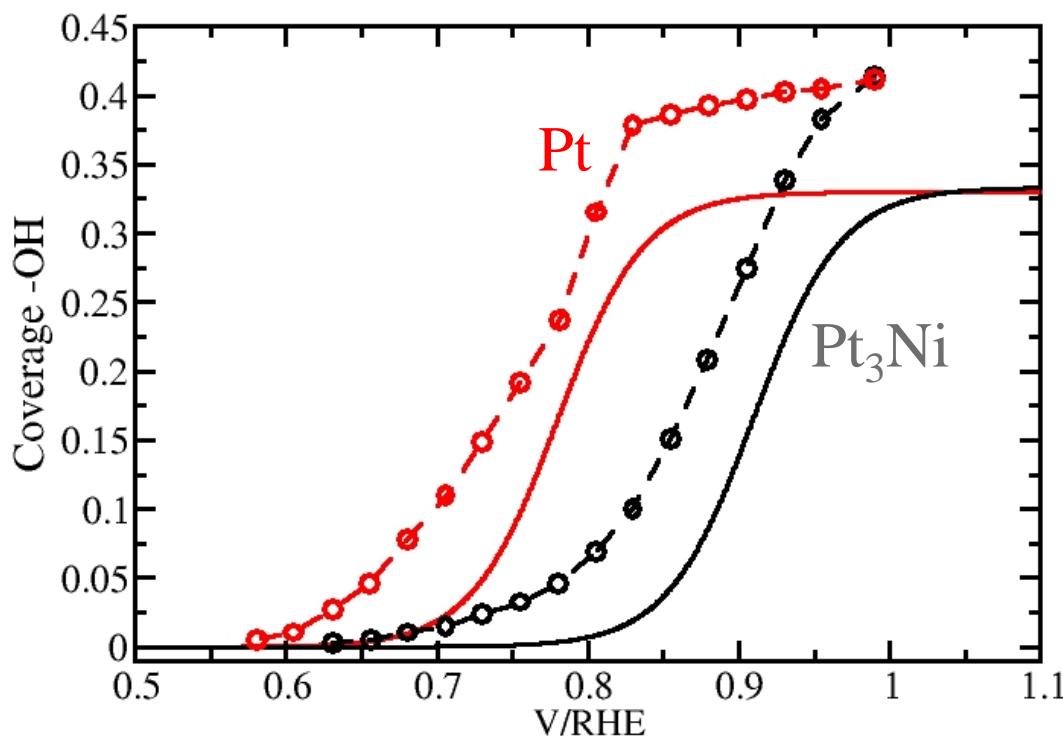


$\gamma_N(\mu, \phi_e)$ 

OH-coverage  
 $\text{H}_2\text{O} \leftrightarrow \text{OH}^* + \text{H}^+ + \text{e}^-$

Langmuir isotherm

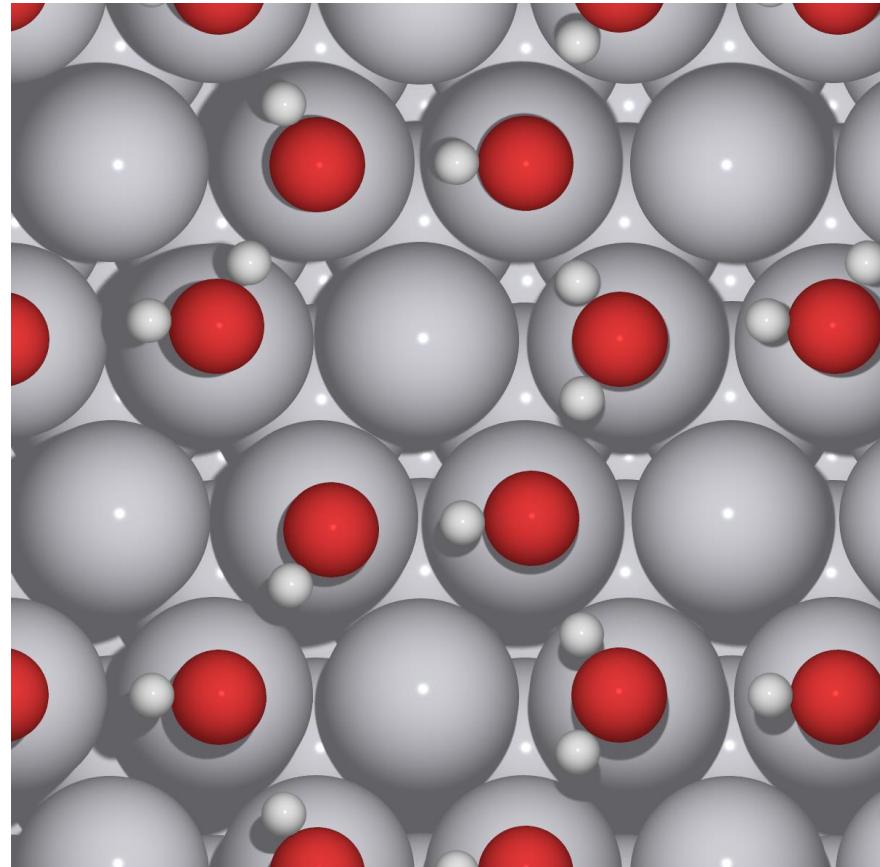
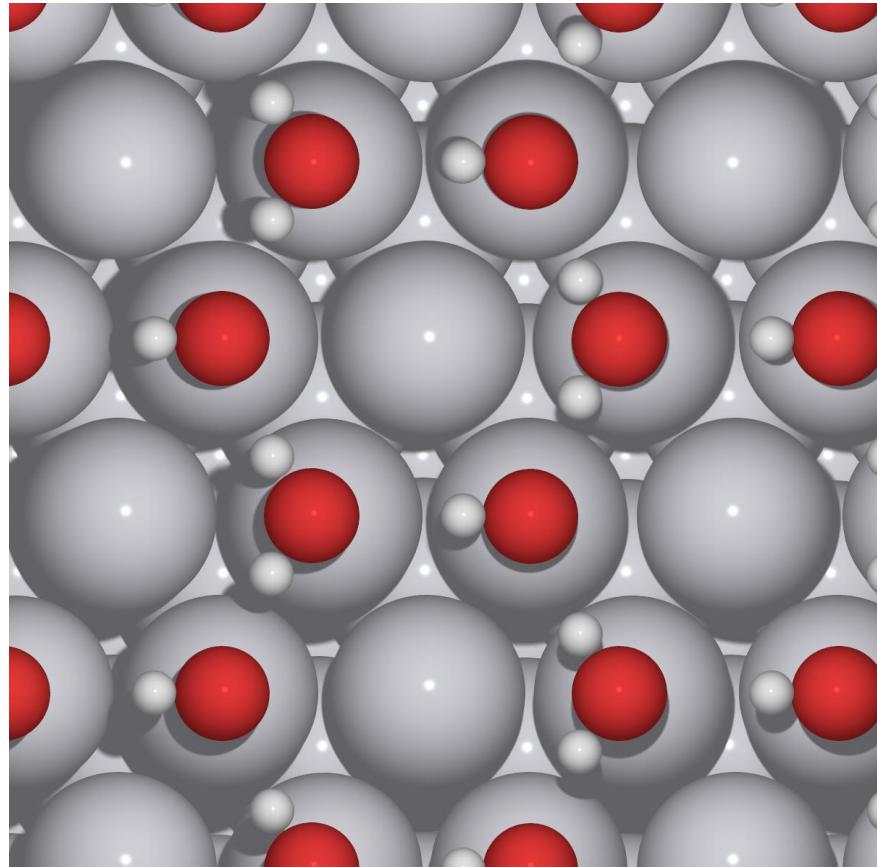
$$\Theta_{\text{OH}} = 1/3 \cdot 1/(1 + \exp((\Delta G_{\text{OH}} - eU)/kT))$$



Stamenkovic, Fowler, Mun, Wang, Ross, Lucas and Markovic, *Science*, 2007, **315**, 493-

Rossmisl, Karlberg, Jaramillo, Nørskov, *Faraday Discussions* **140**, (2008) 337-346

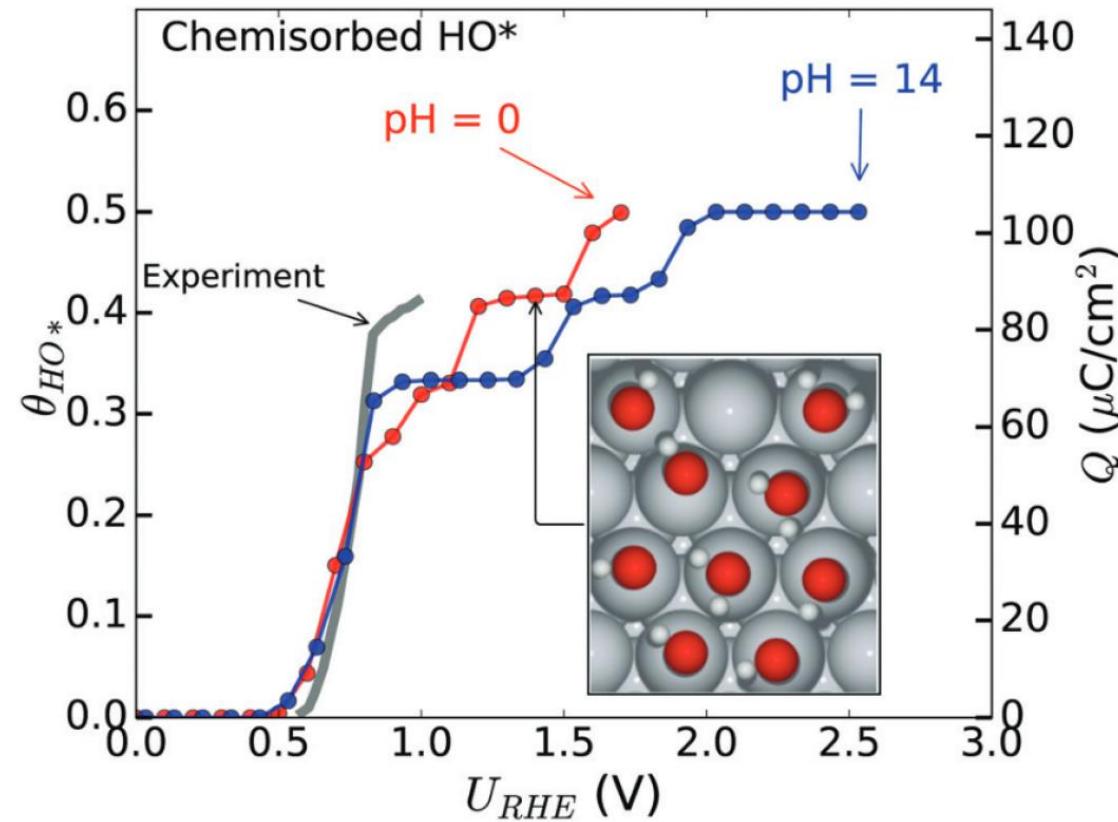
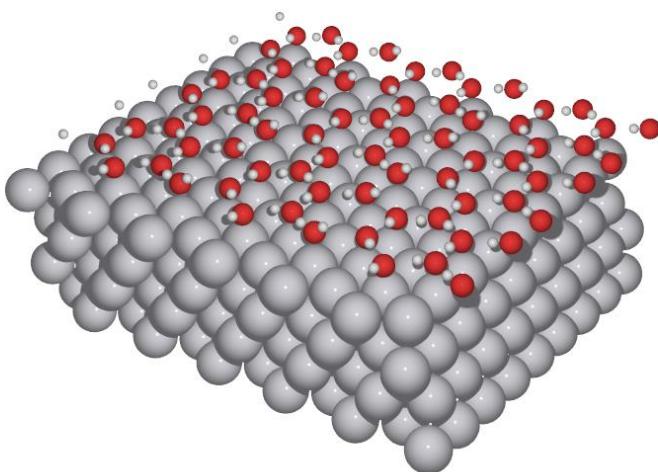




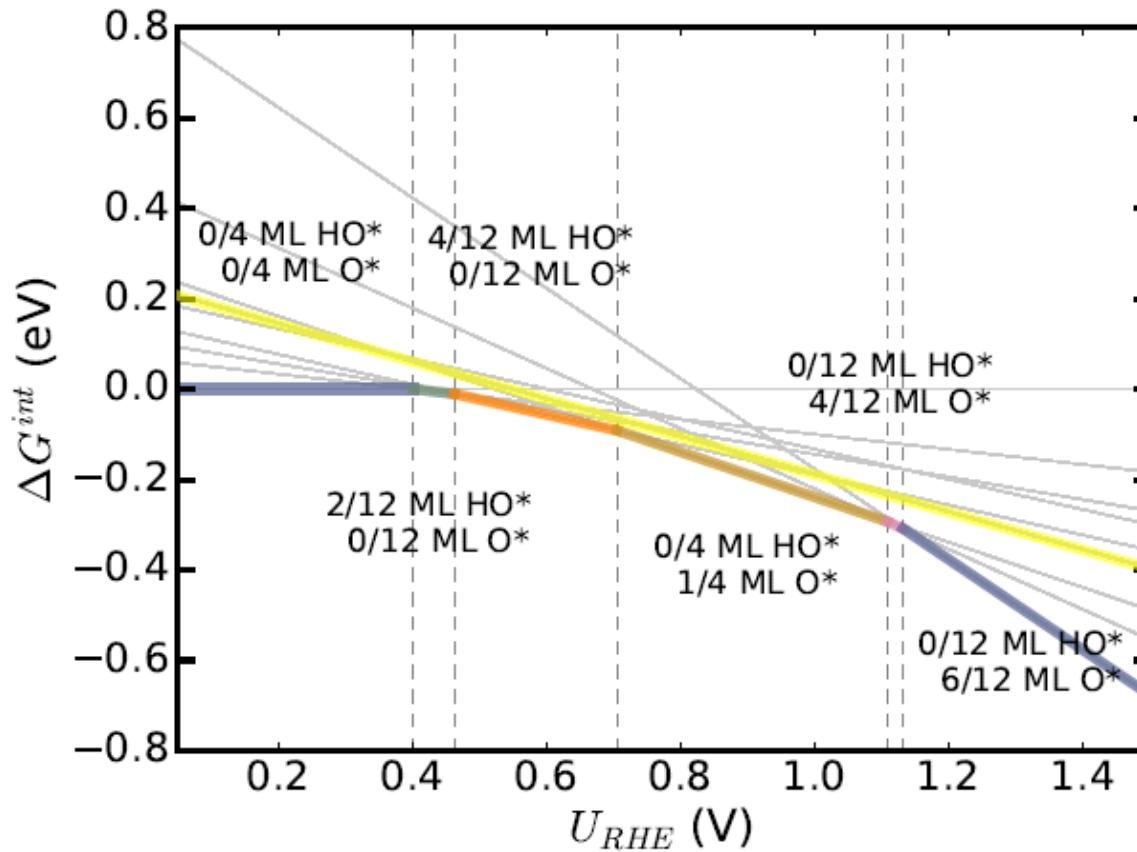
Sted og dato  
Dias 46



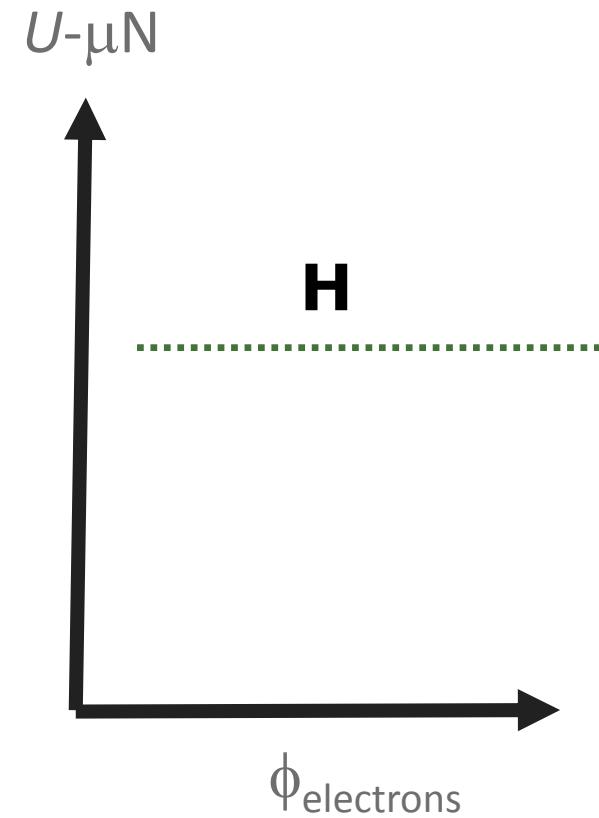
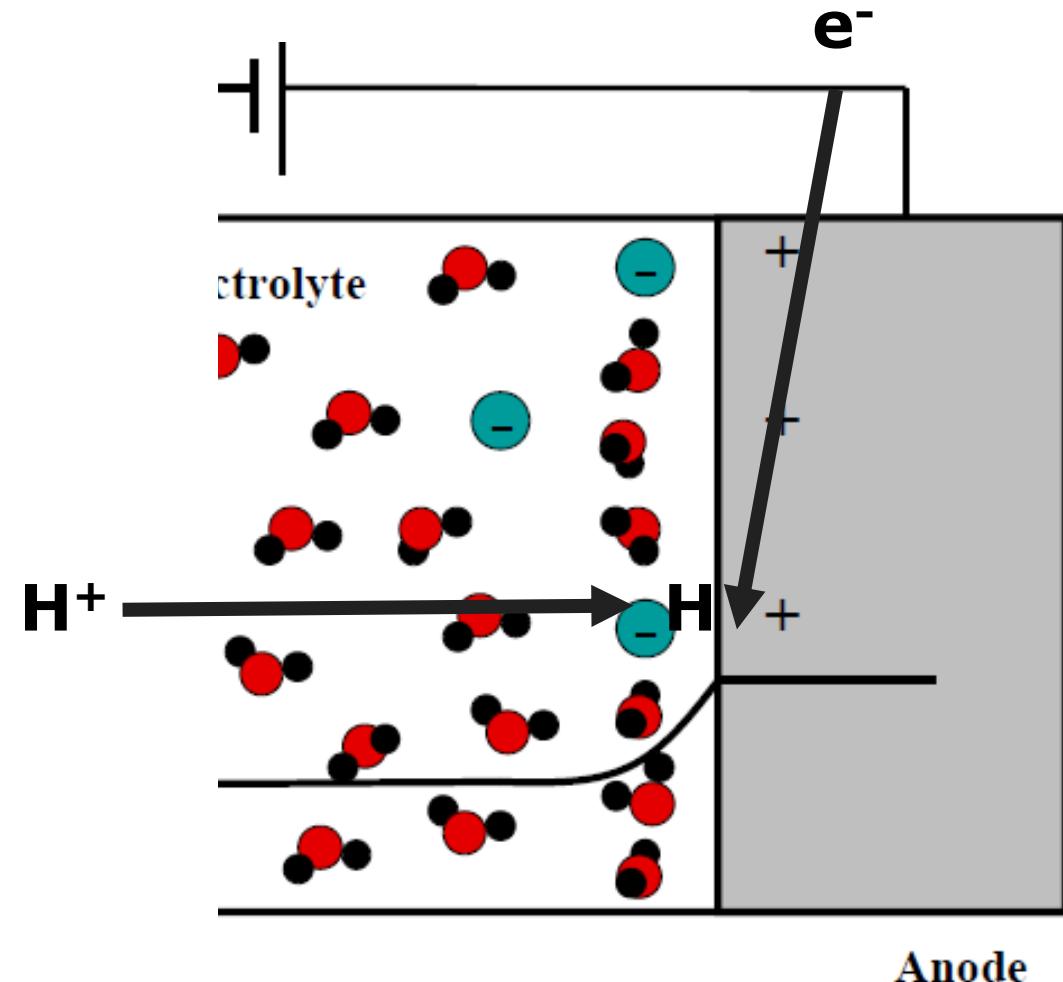
# Structure of OH and H<sub>2</sub>O on Pt(111)



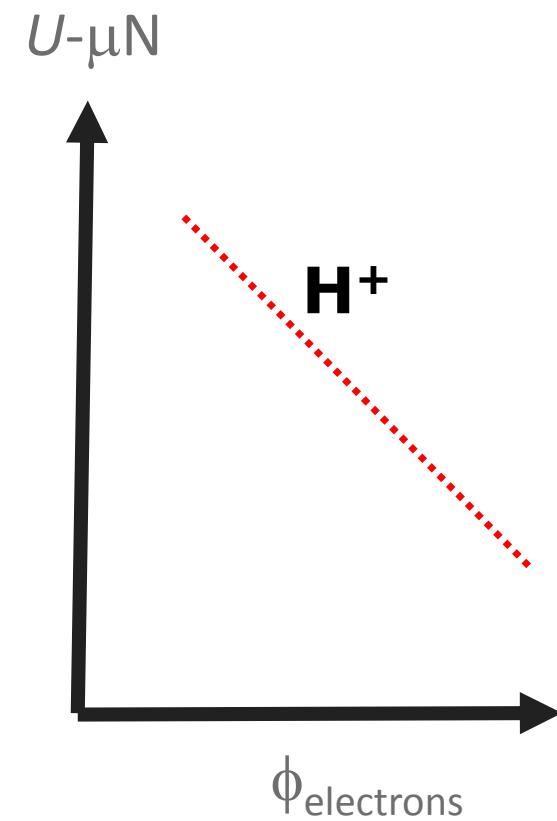
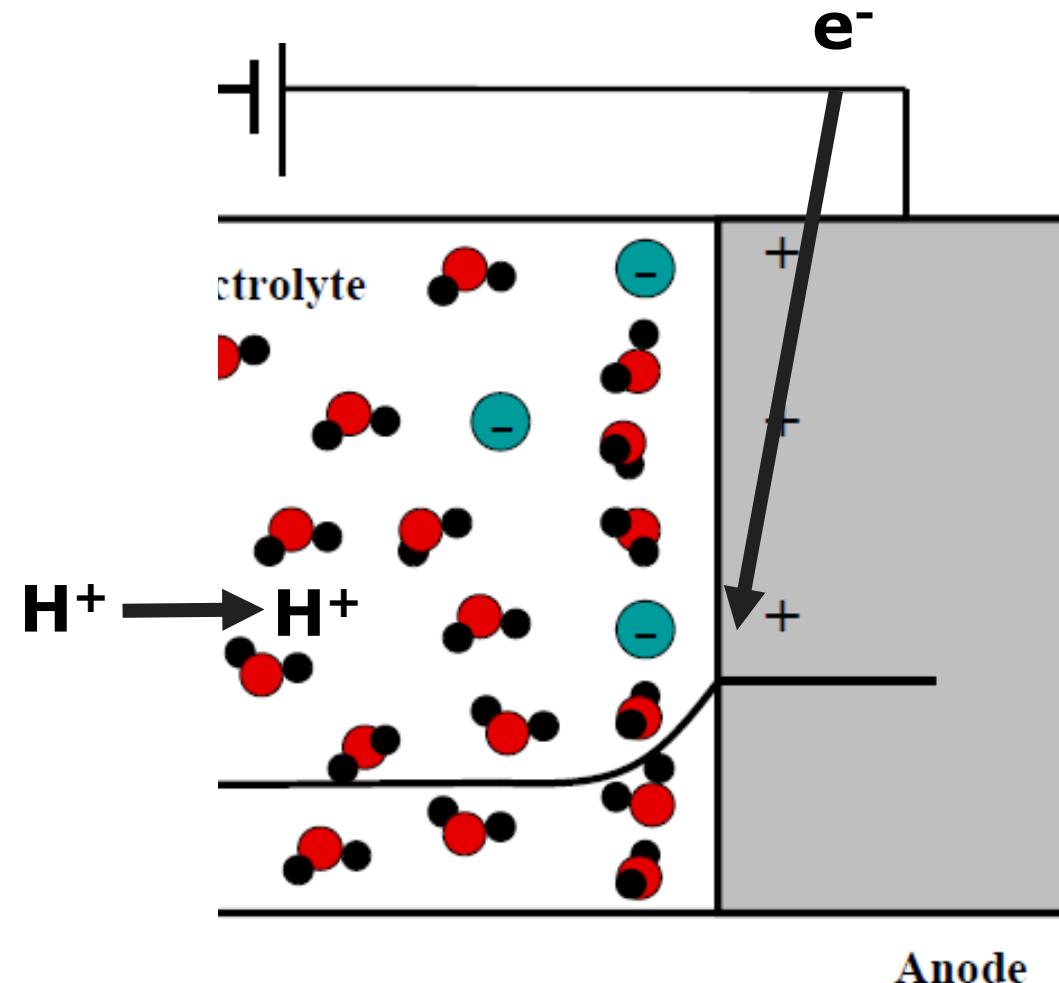
Hansen, Nilsson, Rossmeisl, PCCP, 2017



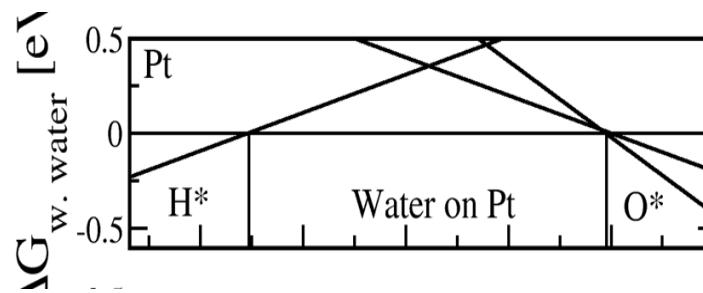
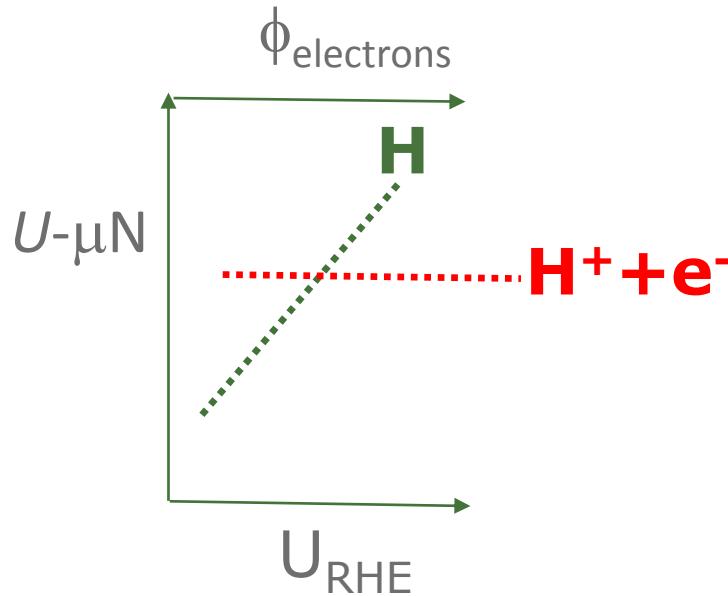
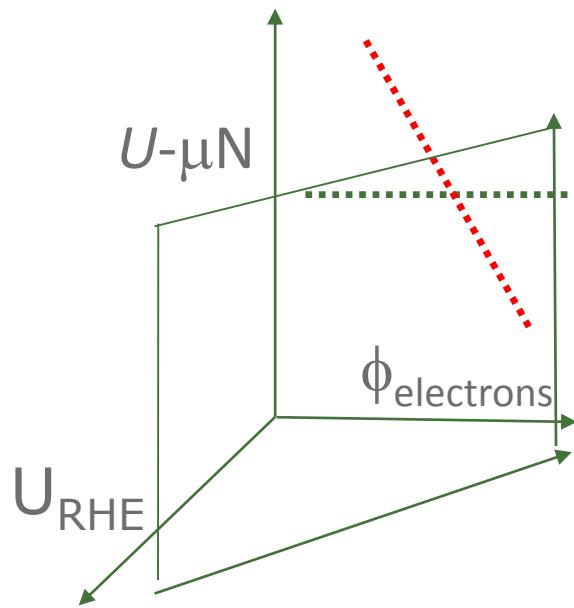
## Charge tranfer?



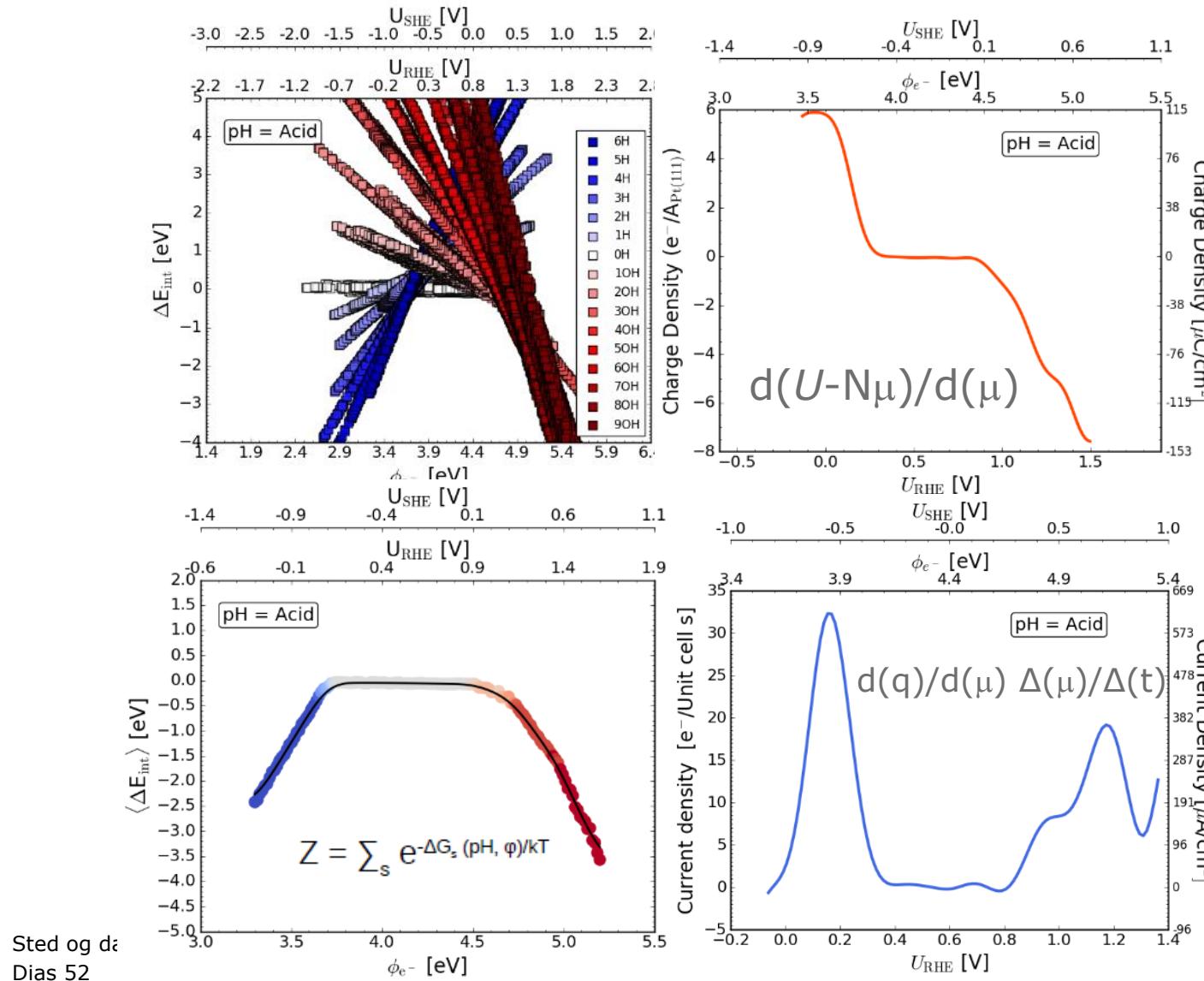
## Open system



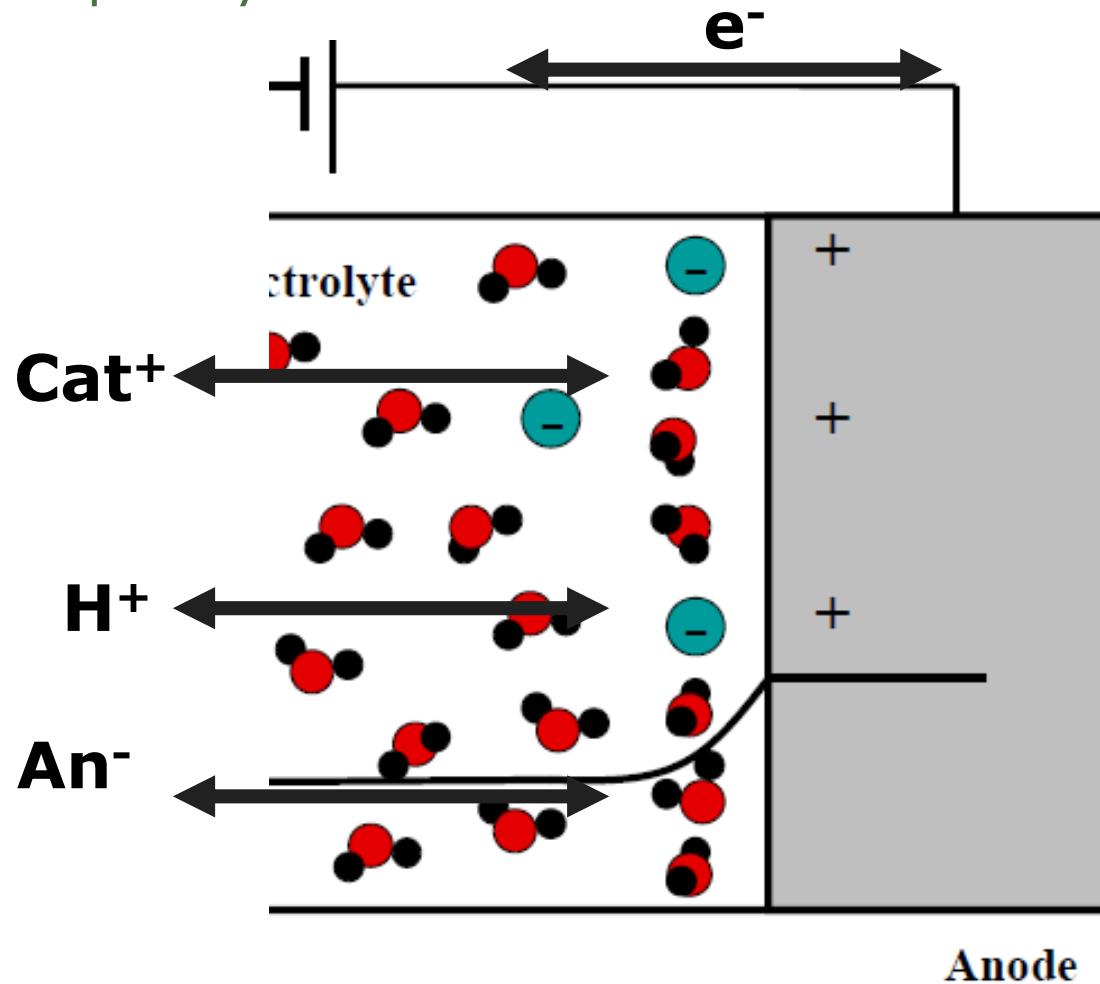
# Coupled proton electron transfer?



# From simulations to CV's

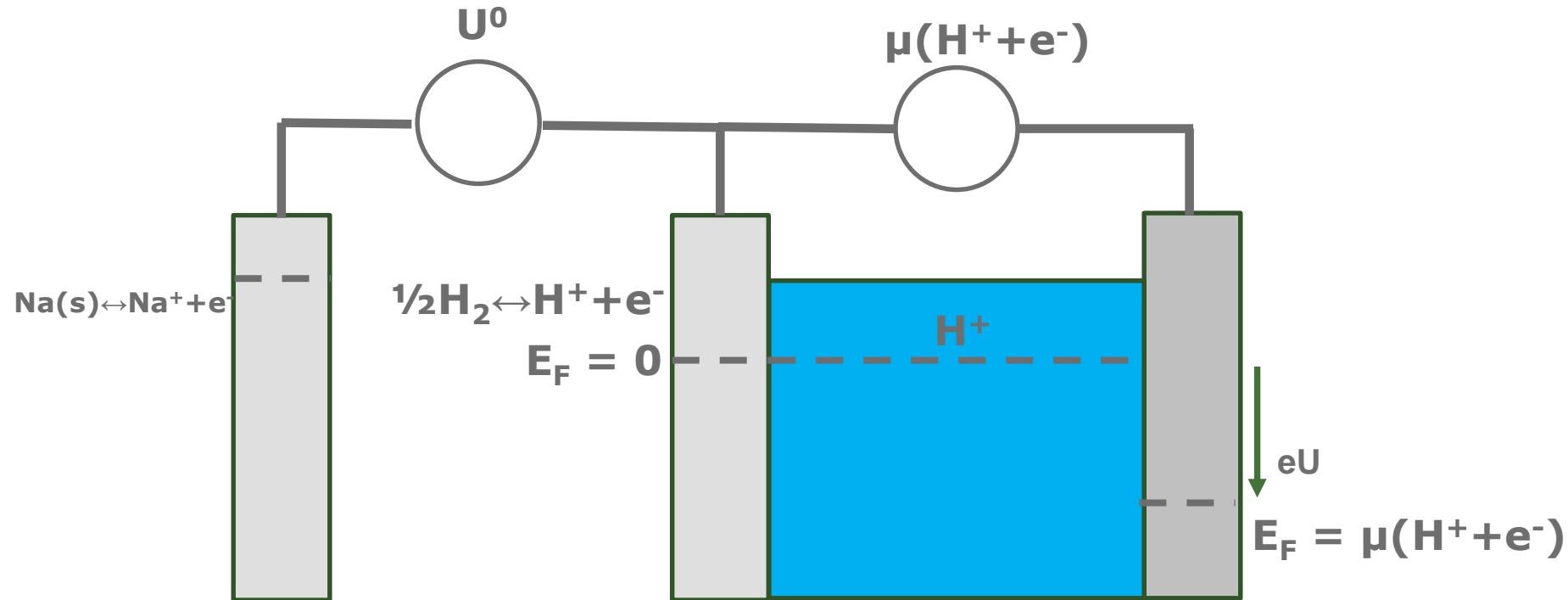


## Open system





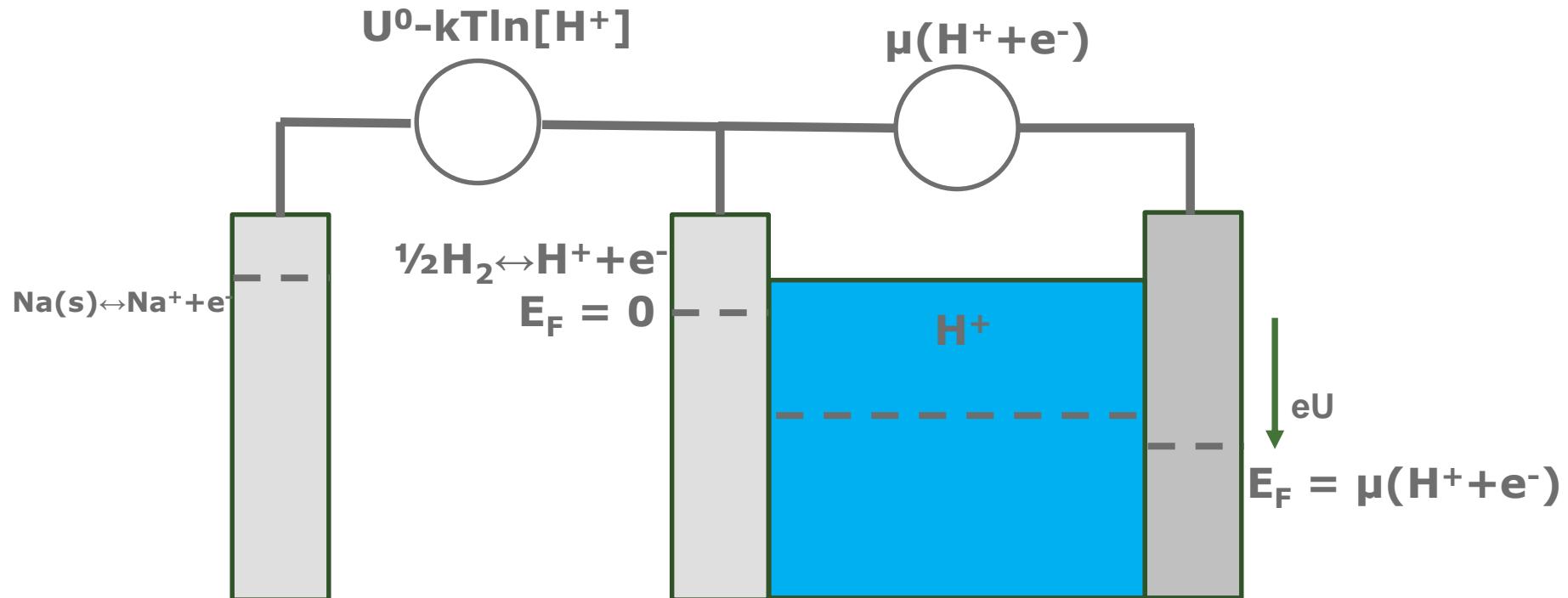
pH = 0,  $[Na^+] = 1M$





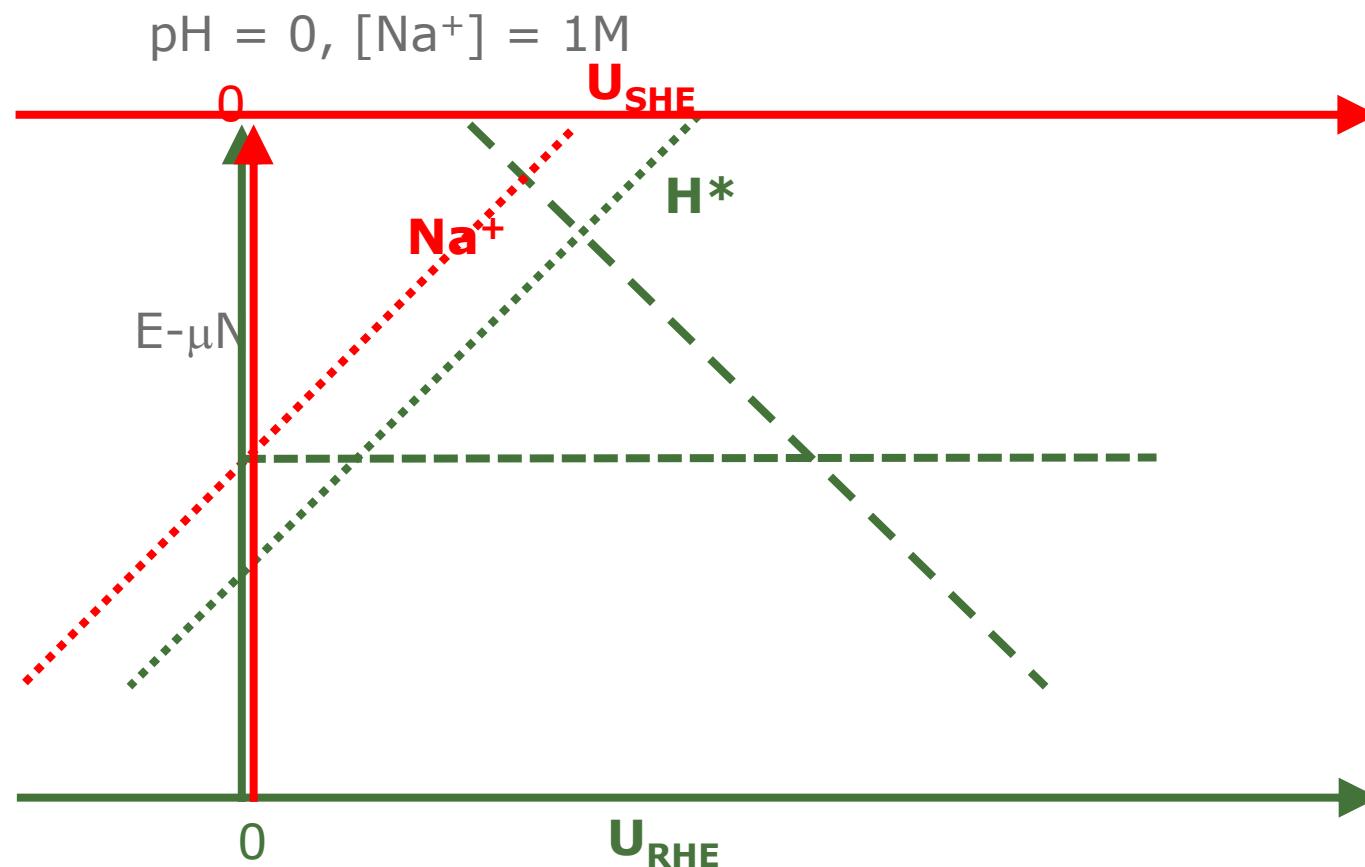
## Faculty of Science

$$\text{pH} = 14, [\text{Na}^+] = 1\text{M}$$



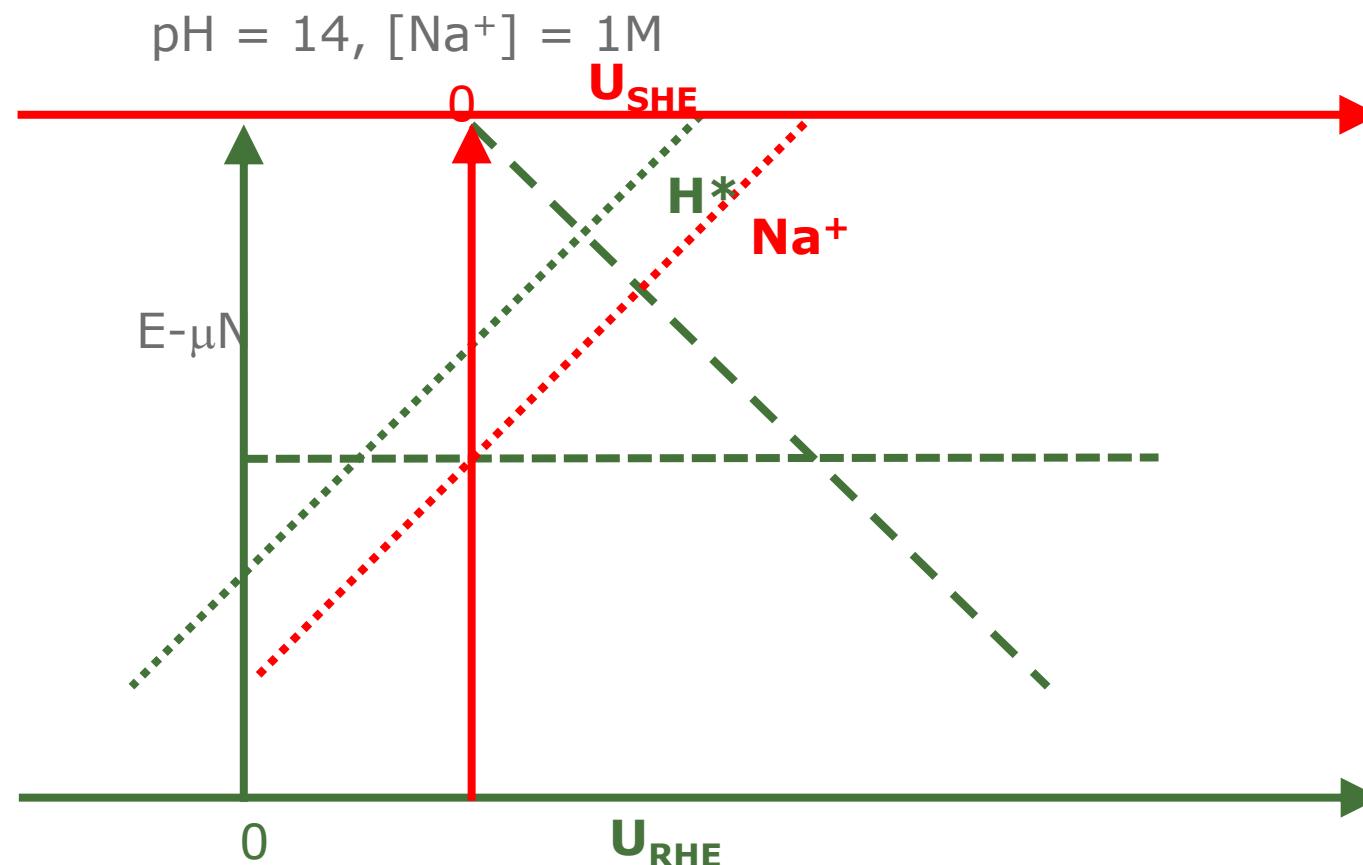


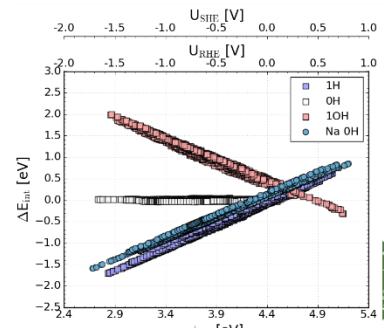
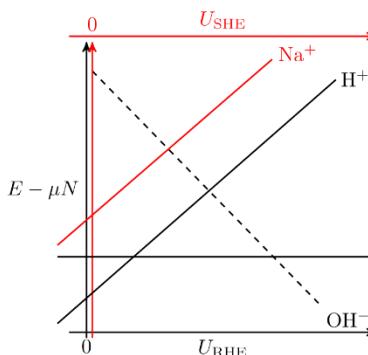
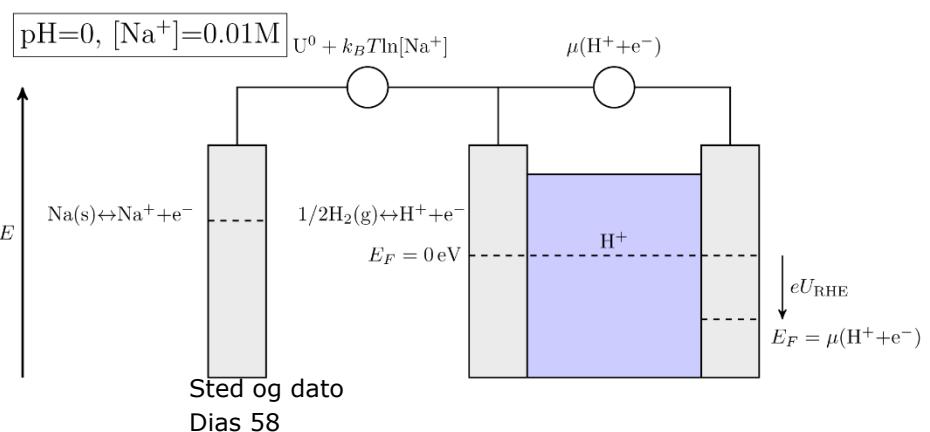
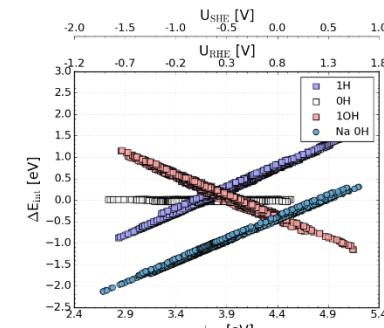
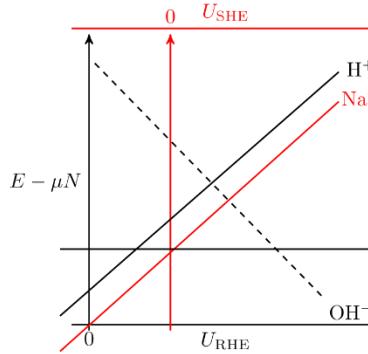
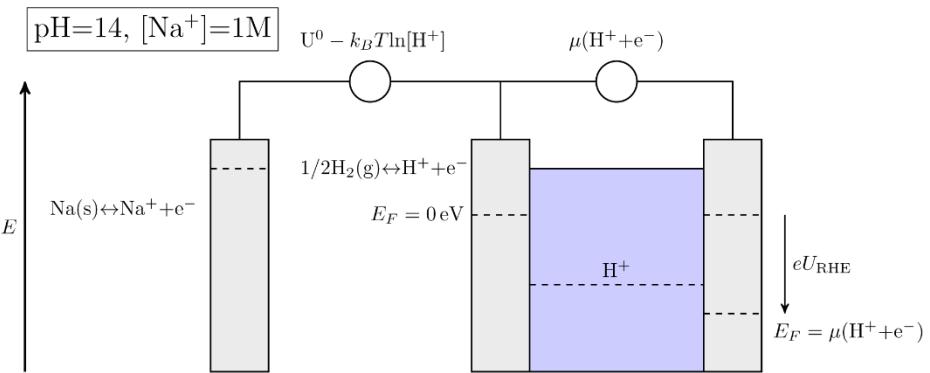
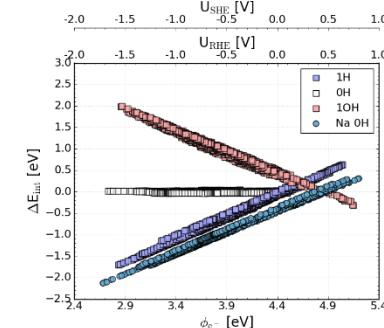
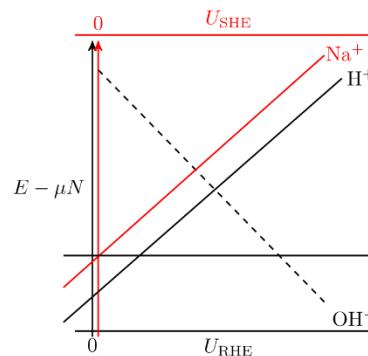
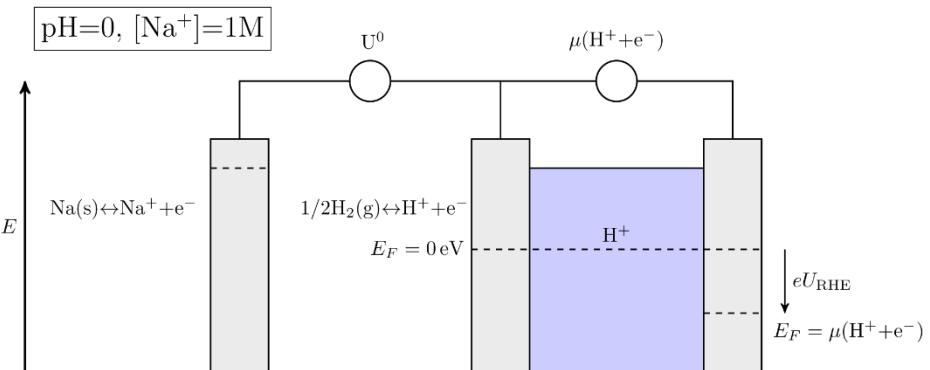
## Faculty of Science



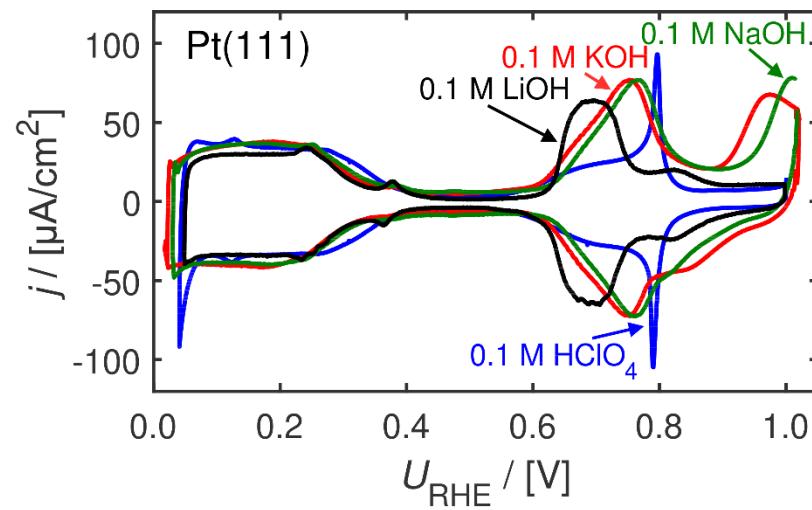
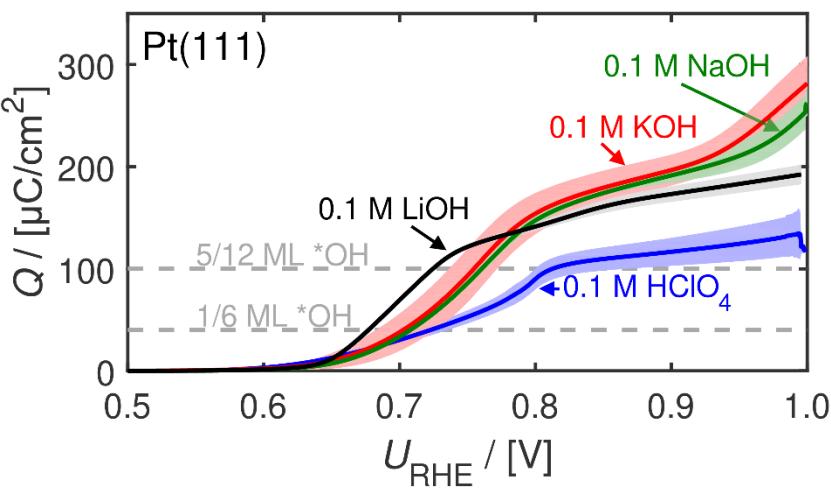


## Faculty of Science





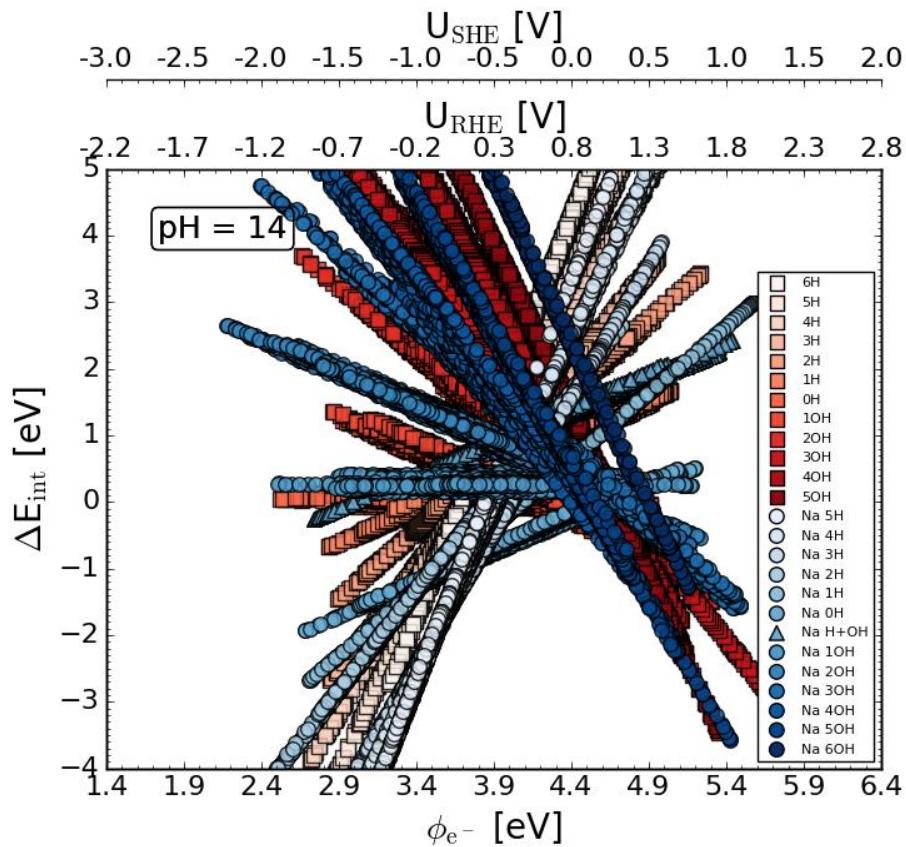
# Pt (111) in Acid and Base



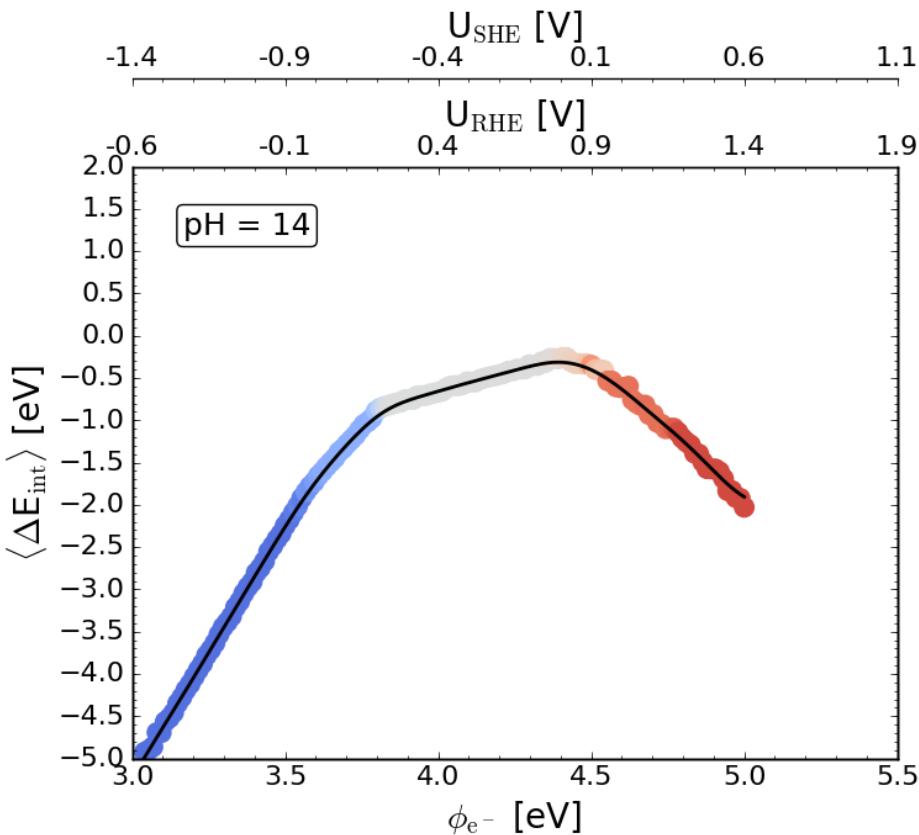
Kim Deng Jensen



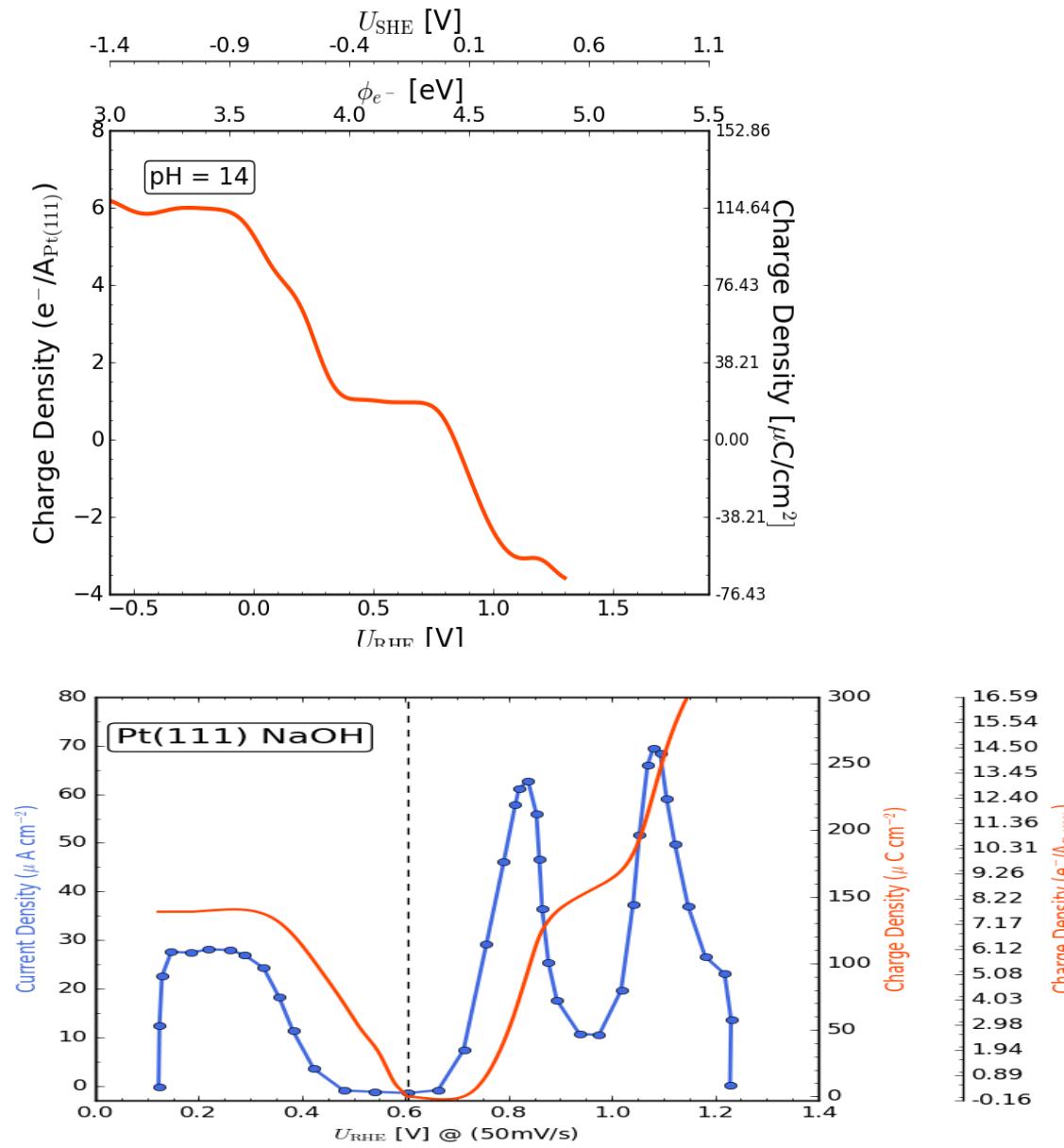
# Pt(111) NaOH



Sted og dato  
Dias 60



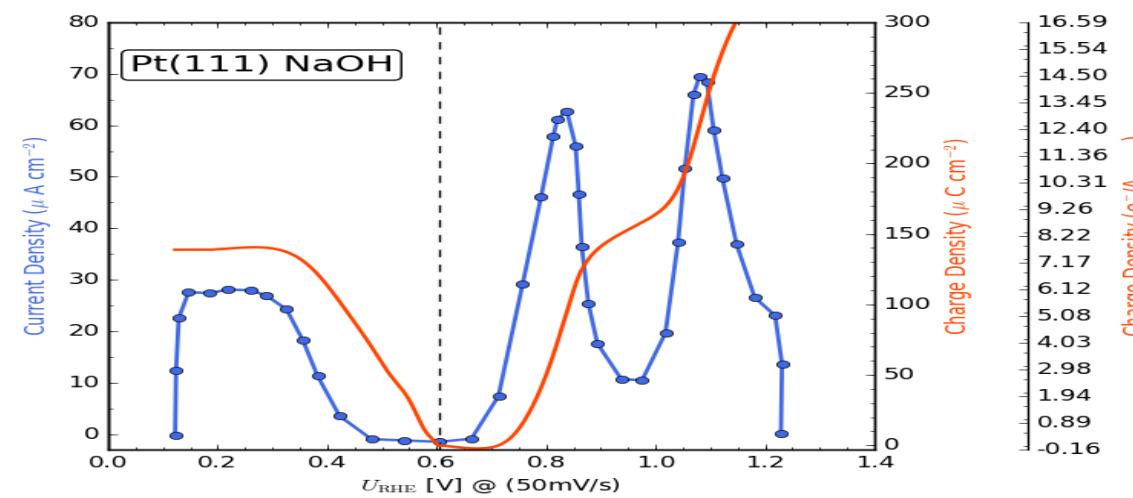
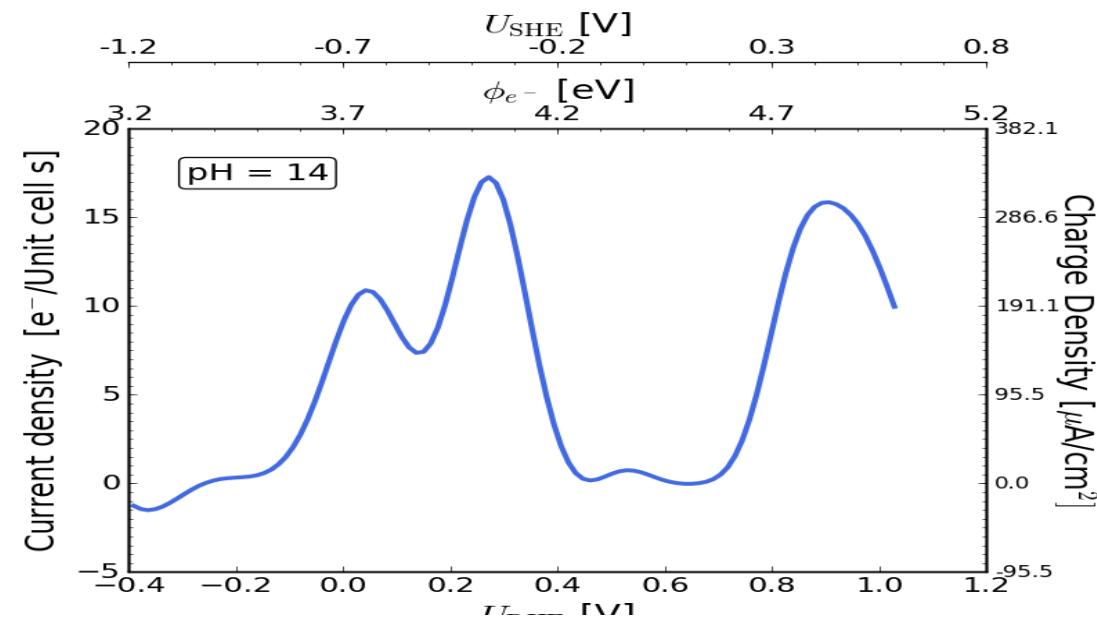
# Pt 111 in NaOH



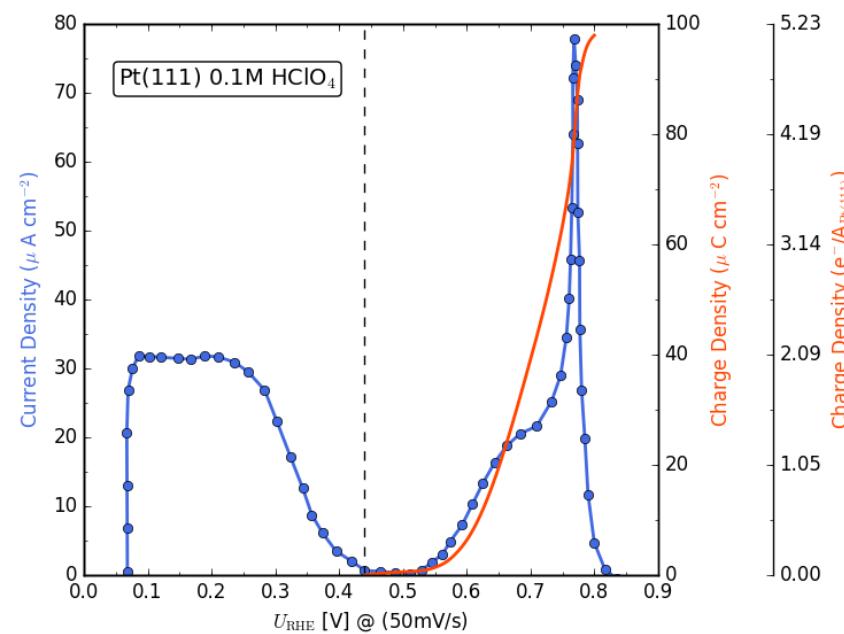
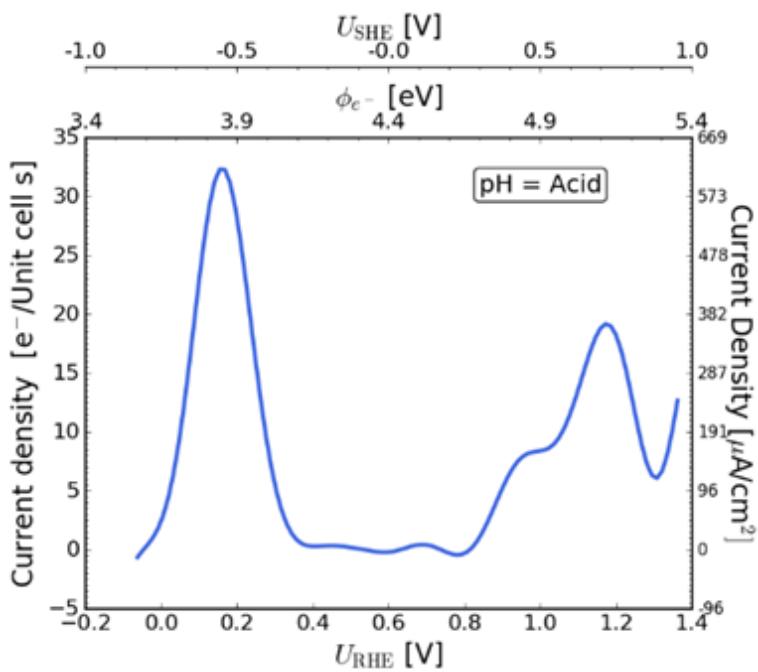
Sted og dato  
Dias 61



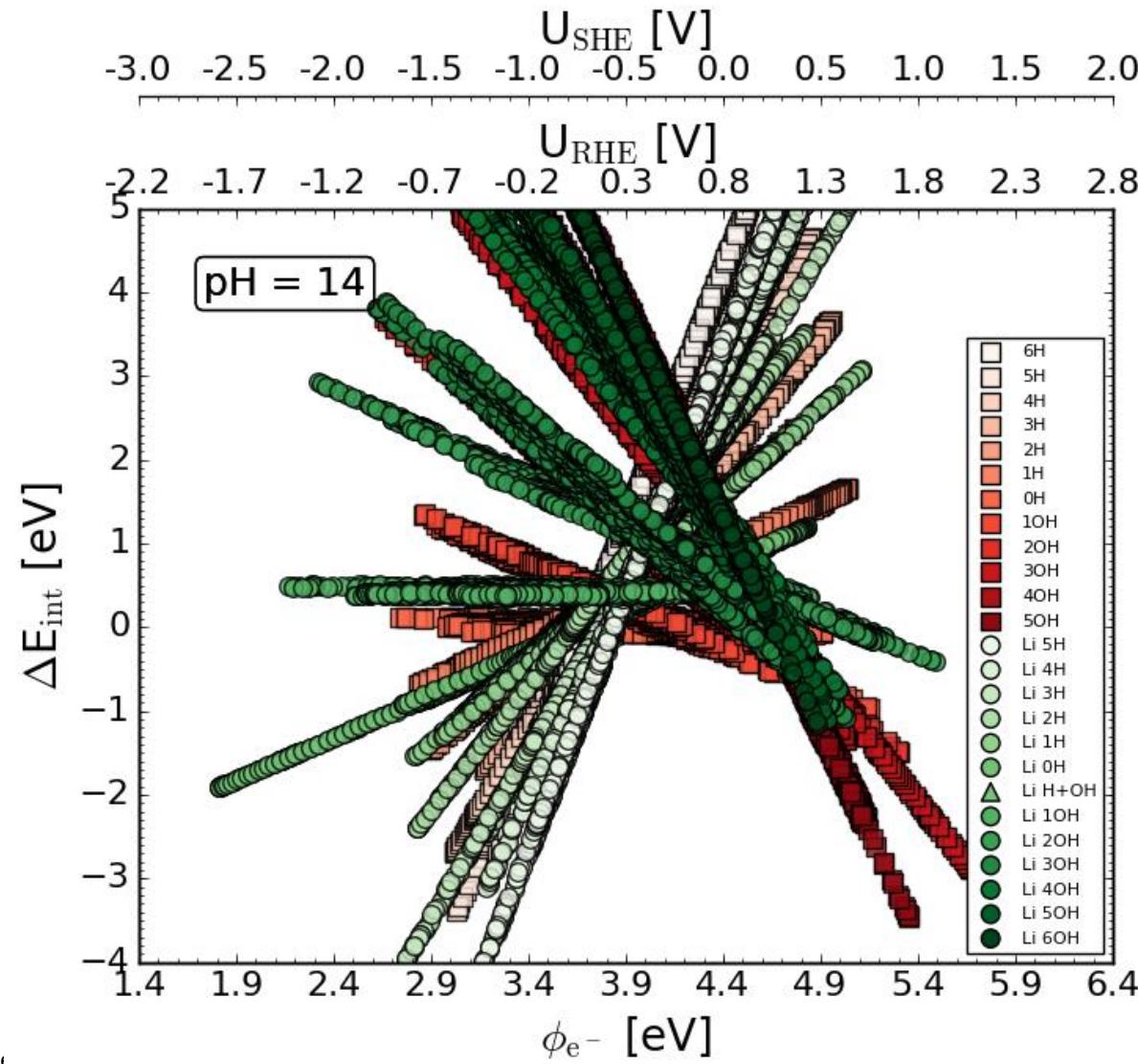
# Pt (111) in NaOH



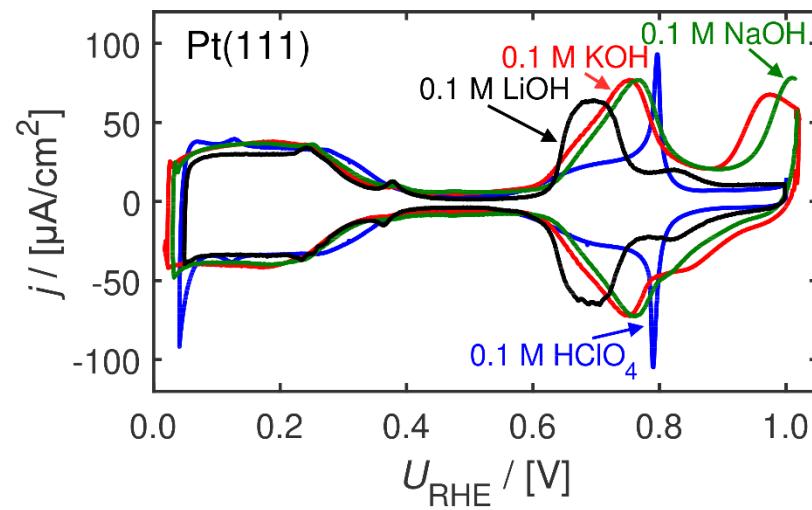
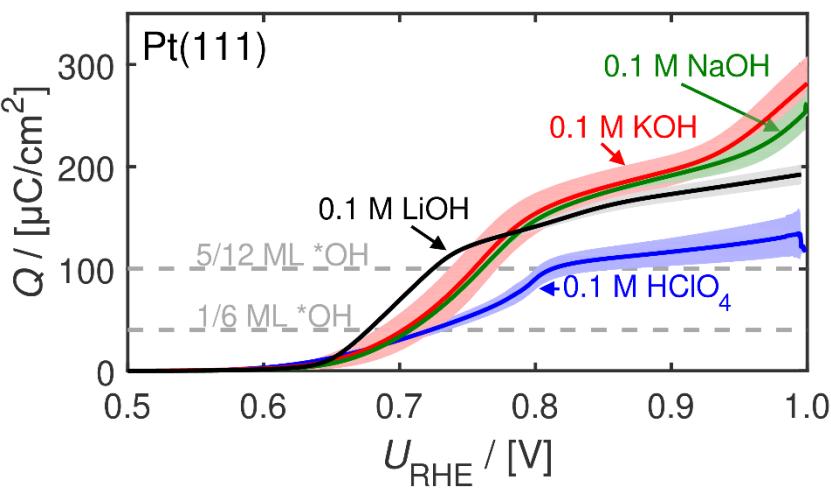
# CV – in acid



# Pt (111) in LiOH



# Pt (111) in Acid and Base LiOH similar to acid



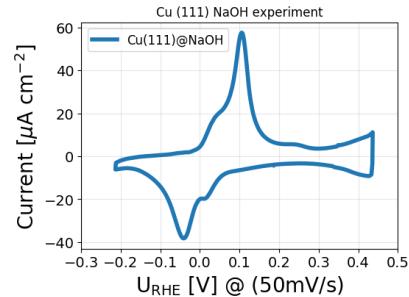
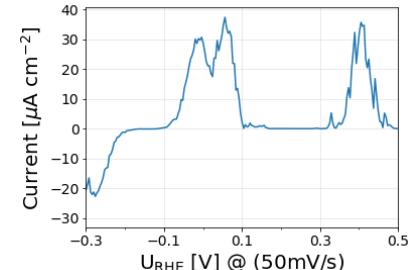
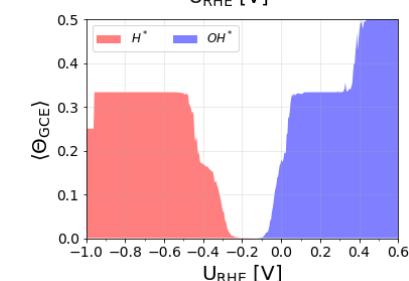
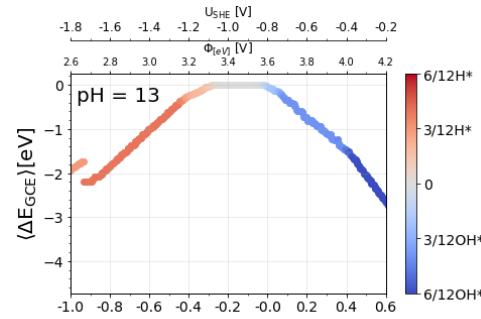
Kim Deng Jensen



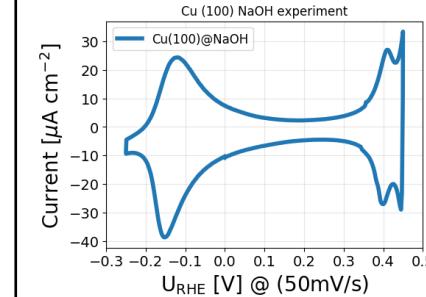
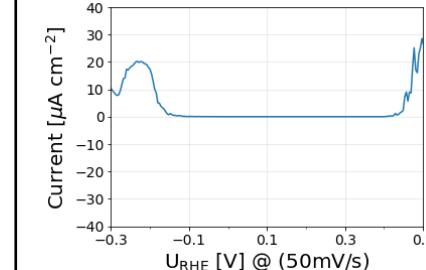
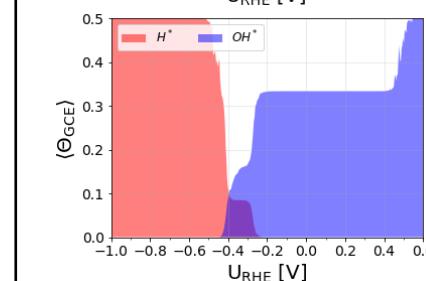
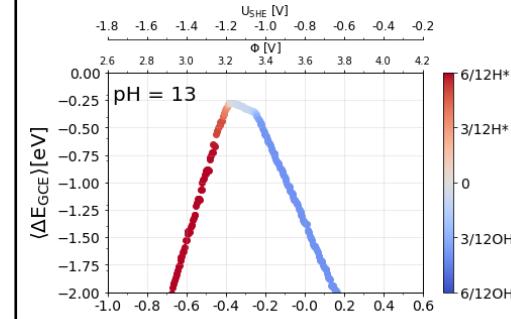
**Alkaline  
(Aqueous)  
pH=13,**

**0.1 [M]  
NaOH**

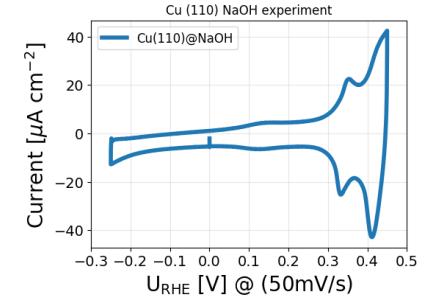
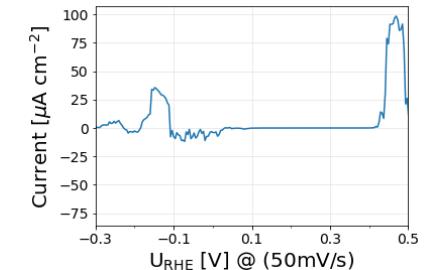
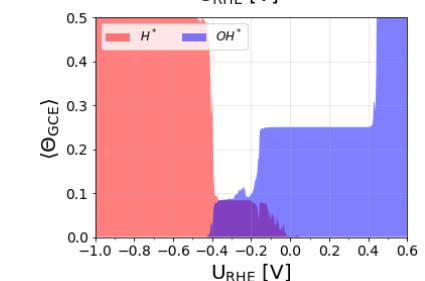
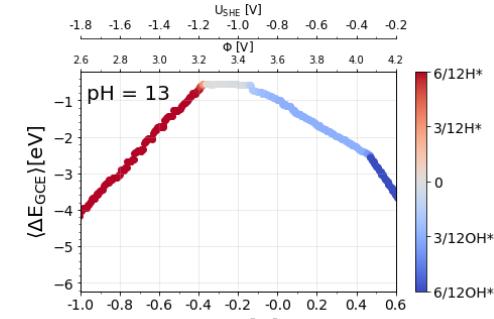
# Cu(111)



# Cu(100)

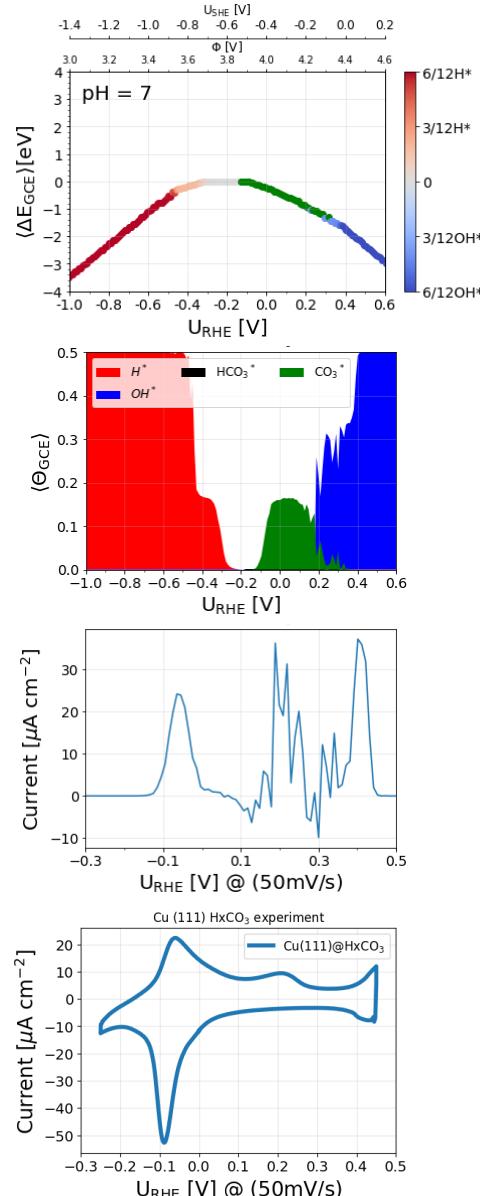


# Cu(110)

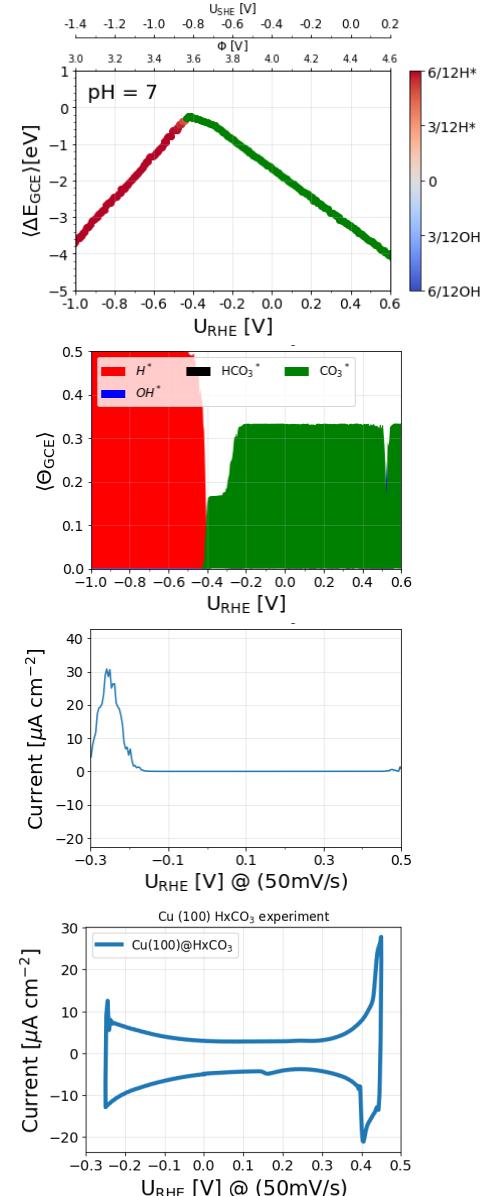


**Neutral  
pH=7,  
0.1 [M]  
 $\text{H}_x\text{CO}_3$**

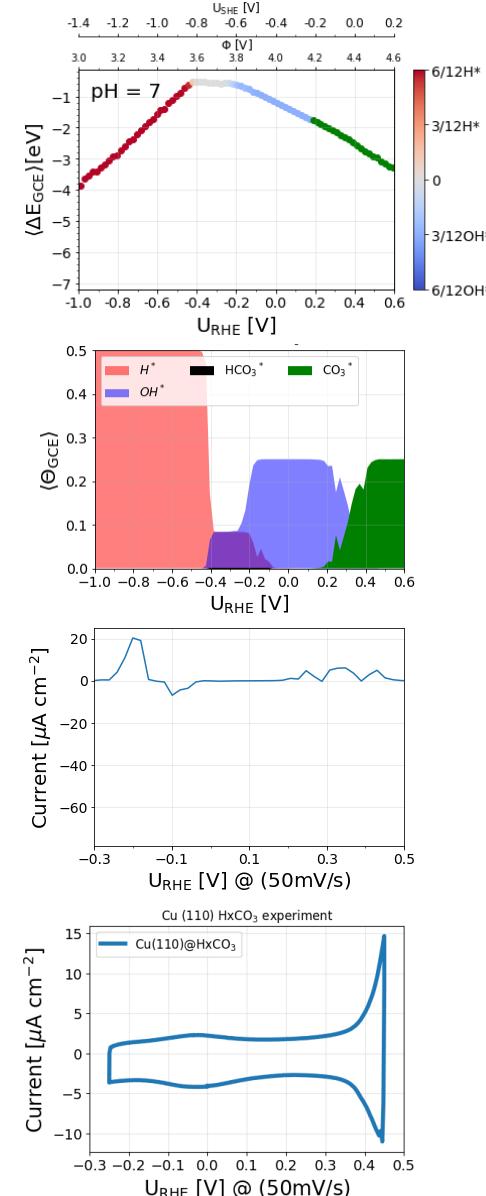
# Cu(111)



# Cu(100)

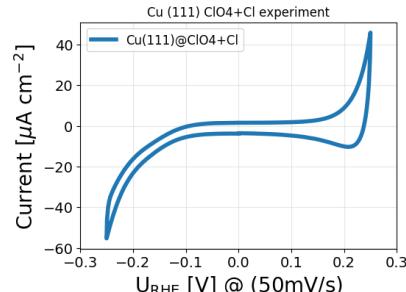
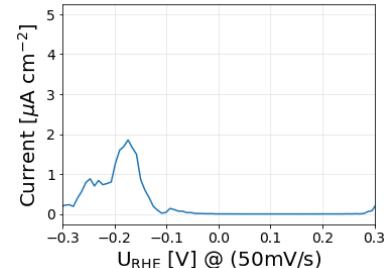
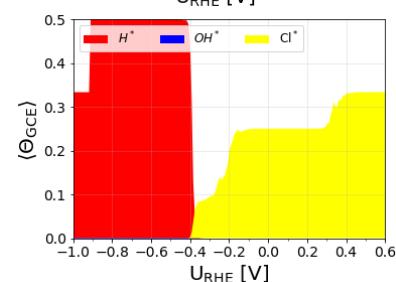
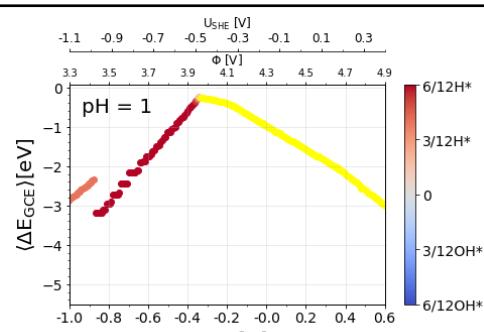


# Cu(110)

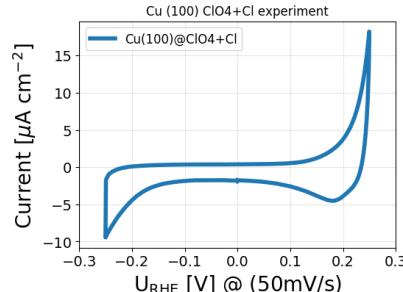
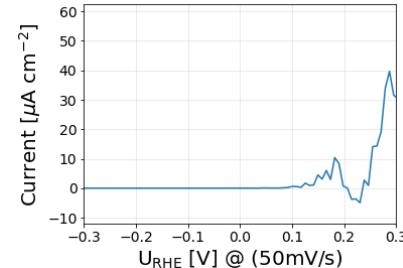
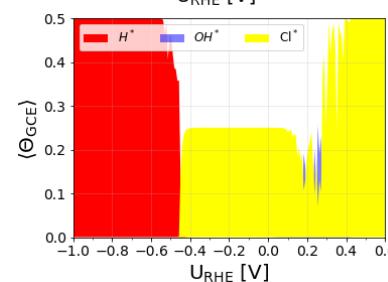
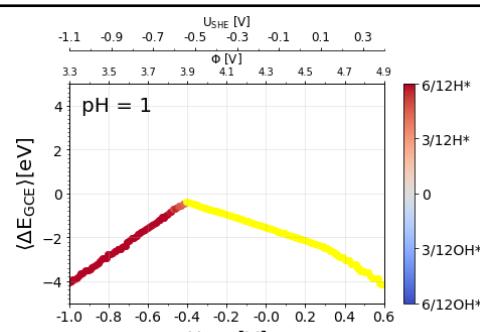


**Acidic**  
**pH=1,**  
**0.1M**  
 $\text{[HClO}_4]$   
 $+ \text{[Cl]}$

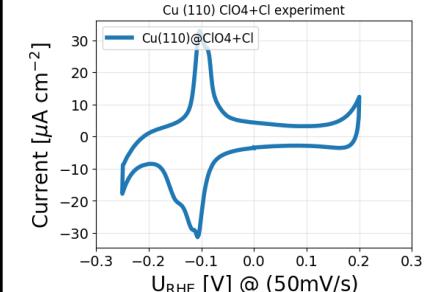
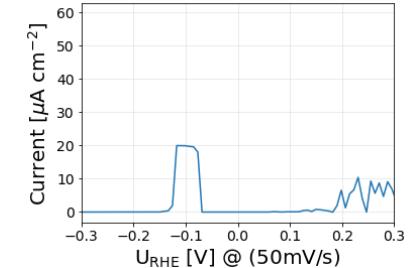
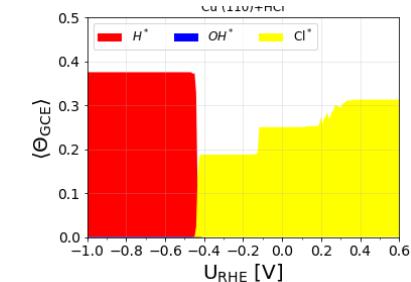
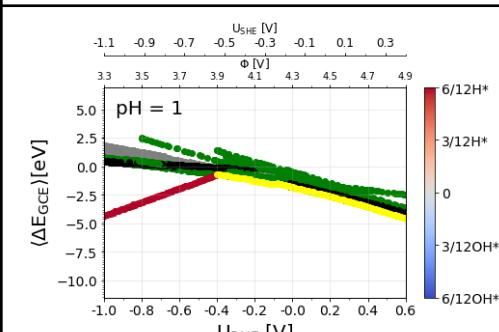
# Cu(111)



# Cu(100)

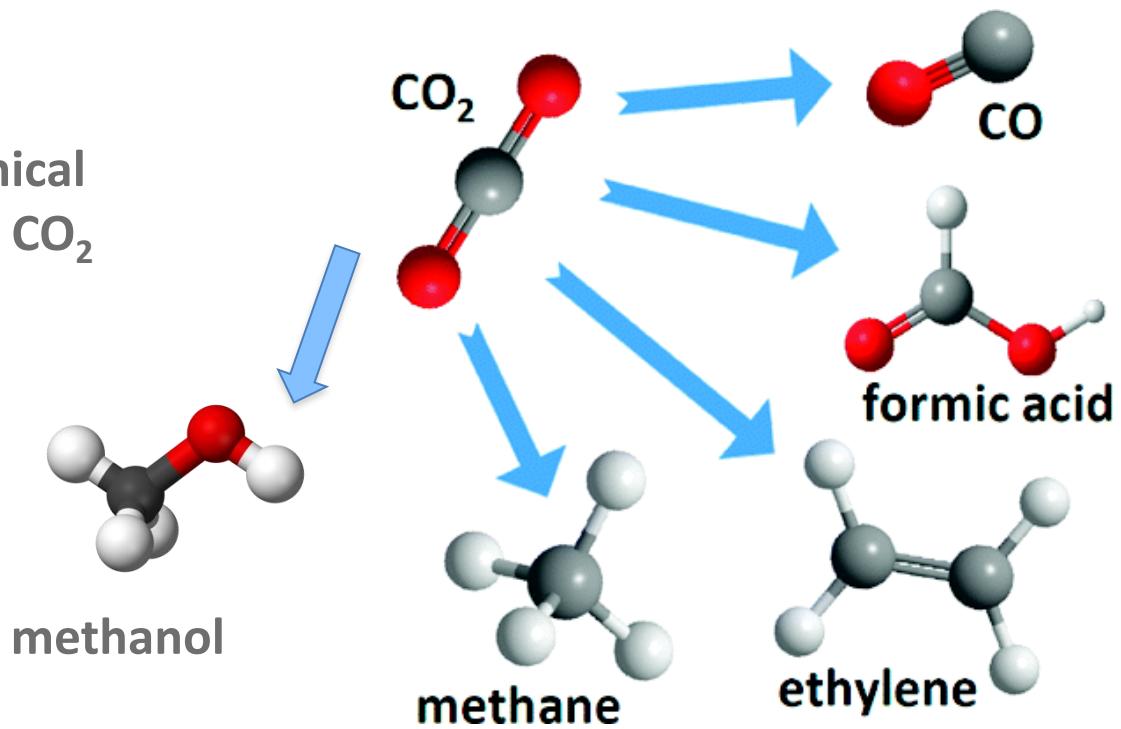


# Cu(110)



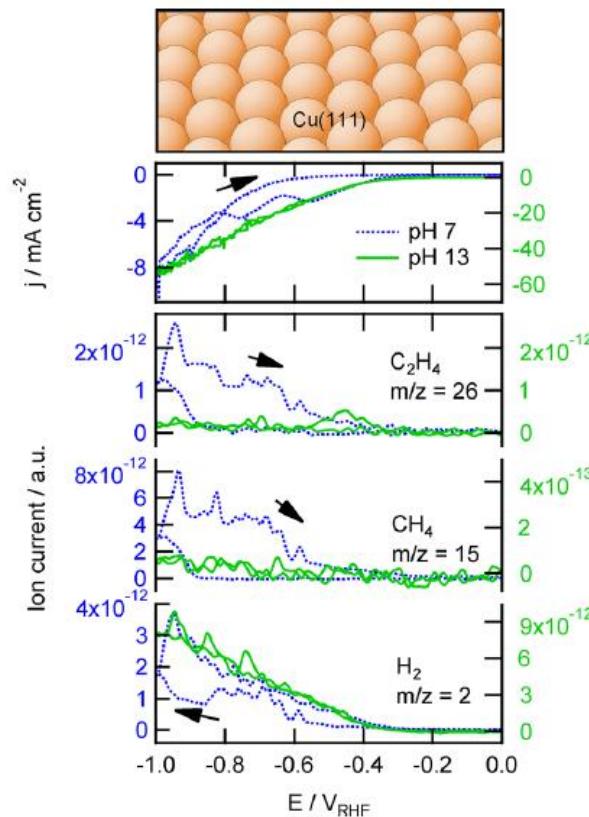


## Electrochemical reduction of CO<sub>2</sub>

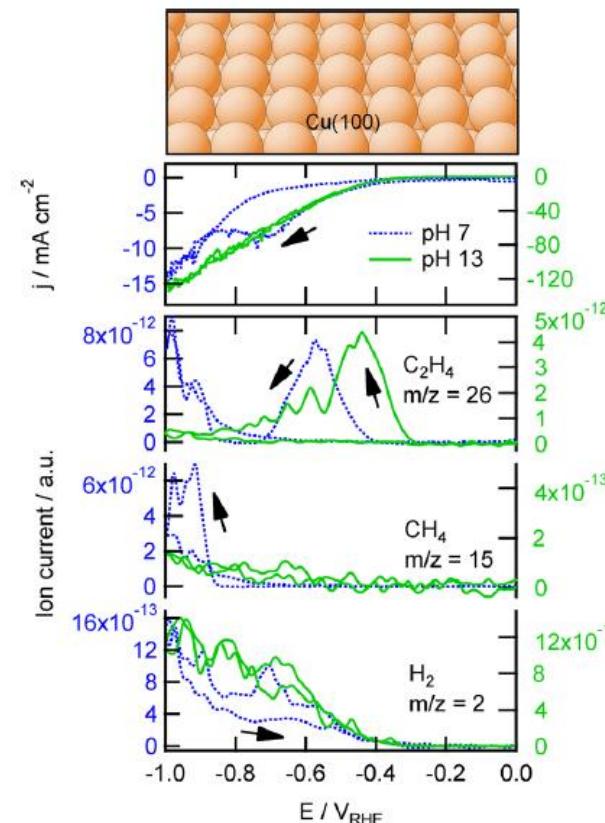


## Two Pathways for the Formation of Ethylene in CO Reduction on Single-Crystal Copper Electrodes

Klaas Jan P. Schouten, Zisheng Qin, Elena Pérez Gallent, and Marc T. M. Koper\*



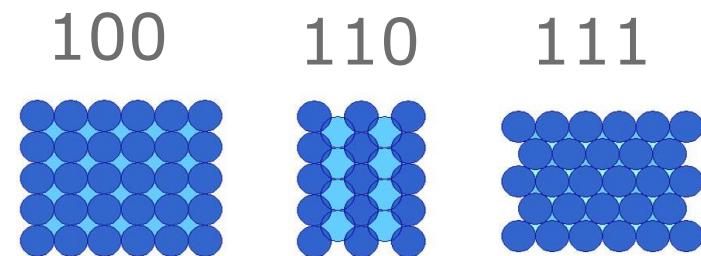
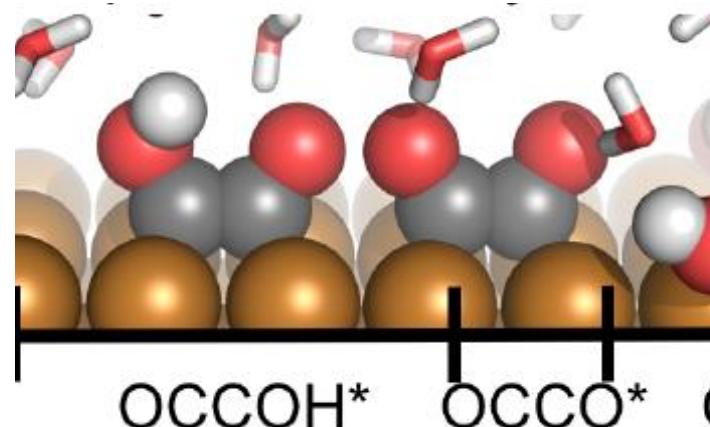
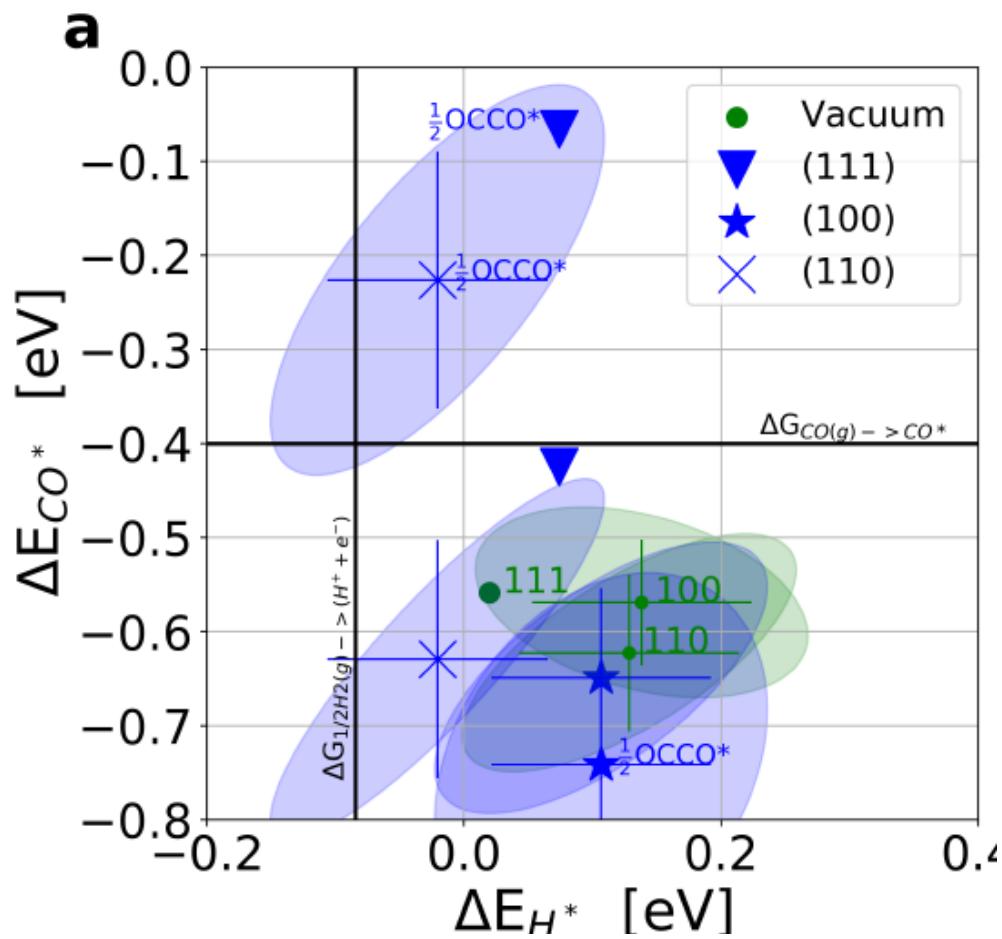
**Figure 1.** Top: (111) facet of the copper fcc crystal. Middle: cyclic voltammograms for the reduction of a saturated solution of CO (~1 mM) on Cu(111) in phosphate buffer (pH 7) and NaOH solution (pH 13). Bottom: associated mass fragments of volatile products measured with OLEMS. Data for pH 7 are shown with blue dotted lines and plotted against the left axis, and data for pH 13 are shown with green solid lines and plotted against the right axis.

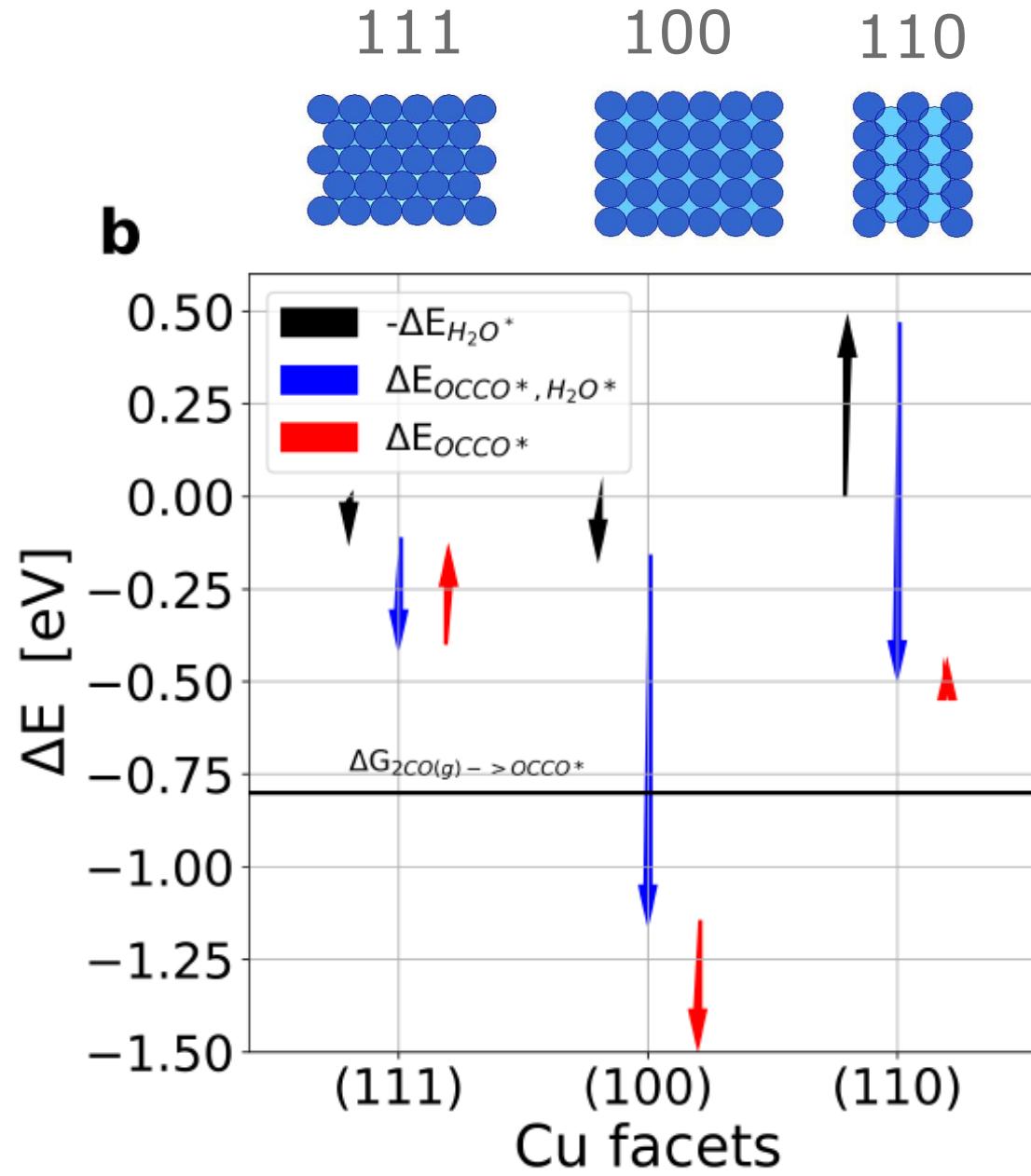


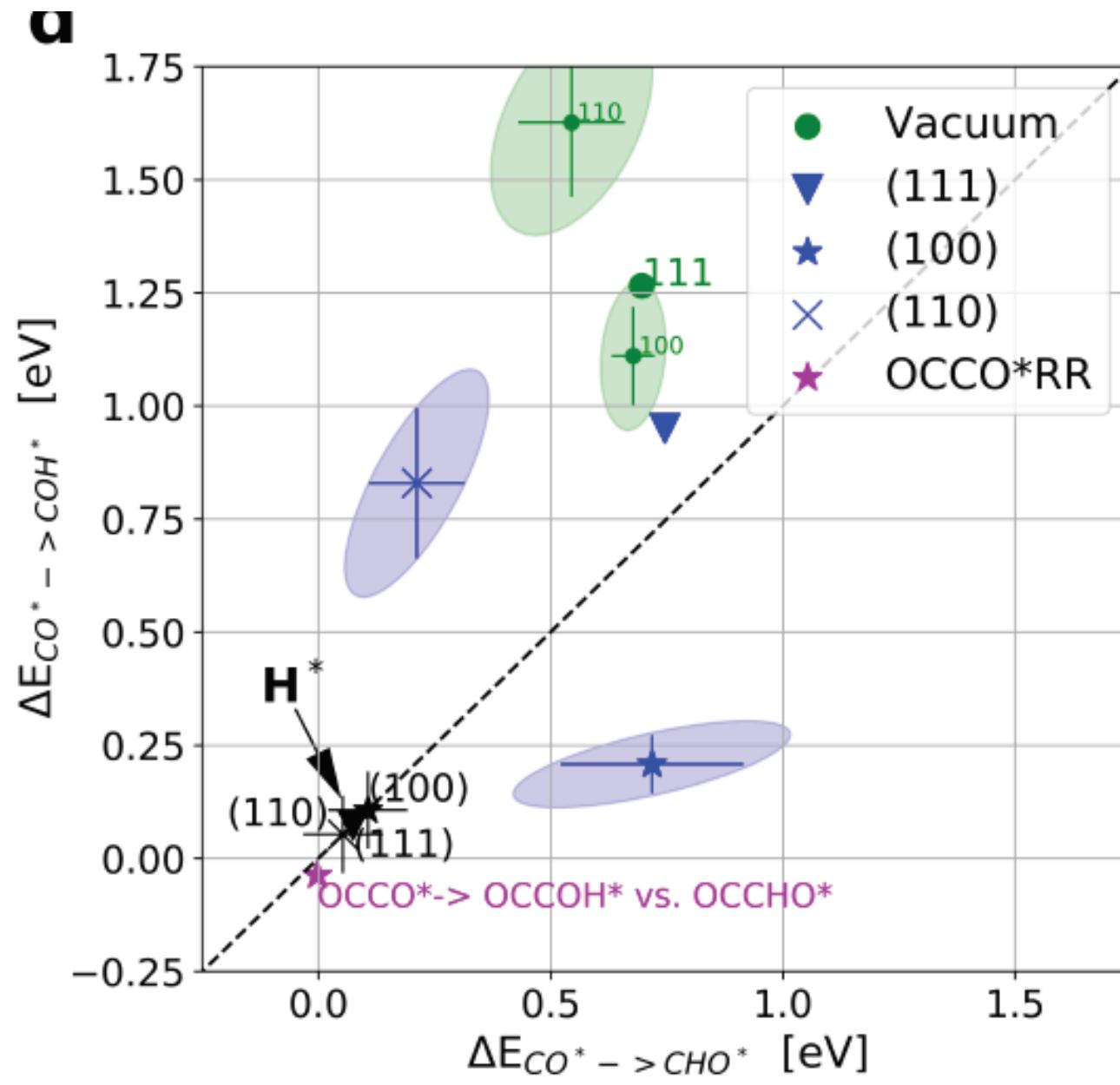
**Figure 2.** Top: (100) facet of the copper fcc crystal. Middle: cyclic voltammograms for the reduction of a saturated solution of CO (~1 mM) on Cu(100) in phosphate buffer (pH 7) and NaOH solution (pH 13). Bottom: associated mass fragments of volatile products measured with OLEMS. Data for pH 7 are shown with blue dotted lines and plotted against the left axis, and data for pH 13 are shown with green solid lines and plotted against the right axis.



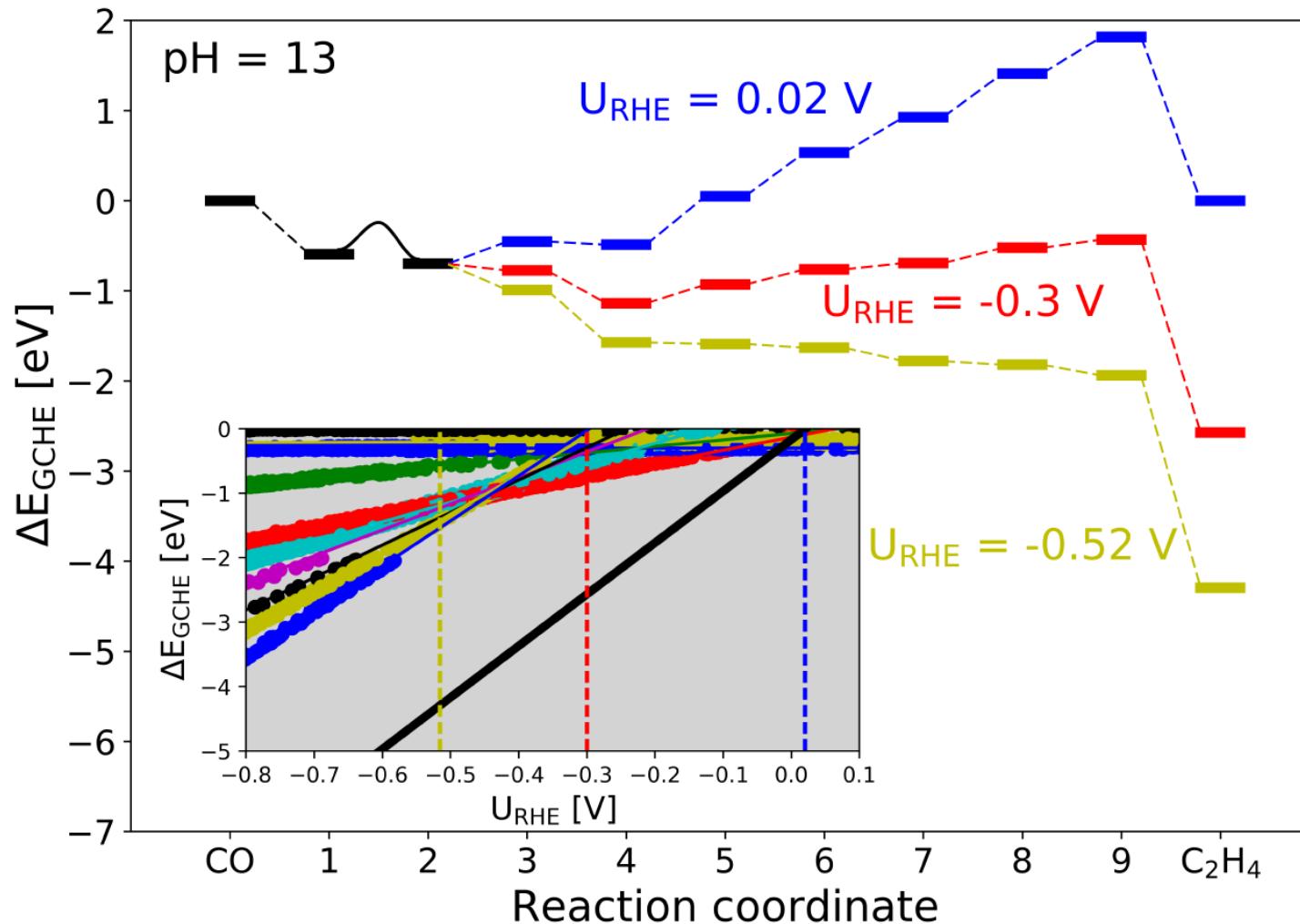
## OCCO





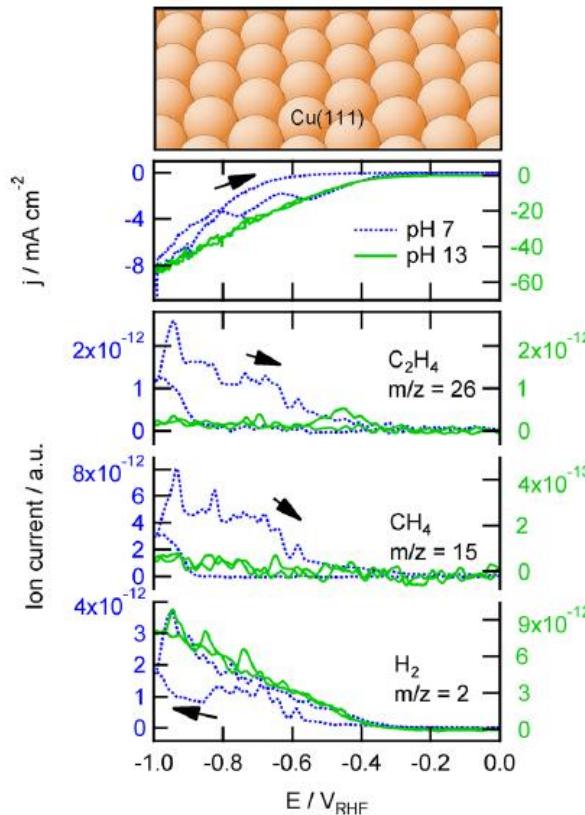


## C-C coupling

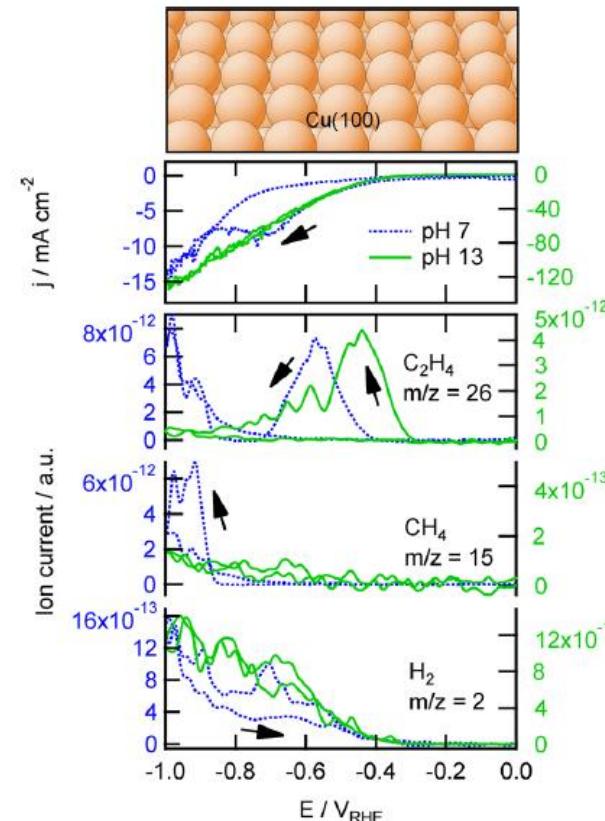


## Two Pathways for the Formation of Ethylene in CO Reduction on Single-Crystal Copper Electrodes

Klaas Jan P. Schouten, Zisheng Qin, Elena Pérez Gallent, and Marc T. M. Koper\*



**Figure 1.** Top: (111) facet of the copper fcc crystal. Middle: cyclic voltammograms for the reduction of a saturated solution of CO (~1 mM) on Cu(111) in phosphate buffer (pH 7) and NaOH solution (pH 13). Bottom: associated mass fragments of volatile products measured with OLEMS. Data for pH 7 are shown with blue dotted lines and plotted against the left axis, and data for pH 13 are shown with green solid lines and plotted against the right axis.



**Figure 2.** Top: (100) facet of the copper fcc crystal. Middle: cyclic voltammograms for the reduction of a saturated solution of CO (~1 mM) on Cu(100) in phosphate buffer (pH 7) and NaOH solution (pH 13). Bottom: associated mass fragments of volatile products measured with OLEMS. Data for pH 7 are shown with blue dotted lines and plotted against the left axis, and data for pH 13 are shown with green solid lines and plotted against the right axis.

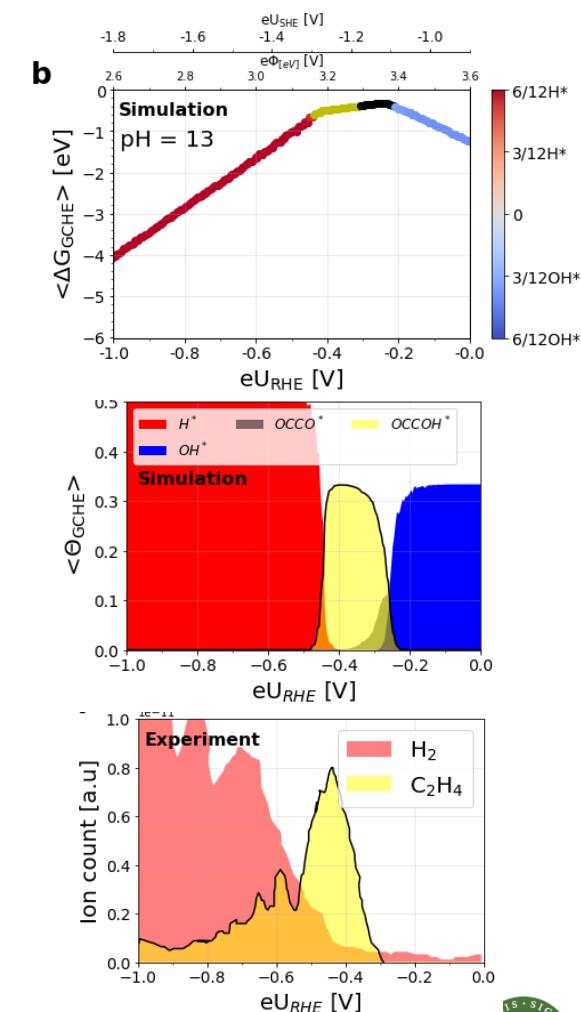
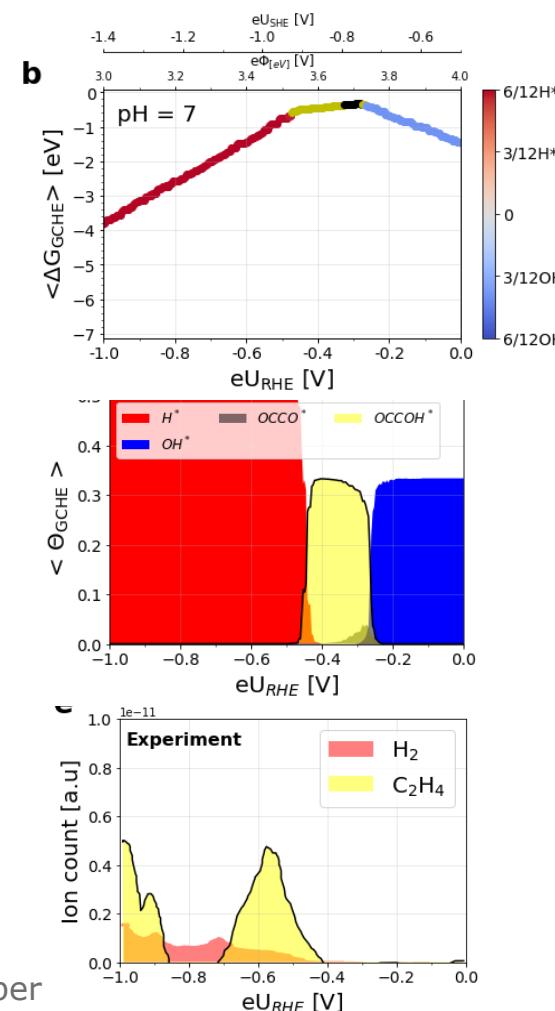
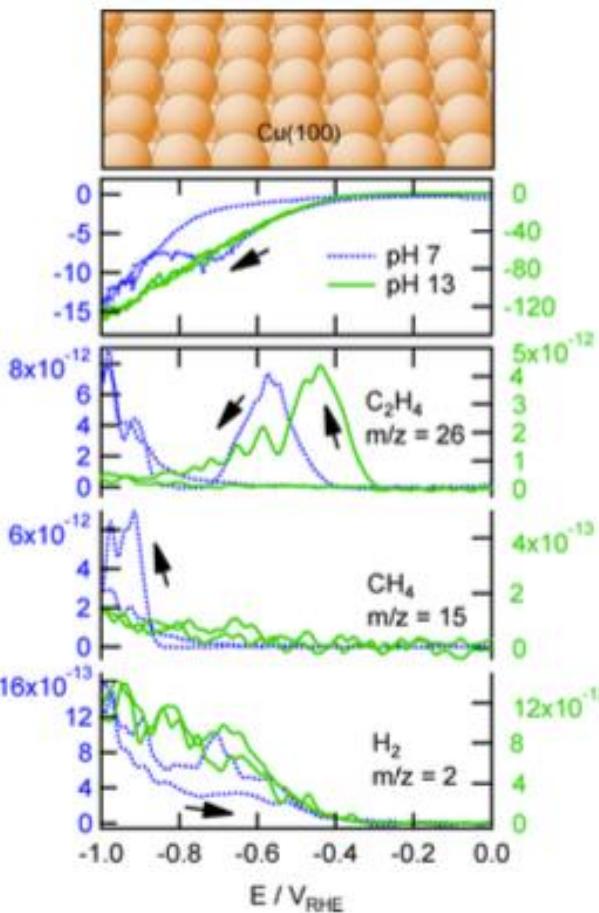


pH 7 = Phosphate buffer

pH 13 = NaOH electrolyte

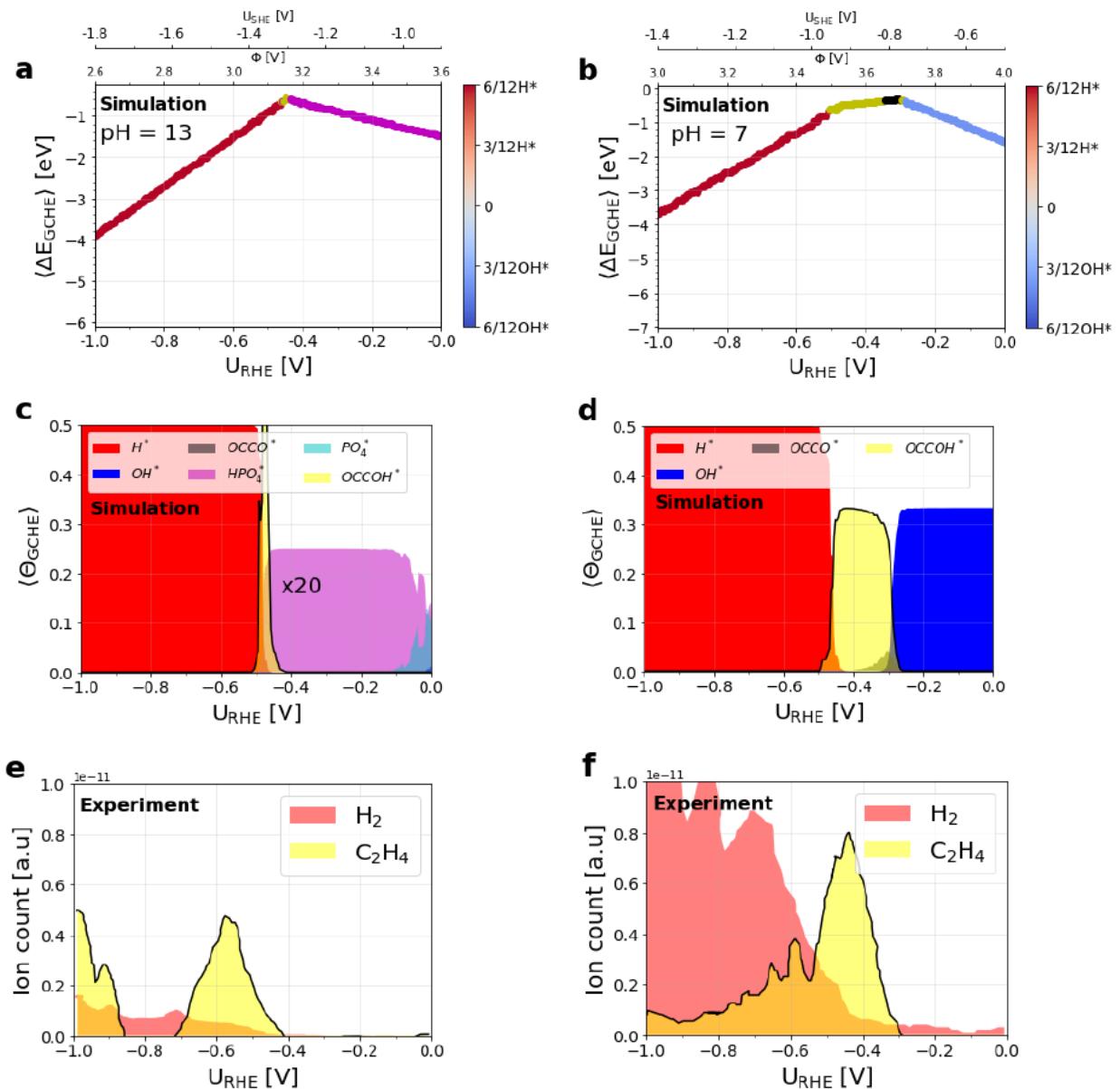
Water Electrolyte

Water Electrolyte



Klaas Jan P. Schouten, ...., Marc M.T. Koper  
J. Am. Chem. Soc. 2012, 134, 9864–9867

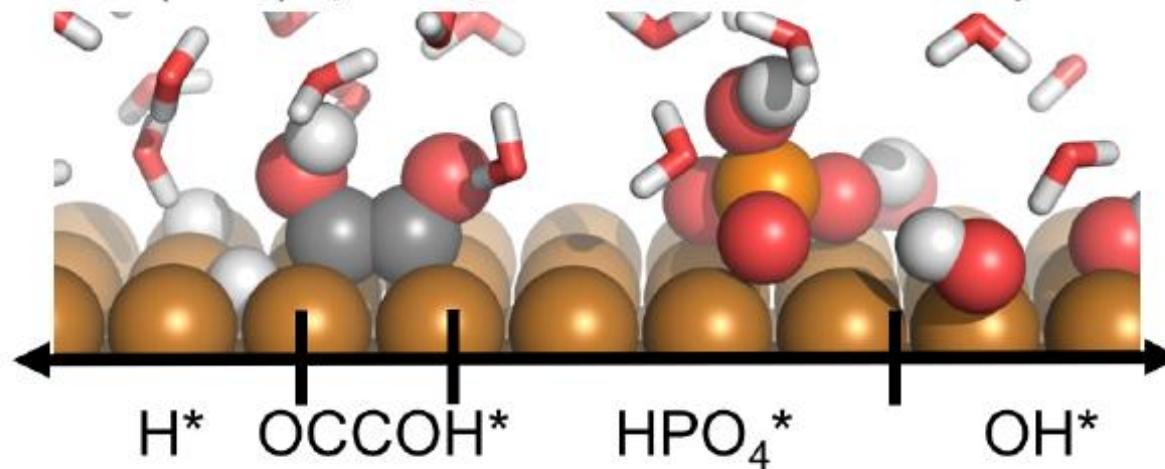
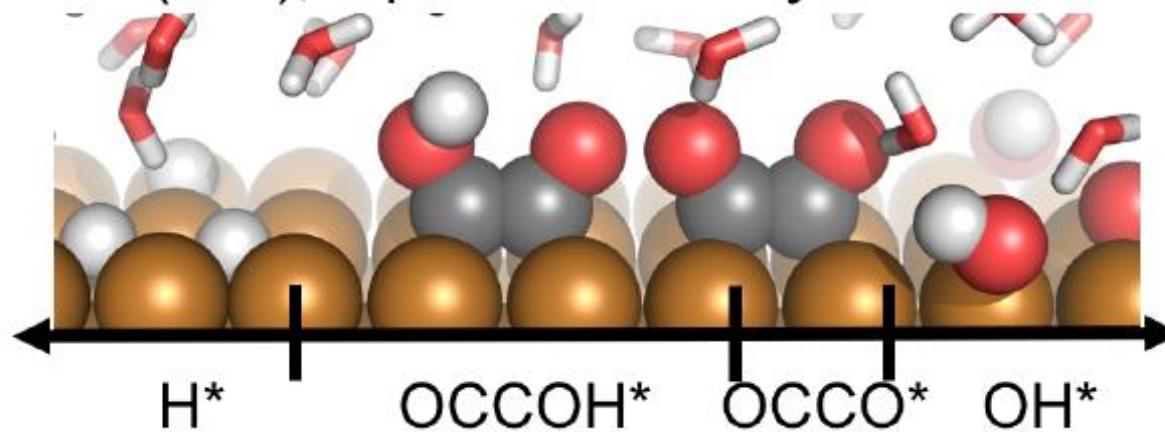




Sted og dato

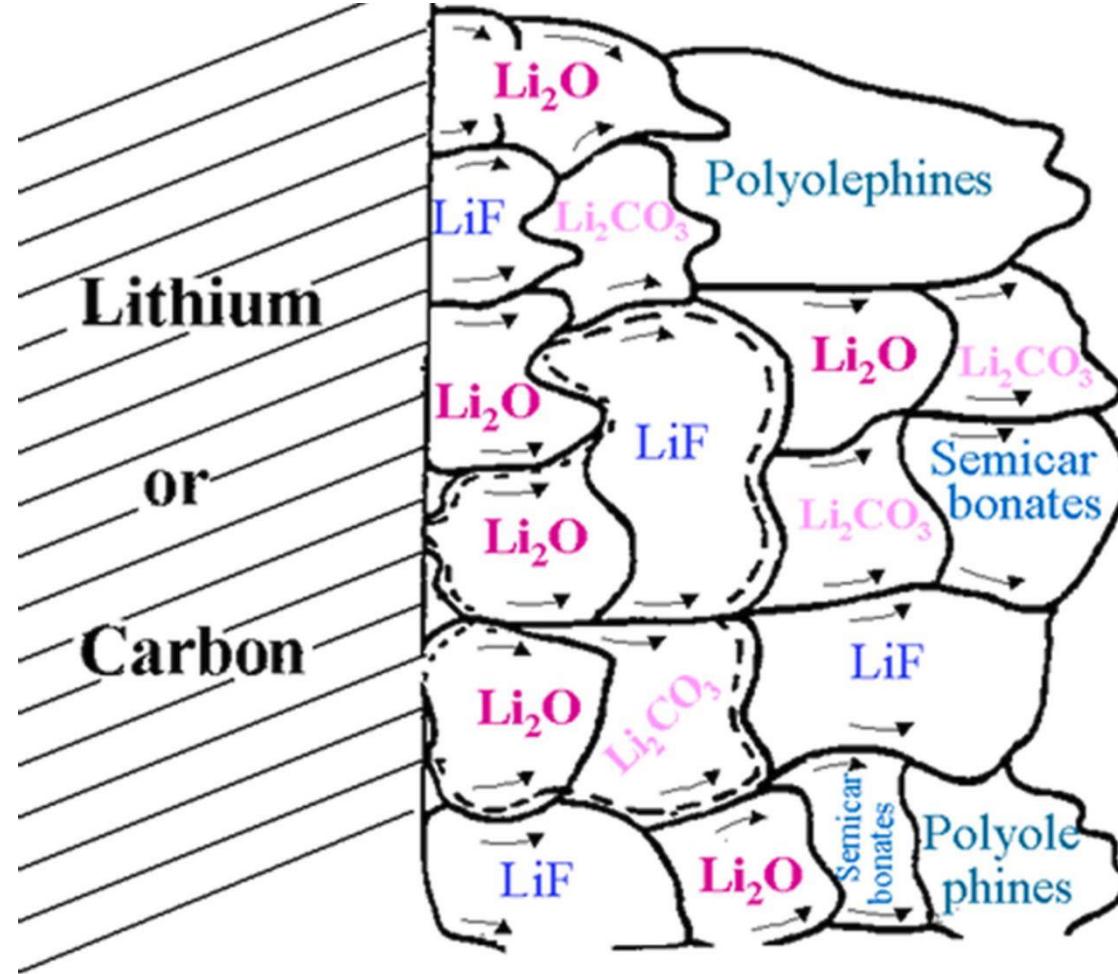
Dias 77



**a Cu(100), phosphate buffer electrolyte****b Cu(100), aqueous electrolyte**

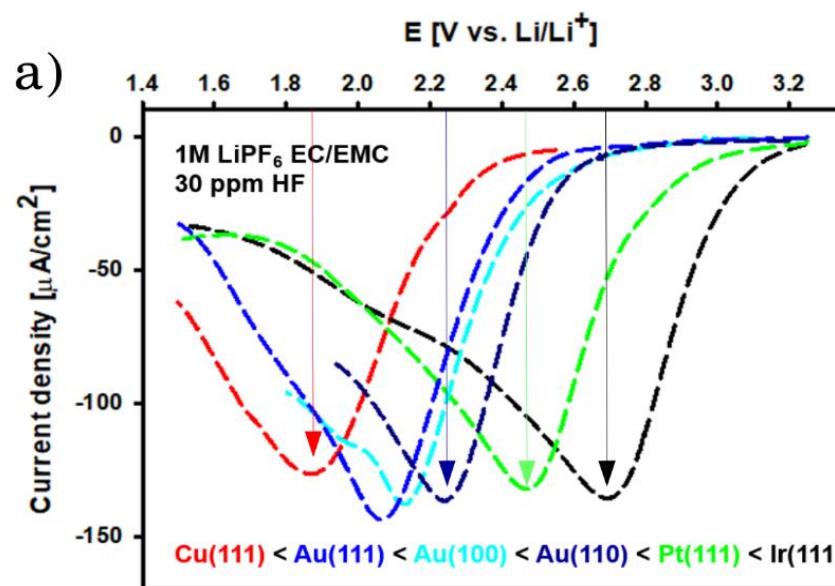
A. Bagger, L. Arnarson, MH. Hansen, E Spohr, J Rossmeisl. submitted

## SEI-layer formation (LiF)



# The Electrochemical Response of Electrodes in LP57

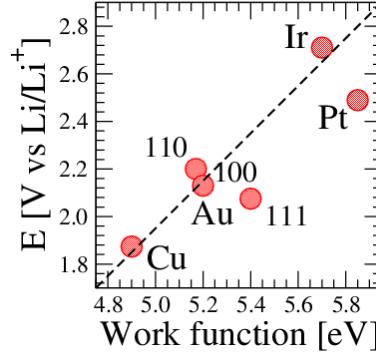
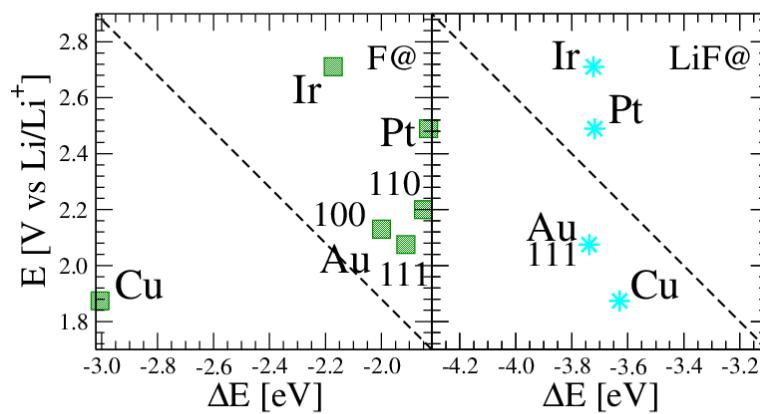
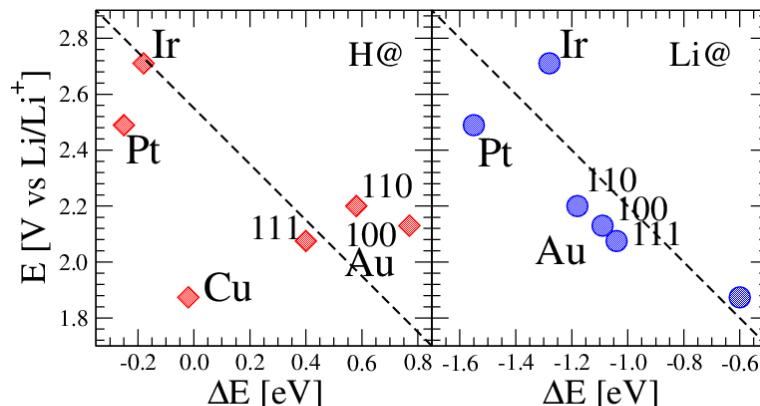
## Voltammetry in LP57



D. Strmcnik, I.E. Castelli, J.G. Connell, D. Haering, M. Zorko, P. Martins, P.P. Lopes, B. Genorio, T. Østergaard, H. Gasteiger, F. Maglia, B.K. Antonopoulos, V.R. Stamenkovic, J. Rossmeisl and N.M. Markovic. *Nature Catalysis* 2018



# Possible Descriptors

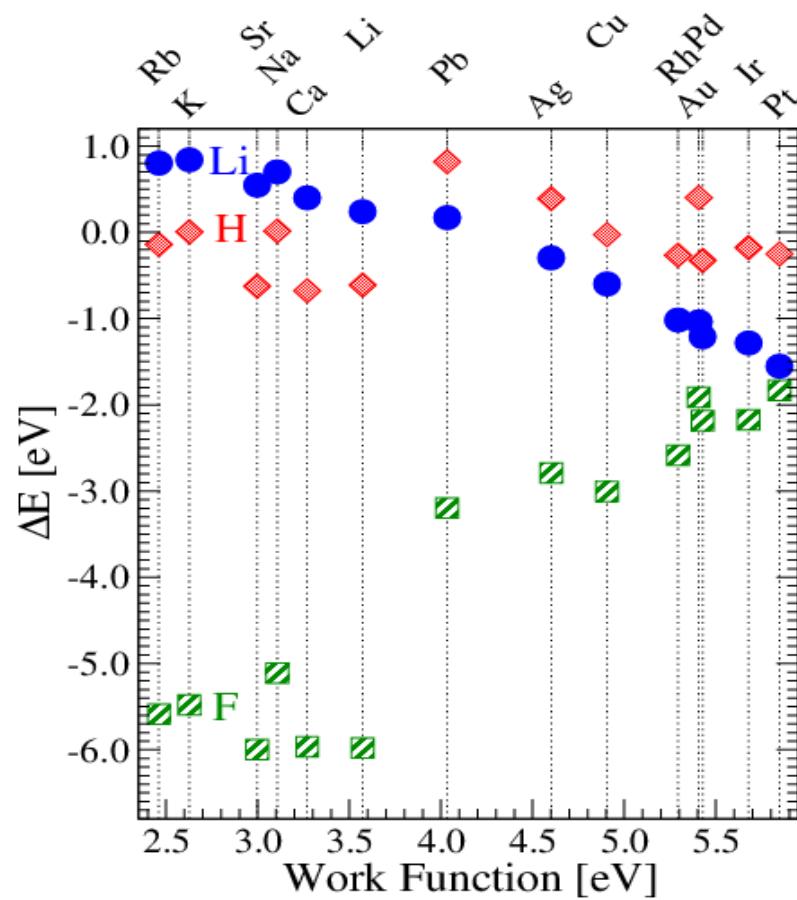


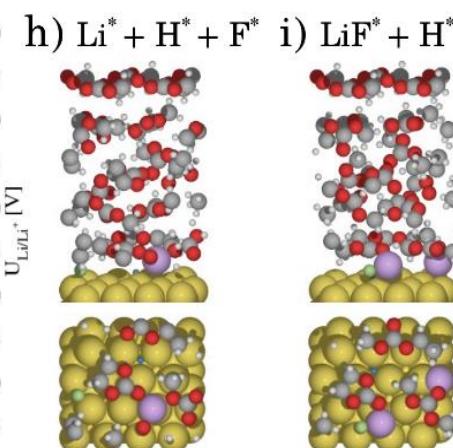
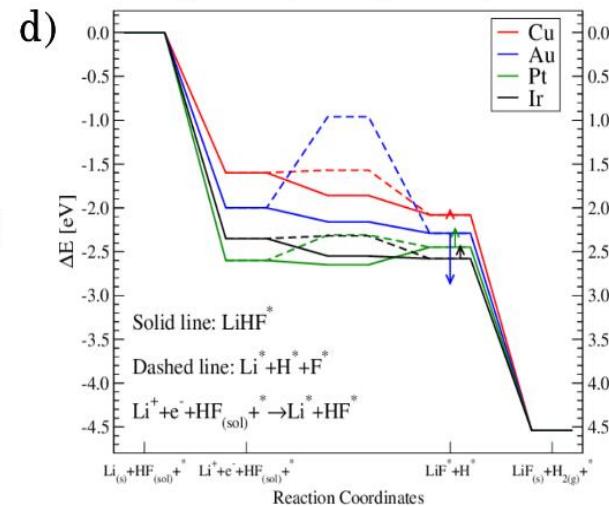
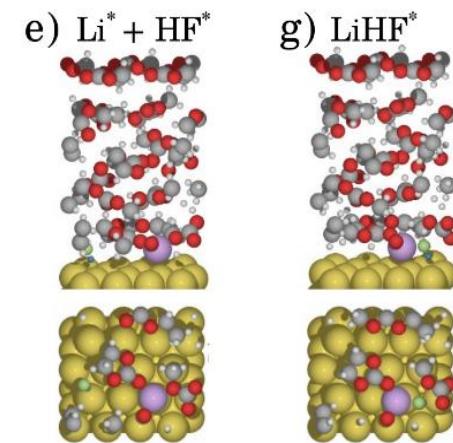
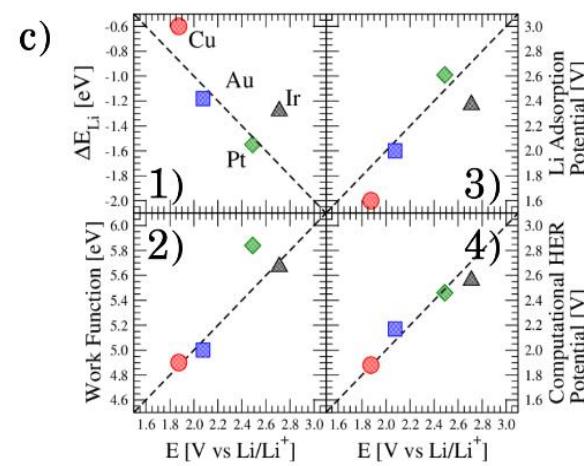
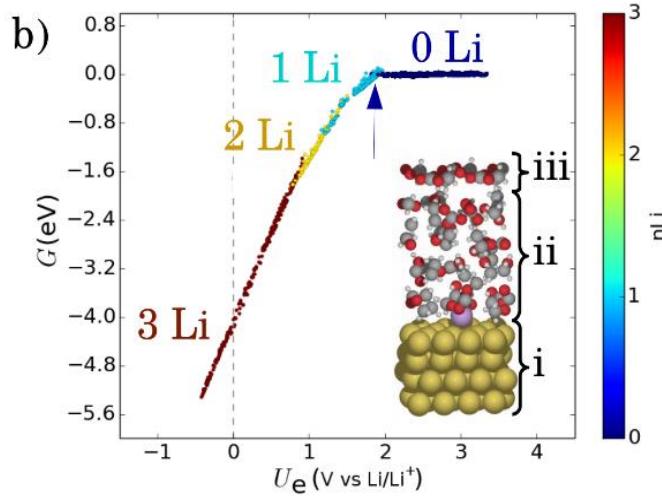
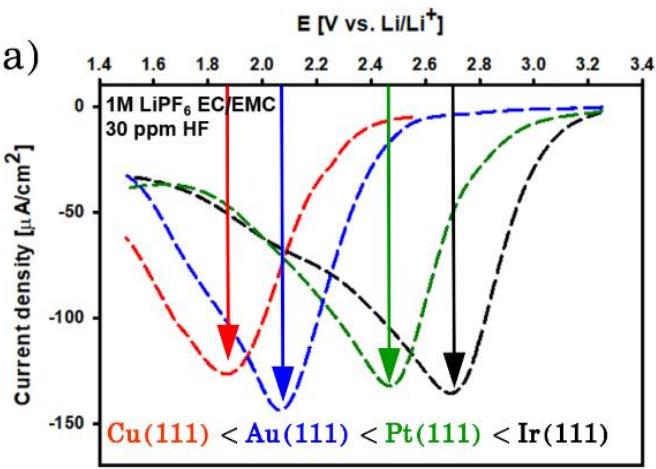
**Adsorption energies and work functions can be descriptors for the electrostatic response.**



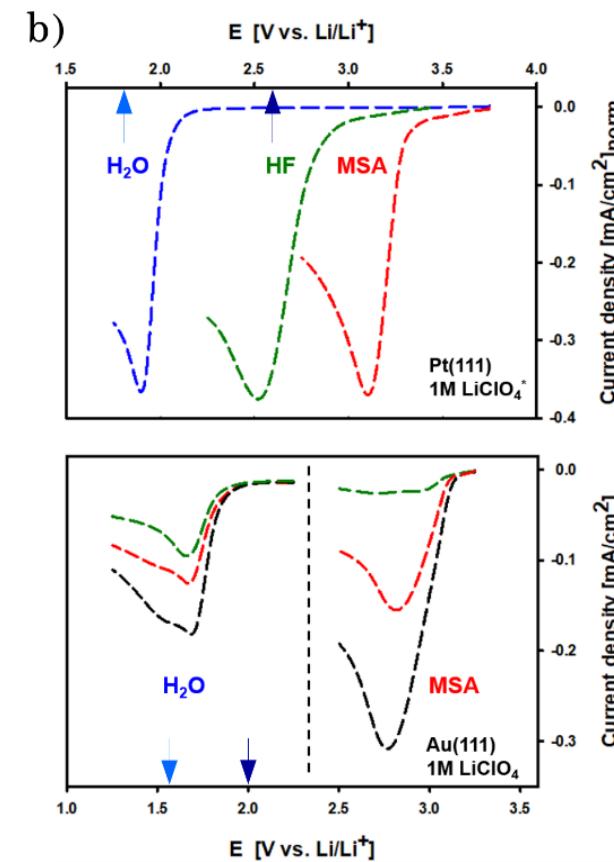
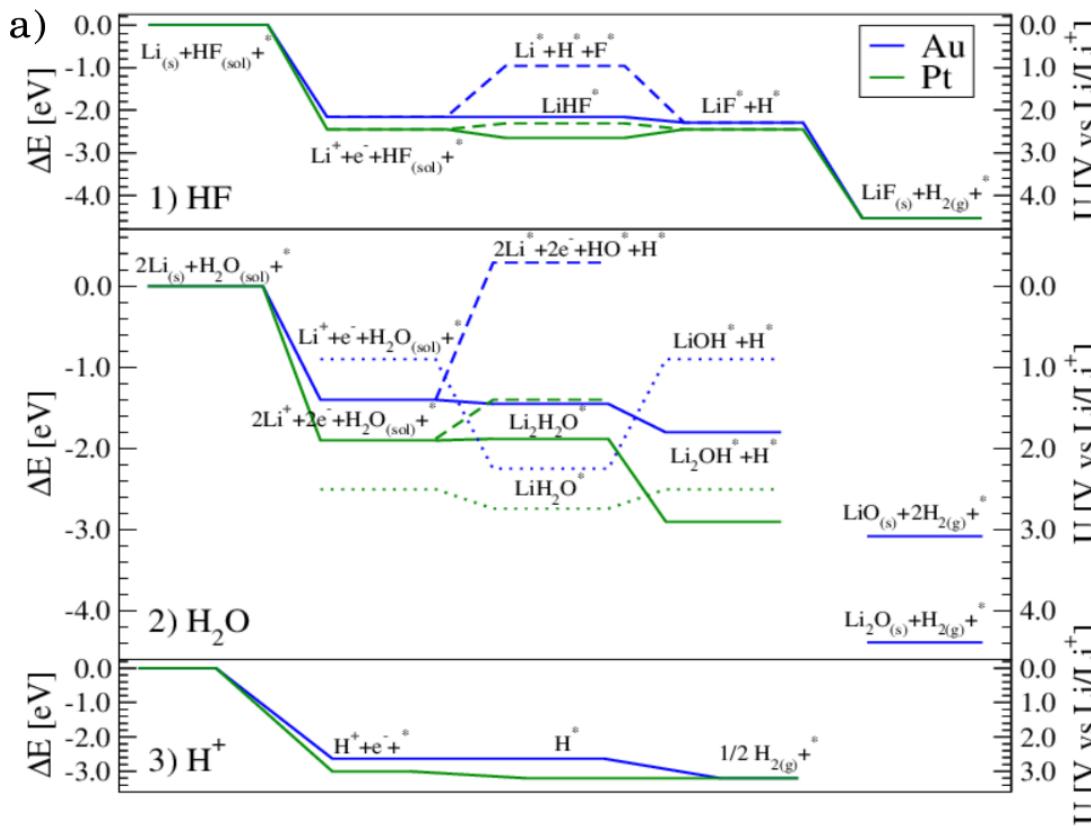
# Adsorption of Li, F, and H on Various 111 Surfaces

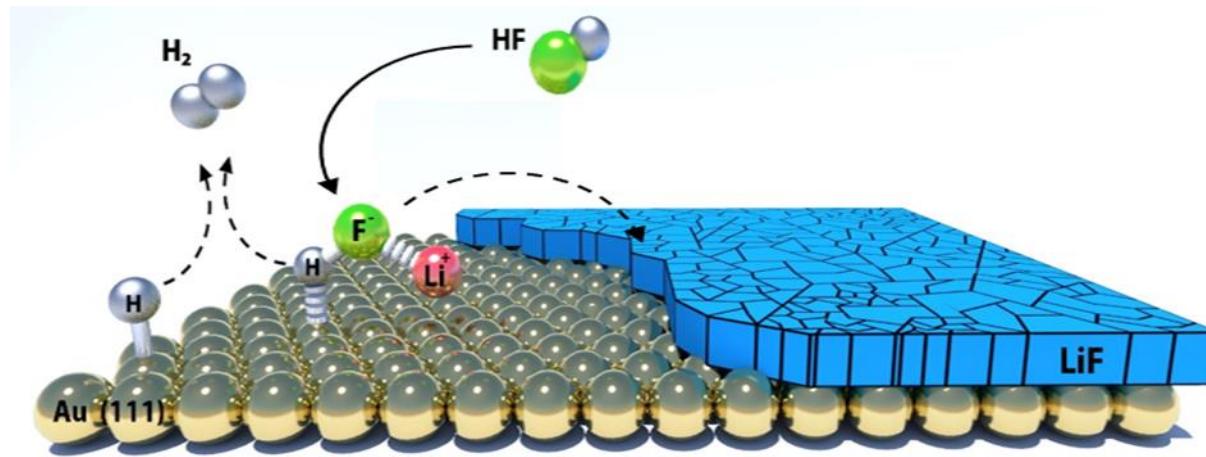
Trends in adsorption energies of **lithium** on various surfaces.  
Comparison with other adsorbates, like **hydrogen** and **fluorine**.





# Other sources of protons.





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# Summary

The Computational Hydrogen Electrode can be generalized to account for pH.

Only standard force/energy calculations.

A posteriori analysis ensures constant chemical potential of protons and electrons.

We obtain the structure of the interface as function of pH and potential.

Which in some cases determine the electrocatalytic properties.



# Questions?

There is only a few protons in the electrolyte don't you have too many protons in the simulations?

Decoupled electron-proton transfer?

Have you included the entropy in the simulations?

Why do you use explicit solvent?

